

# **Leaky Integrate-and-Fire Network Model in Approximating Local Field Potential**

## **Abstract**

The local field potential (LFP) serves as a valuable indicator of neural network activity, reflecting the intricate flow of information within the brain. However, the interpretation of LFP signals can be challenging due to the complex contributions from multiple neural sources. This thesis explores the efficacy of the leaky integrate-and-fire (LIF) network model in approximating LFP signals, offering a computationally efficient yet adaptable framework for modeling brain dynamics. Through a combination of literature reviews, software implementation, and validation procedures, this research investigates the LIF model's potential contributions to the field of neurophysiology.

## **Background**

The local field potential (LFP) is a measure of brain activity that reflects the highly dynamic flow of information across neural networks (Herreras). While this technique of using LFP to investigate brain function in nonhuman animals has been overshadowed by action potential for several years, LFPs have grown in importance in neurophysiological investigations since recent reports suggest that LFPs supplement action potential recordings by indexing activity relevant to EEG, MEG, and hemodynamic (fMRI) signals (Kajikawa). These signals are important because they capture neural processes that are not visible in spiking activity alone, offering insight into how networks of neurons interact, synchronize, and process information. As a result of this emerging interest, efforts to better understand and interpret LFPs have intensified.

## **Literature Review**

There are a few different ways researchers have tried to approximate the LFP from simplified spiking models. One method, from Rasch et al. (2009), uses a linear filter to estimate

LFPs from spike trains. They developed a model that takes the spikes from one or a few neurons and applies a filter to estimate the LFP time course. While this approach works under certain conditions, it relies heavily on the assumption that spike timing alone contains enough information to predict the LFP, which is not always true. It also doesn't account for the continuous synaptic currents that are actually generating the extracellular signal.

Another method, proposed by Telenczuk et al. (2020), is based on the concept of unitary LFPs (uLFPs), which is the signal generated by a single neuron's output. Their kernel-based model uses recorded or simulated uLFPs as templates and then convolves those with spike trains to estimate the total LFP. This method can be applied to point-neuron models, but it still uses spikes as input rather than synaptic currents. That makes it slightly more abstract, since it doesn't directly model the sources of the LFP.

In contrast, Mazzoni et al. (2015) developed a proxy that is based directly on synaptic currents, which are the main drivers of the LFP. Their method starts by running a simulation of a LIF network to get the AMPA (excitatory) and GABA (inhibitory) currents. These currents are then injected into a realistic 3D model of a cortical column with morphologically detailed neurons to compute a ground-truth LFP. From there, they derived a function — the Weighted Sum LFP (WSLFP) — that approximates the LFP using only the AMPA and GABA currents from the LIF network.

This model is useful and stand-out because it is both efficient and biologically grounded. It captures the core features of the LFP without needing a full biophysical simulation every time. The function is a weighted sum of the synaptic currents, and the weights can be adjusted depending on the spatial arrangement of the neurons or other factors. This makes the model easy to reuse in different network configurations without affecting the spiking dynamics.

## Experiment Methods

Our research focused on implementing the WSLFP model proposed by Mazzoni et al. (2015) in a Python-based software package. The research methodology followed a structured approach centered on coding, testing, and validating our implementation to ensure that it correctly reproduced the expected behavior of the WSLFP calculation. The core function used to approximate the LFP in our implementation is based on the WSLFP model from Mazzoni et al. (2015), shown in the equation below. This formula expresses the LFP signal as a function of synaptic currents, where AMPA and GABA currents from pyramidal neurons are summed and weighted. The first part of the function represents the spatial scaling factor based on the electrode's position, while alpha scales the inhibitory GABA contribution. The normalization function ensures the correct unit scaling of the computed LFP. Our research involved implementing this model in Python and validating it against the expected theoretical outputs.

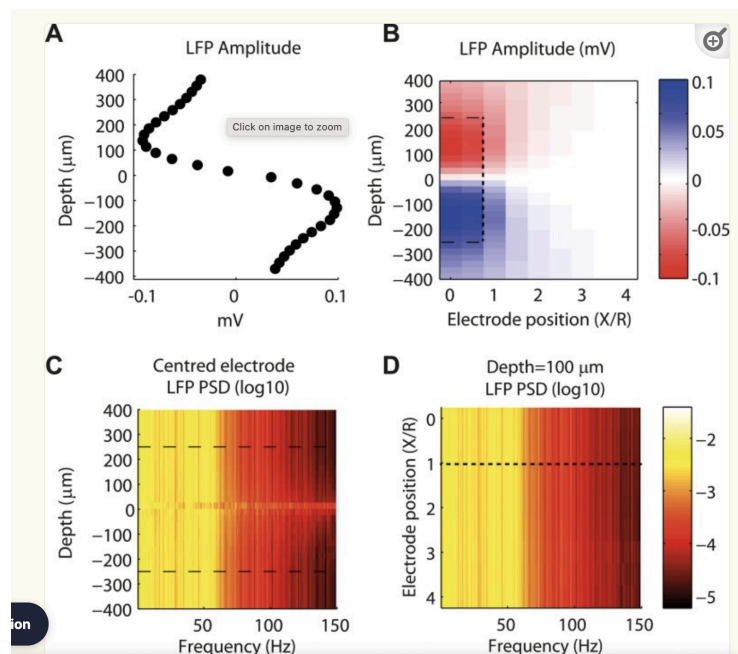
$$LFP_{ws}(r, d, t) = f_{ws}(r, d) * Norm \left[ \sum_{pyr} AMPA(t - \tau_{AMPA}) - \alpha \left( \sum_{pyr} GABA(t - \tau_{GABA}) \right) \right]$$

To verify our implementation, a suite of unit tests was developed to validate the expected behavior of key functions and ensure the overall correctness of the WSLFP model. These tests provided a consistent framework for identifying potential issues with input handling and output shape. The test cases covered input conditions, including different combinations of AMPA and GABA synaptic currents, randomized source and electrode coordinates, and edge cases involving numerical instability or empty arrays. The tests also included checks for spatial and temporal behavior, such as verifying that electrodes positioned closer to neurons produced stronger signals and that signal amplitude changed appropriately with depth. Time-dependent tests evaluated whether LFP values increased consistently with later evaluation points, as expected from the

weighted sum formulation. In addition, boundary conditions were tested to confirm that AMPA times occurred sufficiently in advance of the evaluation times and that the function correctly raised exceptions when inputs were out of range or malformed.

The final implementation was documented in a demonstration notebook, illustrating the practical usage of our software package. This ensures that other researchers can easily use, modify, and build upon our implementation.

Since our study was focused on software development and implementation, rather than conducting new neuroscience experiments, data collection was minimal. Our results primarily serve as a replication and verification of the Mazzoni et al. (2015) method within a computational framework.



## Data

This image, adapted from Mazzoni et al. (2015), provides insights into the characteristics of simulated LFPs within a three-dimensional (3D) neural network as a function of both depth and lateral position relative to the network's center.

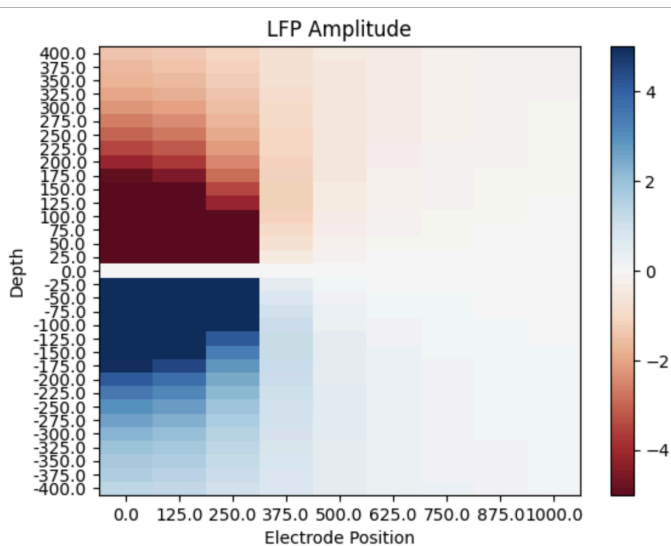
(A) It illustrates the LFP signal's amplitude, measured as the standard

deviation of the signal over 10 seconds, resulting from a thalamic input of 1.5 spikes per millisecond at intervals of 50 μm in depth. The dashed lines demarcate the network's spatial boundaries, which extend from -250 μm to 250 μm along the lateral dimension.

(B) This plot displays the LFP signal's amplitude across various depths and distances from the network's center, measured in units of the network's radius ( $R = 250 \mu\text{m}$ ). The dashed lines distinguish between regions inside the network (where  $X/R \leq 1$  and  $-250 \mu\text{m} < d < 250 \mu\text{m}$ ) and outside the network.

(C) It presents the Power Spectral Density (PSD) of the LFP signal at the network's central location for different depths, again with dashed lines indicating the network boundaries within a range of  $-250 \mu\text{m}$  to  $250 \mu\text{m}$  in depth.

(D) Here, the PSD of the LFP signal is depicted at varying distances from the center of the 3D network, focusing on a reference depth of  $100 \mu\text{m}$ . The dashed line signifies the boundary of the network at  $X/R = 1$ .



This is the result that was generated by my research partner, Olivia Klemmer, for the graphing portion of our research. The data was extracted from the original figure in the Mazzoni et al. (2015) paper and re-plotted to create this graph. The provided graphs were generated using Matplotlib to replicate certain results relevant to your research.

Since our research primarily involves implementing functions in Python, these graphs serve as a reference or benchmark to test the accuracy of the implemented functions. It aligns with the graphs in the original paper (seen above), which asserts the function implemented should be correct.

## **Discussion**

In this study, we implemented and tested the WSLFP model proposed by Mazzoni et al. (2015) to estimate LFP signals from LIF network models. Our primary objective was to ensure that our software correctly replicated the mathematical framework and computational methodology outlined in their work. Rather than validating the effectiveness of their approach in a broader sense, we focused on confirming that our implementation accurately reproduced the expected computational behavior.

## **Accuracy of Implementation**

A critical component of our study was verifying whether our Python-based implementation of the WSLFP model produced results consistent with the theoretical expectations from the Mazzoni paper. The result of the research closely aligns with those reported in the original research, confirming the robustness of the mathematical formulation when implemented in software. This successful replication suggests that the weighted sum approach effectively captures key aspects of LFP generation in point-neuron network models.

## **Limitations**

However, it is important to note the inherent limitations of our study. The main part of the limitation is our reliance on the assumptions and parameters outlined in the original Mazzoni research. While these parameters provided a structured framework for our replication, they also constricted the scope of our inquiry. This means that while we verified our implementation's correctness, we did not critically assess the limitations of the WSLFP model itself.

## **Future Directions**

The horizon of our research does not end here. Drawing from the implementation and the limitations identified, we propose several avenues for future exploration:

1. Sensitivity Analyses: A systematic sensitivity analysis could explore how variations in network architecture, synaptic weight distributions, and electrode placement affect the computed LFP. This would provide insight into the robustness of the WSLFP model under different conditions.

2. Comparisons with Alternative Models: While our study focused on implementing the WSLFP model, other LFP approximation techniques, such as kernel-based methods (Telenczuk et al., 2020) or linear estimation models (Rasch et al., 2009), could be tested for comparison. Understanding the trade-offs between these approaches would offer a clearer picture of when the weighted sum approximation is most useful.

## **Conclusion**

This study successfully implemented the WSLFP model proposed by Mazzoni and verified its computational accuracy through systematic testing. By replicating the mathematical framework in Python, we demonstrated that the model is both computationally feasible and suitable for simulating LFPs in large-scale neural networks. While our work primarily focused on software implementation, it underscores the importance of computational approaches in neuroscience for modeling neural dynamics. Future research should explore sensitivity analyses, alternative modeling approaches, and empirical validation to enhance the accuracy and applicability of LFP estimation methods. As computational neuroscience continues to evolve, refining these models will contribute to a deeper understanding of brain activity and its broader implications in broader fields.

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