

GEORGIA INSTITUTE OF TECHNOLOGY  
OFFICE OF CONTRACT ADMINISTRATION  
SPONSORED PROJECT INITIATION

*add*

Date: DECEMBER 14, 1976

Project Title: HYDROTHERMAL CIRCULATION ON MID-OCEAN RIDGE CRESTS

Project No: G-35-625

Project Director: DR. R. P. LOWELL

Sponsor: NATIONAL SCIENCE FOUNDATION

Agreement Period: From 1/1/77 Until 12/31/79  
24 MONTH BUDGET PERIOD PLUS 6 MONTHS FOR SUBMISSION OF  
REQUIRED REPORTS, ETC.

Type Agreement: GRANT NO. OCE-76-81876

Amount: \$37,200 NSF  
5,573 GIT(G-35-323)  
\$42,773 TOTAL

Reports Required: ANNUAL LETTER TECHNICAL FINAL REPORT

Sponsor Contact Person (s):

Technical Matters

Contractual Matters

(thru OCA)

MR. GAYLORD L. ELLIS  
GRANTS OFFICER  
NATIONAL SCIENCE FOUNDATION  
WASHINGTON, D. C. 20550  
(202) 632-5965

Defense Priority Rating:

Assigned to: GEOPHYSICAL SCIENCE (School/Laboratory)

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Project Code (GTRI)  
Other \_\_\_\_\_

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GEORGIA INSTITUTE OF TECHNOLOGY  
OFFICE OF CONTRACT ADMINISTRATION  
SPONSORED PROJECT TERMINATION

Date: January 29, 1981

Project Title: Hydrothermal Circulation on Mid-Ocean Ridge Crests

Project No: G-35-625

Project Director: Dr. R. P. Lowell

Sponsor: National Science Foundation

Effective Termination Date: 12/31/79

Clearance of Accounting Charges: 12/31/79

Grant/Contract Closeout Actions Remaining:

- ☐ Final Invoice and Closing Documents
- ☒ Final Fiscal Report VIA FCTR
- ☒ Final Report of Inventions
- ☐ Govt. Property Inventory & Related Certificate
- ☐ Classified Material Certificate
- ☐ Other \_\_\_\_\_

Assigned to: Geophysical Science (School/~~Laboratory~~)

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EES Information Office  
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Project Code (GTRI)  
Other C. E. Smith

61-30-645

GEORGIA INSTITUTE OF TECHNOLOGY  
SCHOOL OF GEOPHYSICAL SCIENCES

Atlanta, Georgia 30332  
(404) 894-2857

Central Processing Station  
National Science Foundation  
Washington, D.C. 20550

Attention: Dr. Donald F. Heinrichs, Director  
Submarine Geology and Geophysics Program  
Oceanography Section  
Division of Ocean Sciences

Subject: Annual Technical Letter Report on Research Proposal  
entitled "Hydrothermal Circulation on Mid-Ocean Ridge  
Crests" for the period January 1, 1977 to December  
31, 1977. Grant # OCE-76-81876

Dear Dr. Heinrichs:

The following briefly summarizes the research accomplished, personnel supported, and papers written during the past year.

RESEARCH

Over the past year, we have concentrated upon modifying and improving the finite difference models which we had developed (Lowell and Patterson, 1978). We have tried to investigate the effect of a radiative upper boundary condition, the effect of topography, and the effect of sedimentary cover. To date we have been only partially successful.

A. The Radiative Condition

The numerical models of Lowell and Patterson (1978), and Fehn et al. (1977) have used an isothermal upper boundary condition. This means that convection merely acts to redistribute the conductive heat flux through the surface and, in the case of Lowell and Patterson's transient model, gives an increased total heat flux through the surface. There are no undetectable

"convective" losses. We have attempted to rectify this situation by applying a radiative temperature condition at the ocean floor. For reasonable values of the heat transfer coefficient, and a permeability of the order of 0.01 Darcy, the ratio of convective to conductive flux was small, and the "near zero" heat flux values which are often measured near ocean ridge axes are not accounted for.

This suggests that permeability near ridge axes must be significantly greater than 0.01 Darcy, in order for free convection to give rise to large scale convective losses. High permeabilities may be due to large scale fracturing as suggested by Lowell (1975) or Wolery and Sleep (1977) or, perhaps, to the penetration model of Lister (1974). Another alternative is that the flow is a topography-driven forced convection, rather than free convection. Some of these results (Lowell et al., 1977) were presented at a symposium sponsored by the Geophysics Division of the Geological Society of America and held at the Society's Annual Meeting in Seattle, November 7-9, 1977. The symposium was organized by P.A. Rona and myself. A summary report of the symposium has been submitted for publication (Rona and Lowell, 1978).

#### B. Effect of Topography

The presence of an irregular upper boundary adds a driving force to the convection by generating both a horizontal temperature gradient and, in the case of an open upper surface, a horizontal pressure gradient. We have attempted to model the temperature effect of the irregular topography of ocean ridges by considering convection with a horizontal temperature gradient on the upper surface. We have encountered severe numerical difficulties and have not yet obtained useful results. The work is continuing.

C. Effect of Sedimentary Cover

We have just initiated some work on the effect of an impermeable layer of sediment overlying the oceanic crust. The goal is to find out whether the presence of convection in the crust can be deduced from heat flow measurements in the sediment. That is, what thickness of sediment is required to smooth the heat flux beyond detection.

BIBLIOGRAPHY

- Fehn, U., L.M. Cathles, and H.D. Holland, 1977, Hydrothermal convection at mid-ocean ridges, EOS, 58, 514.
- Lister, C.R.B., 1974, On the penetration of water into hot rock, Geophys. J. Roy. Astr. Soc., 39, 465-509.
- Lowell, R.P., 1975, Circulation in fractures, hot springs and convective heat transport on ocean ridge crests, Geophys. J. Roy Astr. Soc., 40, 351-365.
- Lowell, R.P., P.L. Patterson, and J.K. Fulford, 1977, Numerical modeling of hydrothermal circulation at slow spreading ridges, Geol. Soc. Am. Annual Meeting Program with Abstracts, 9, No. 7, p. 1075-1076.
- Lowell, R.P. and P.L. Patterson, 1978, Numerical models of hydrothermal circulation at an ocean ridge axis, submitted to The Dynamic Environment of the Sea Floor, ed by F.T. Manheim and K. Fanning.
- Rona, P.A. and R.D. Lowell, 1978, Symposium: Hydrothermal systems at oceanic spreading centers - a report, submitted to Geology.
- Wolery, T.J. and N.H. Sleep, 1977, The egress of hydrothermal fluid at mid-oceanic ridges, Geol. Soc. Am. Annual Meeting Program with Abstracts, 9, No. 7, p. 1233-1234.

STUDENTS SUPPORTED

Mr. James K. Fulford, Aug., 1976 to present. Mr. Fulford has been doing the finite difference modeling as discussed above. This work will form the bulk of his M.S. thesis, which he expects to complete by June, 1978.

PAPERS

Lowell, R.P., P.L. Patterson, and J.K. Fulford, 1977, Numerical modeling of hydrothermal circulation at slow spreading ridges, Geol. Soc. Am. Annual Meeting Program with Abstracts, 9, No. 7, p. 1075-1076.

Rona, P.A. and R.P. Lowell, 1978, Symposium: Hydrothermal systems at oceanic spreading centers - a report, submitted to Geology.

Respectfully submitted,

Robert P. Lowell  
Principal Investigator

ANNUAL TECHNICAL LETTER REPORT

G-35-625

SUBMITTED BY: Robert P. Lowell

DATE: May, 1979

TITLE: Hydrothermal Circulation on Mid-Ocean Ridge Crests

GRANT PERIOD: 1/1/77 to 6/30/79

FUNDED AMOUNT: \$37,200

PRINCIPAL INVESTIGATOR: Robert P. Lowell  
School of Geophysical Sciences

GRANTEE: Georgia Institute of Technology  
Atlanta, Georgia 30332

REPORT PERIOD: 1/1/78 to 12/31/78 (A)

This work has been supported by the National Science Foundation,  
Division of Ocean Sciences, under grant no: OCE-76-81876

## Introduction

Below is a progress report for NSF grant OCE-76-81876. It outlines the main research results for the 1978 calendar year and indicates the principal thrust of the 1979 progress. During 1978 Mr. James K. Fulford and Ms. Patricia L. Patterson were supported on this research grant. Mr. Fulford completed his M.S. thesis in Fall, 1978 and entered a Ph.D. program in Atmospheric Sciences. Ms. Patterson is currently working on her doctoral research under this grant.

## Objectives of Proposed Research

The objective of the proposed research is to develop reasonable models for hydrothermal circulation in the oceanic crust. The results of these models will be used to interpret observed heat flow patterns at the ocean floor. Such calculations may also provide a key to some aspects of the chemistry of basalt-sea water interactions. The work involves both analytical and numerical modeling.

## Results to date: January 1, 1978 - December 31, 1978

Over the past year, the initial numerical modeling efforts (Patterson, 1976; Lowell, et al., 1977; Patterson and Lowell, 1979) were continued. These efforts have concentrated on the effects of a radiative boundary condition on near axis convection, on the effects of sediment cover, and on the effects of topography. Also, a volume for the series Benchmark Papers in Geology entitled Oceanic Spreading Centers: Hydrothermal Systems, has been prepared in conjunction with Peter Rona.

### A. The Radiative Condition

Ocean ridge convection models which have used an isothermal upper boundary do not permit convective heat transfer across the rock-water interface and hence are not realistic. The early models which we have developed for near axis convection (Patterson, 1976; Patterson and Lowell, 1979) are of this type as are others in the literature (e.g. Fehn and Cathles, 1978). We have attempted to remedy this problem by applying a radiative condition at the upper surface, however, for values of the permeability of  $10^{-10}$  cm<sup>2</sup> or less, the ratio of convective to conductive heat flux remains small. This suggests that the permeability near the axis must be substantially greater than  $10^{-10}$  cm<sup>2</sup> and probably arises from large scale discrete fractures (e.g. Lowell, 1975; Sleep and Woley, 1978) this result is discussed further in Fulford (1979).

### B. Effect of Sediment Cover

A second numerical problem which was investigated was the problem of the sealing of a convection system by a sedimentary layer of low permeability. The questions to be answered were: (1) What sedimentary thickness/permeability ratios are required to prevent significant fluid exchange across the ocean floor? (2) In the absence of significant fluid exchange, would the convection in the underlying basalt be detectable in conductive heat flow measurements in the overlying sediments?



To answer these questions, the pertinent steady state heat and mass transfer equations were solved by finite differences in a two layer square porous block of dimension  $h$ . The upper surface was isothermal and overlain by a free-standing column of fluid; the bottom was rigid with a constant inward heat flux  $q = 10 \text{ cal/cm}^2\text{-s}$ ; the sides were rigid and insulated. The permeability of the lower, basalt layer was assumed to be  $10^{-10} \text{ cm}^2$  and the upper, sediment layer was assumed to have a permeability of either  $10^{-11} \text{ cm}^2$  or  $10^{-12} \text{ cm}^2$ . The thickness of sediment was varied from 0.4 to 1.6 km, the basaltic layer decreasing in depth as sediment increased so that  $h$  remained at 5 m. The physical properties of the fluid, rock, and sediment were assumed to be constant. The cases modeled are listed in Table 1, and the pertinent results are shown in Figures 1, 2, and 3.

Figure 1 shows the reduction in fluid exchange across the sediment-water boundary as a function of sediment thickness for the two assumed values of sediment permeability. Both curves show a rapid decrease in the fluid exchange rates as thickness increases, the rate of decrease of fluid exchange gradually flattening out at large sediment thicknesses. The results show (a) the smaller the sediment permeability, the greater the reduction in fluid exchange, and (b) for a given permeability, the amount of reduction becomes independent of sediment thickness at large thicknesses. Result (b) is generally in accord with the result of Skilbeck and Anderson (1979) who derive the sealing condition:

$$K_s/K_b \ll \tanh \lambda d$$

where  $d$  is the sediment thickness and  $\lambda$  is the horizontal wave number of the convection cell. Thus as  $d$  gets larger, the condition becomes independent of the sediment thickness. Curve (b) indicates that a sediment thickness of about 1 km and permeability  $10^{-12} \text{ cm}^2$  reduces the fluid exchange across the sea floor by almost two orders of magnitude ( $\sim 98\%$ ).

Figures 2 and 3 show corresponding results for the smoothing of the horizontal variation in conductive heat flux over a cell wavelength. The principal result is that even though the fluid exchange is effectively curtailed, a horizontal heat flux variation is still perceptible. It must be pointed out, however, that the assumed heat flux is quite high and the sediment was assumed to have the same thermal conductivity as basalt. Modifications in these parameters is likely to adversely affect the perceptibility of convection beneath a thick sedimentary cover by means of shallow thermal conduction measurements.

Further details on the effects of sedimentary cover on convection are given in Fulford (1979).

### C. Effects of Topography

The presence of irregular surface topography at the ocean floor, even if the topography is overlain partially or completely with sediments, may influence the pattern of hydrothermal circulation (Lister, 1972). The topography in effect gives rise to horizontal temperature gradients which tend to decrease the fluid buoyancy under

Table 1. Cases Modeled;2

Case	NK	K <sub>1</sub>
1	0	
2a	.4	10 <sup>-11</sup>
2b	.8	
2c	1.2	
2d	1.6	
3a	.4	10 <sup>-12</sup>
3b	.8	
3c	1.2	
3d	1.6	

Explanation:

NK is depth of sediments in km.

K<sub>1</sub> is sediment permeability in cm<sup>2</sup>.

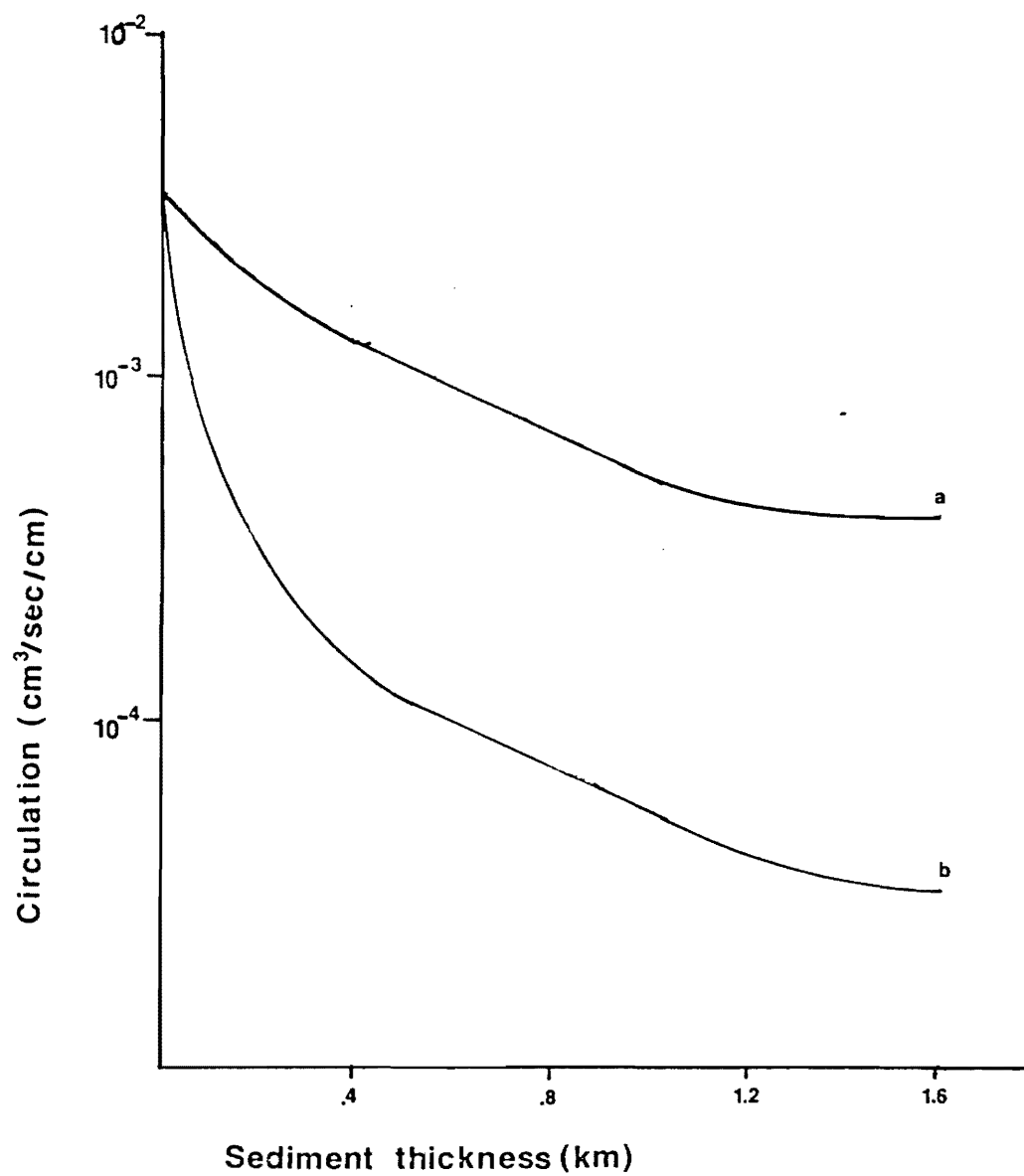


Figure 1. Circulation of fluid versus sediment thickness for sediment of permeability  $10^{-11}$  cm<sup>2</sup> (curve a), and for sediment of permeability  $10^{-12}$  cm<sup>2</sup> (curve b).

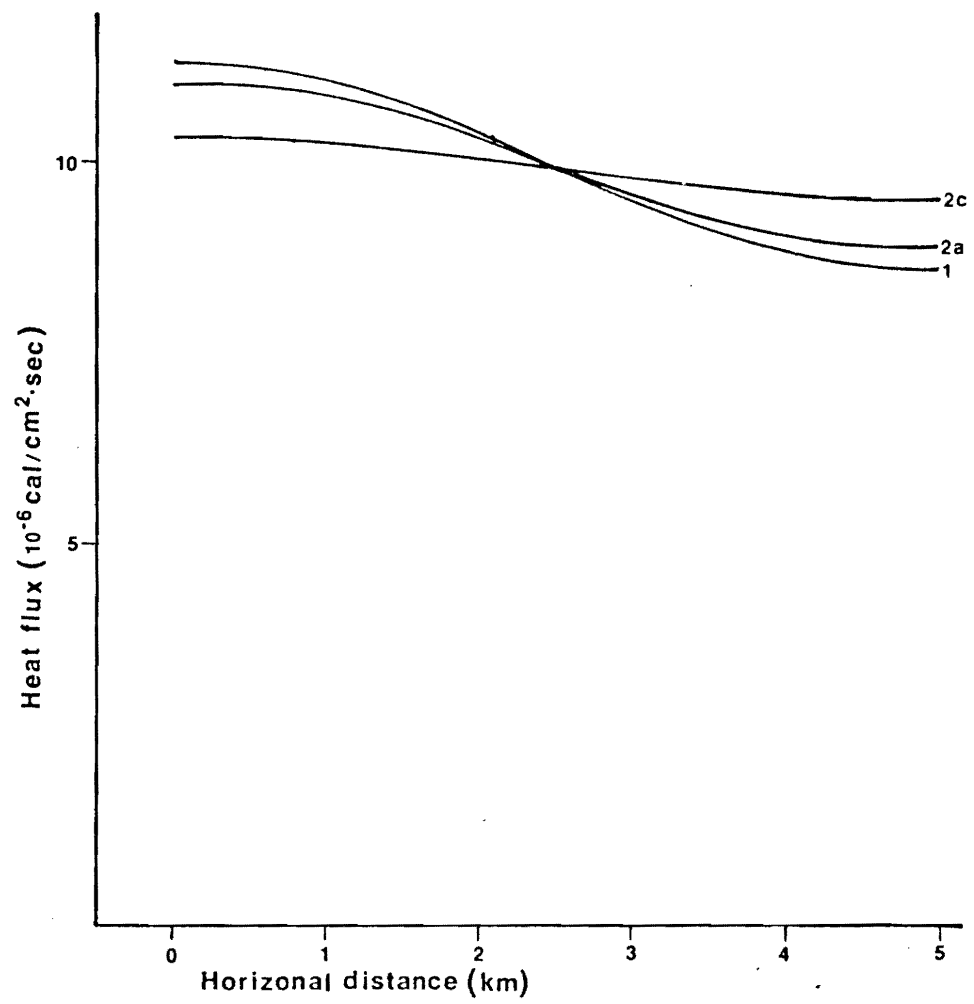


Figure 2. Comparison of surface conductive heat flux for case 2a, 2c, and 1.

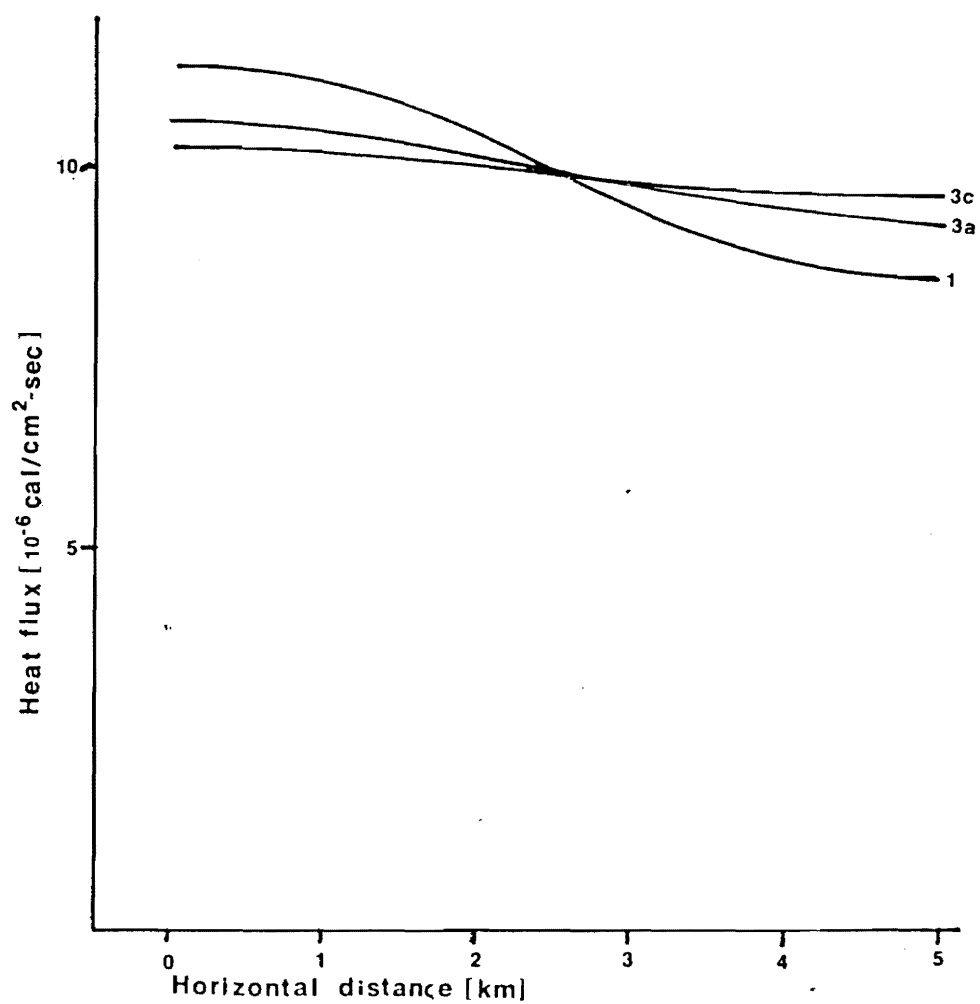


Figure 3. Comparison of surface conductive heat flux for case 3a, 3c, and 1.

regions of low topography and increase the fluid buoyancy under regions of elevated topography. Thus topography may partially control the sites of ascending and descending fluid. Moreover, since the fluid is unconditionally unstable under the action of a horizontal temperature gradient, topographically driven convection may occur in an old ocean crust/sediment layer which is stable with respect to convection due vertical temperature gradients. Such convection may help explain non-linear temperature gradients often measured in old, thickly sedimented oceanic crust.

We have attempted to model this effect numerically; but we have encountered numerical difficulties, and this aspect of the numerical program is currently at a standstill. We have, however, been engaged in some analytical calculations on topographically induced convection. These results will be presented in a future report.

#### Recent Investigations - 1979

In the past few months we have initiated the development of a new numerical model which will emphasize features of the large scale circulation in the oceanic crust. This scheme is aimed at resolving the discrepancy between observed and theoretical conductive heat flow by (1) applying the observed heat flux as an upper boundary condition and by (2) including convective heat losses in a fundamental manner within the finite difference scheme. The first results of this work are to be presented at the Spring AGU meeting (Patterson, 1979). This work is to form the basis of Patterson's Ph.D. dissertation.

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#### Thesis Completed, M.S.

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#### Papers

Rona, P.A. and R.P. Lowell, 1978, Symposium report: hydrothermal systems at oceanic spreading centers, Geology, 6, 299-300.

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Rona, P.A. and R.P. Lowell, editors, Oceanic Spreading Centers: Hydrothermal Systems, 1979, Dowden, Hutchinson and Ross, Stroudsburg, PA, (in press).

ANNUAL TECHNICAL LETTER REPORT

SUBMITTED BY: Robert P. Lowell

DATE: May, 1979

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PRINCIPAL INVESTIGATOR: Robert P. Lowell  
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REPORT PERIOD: 1/1/78 to 12/31/78 (B)

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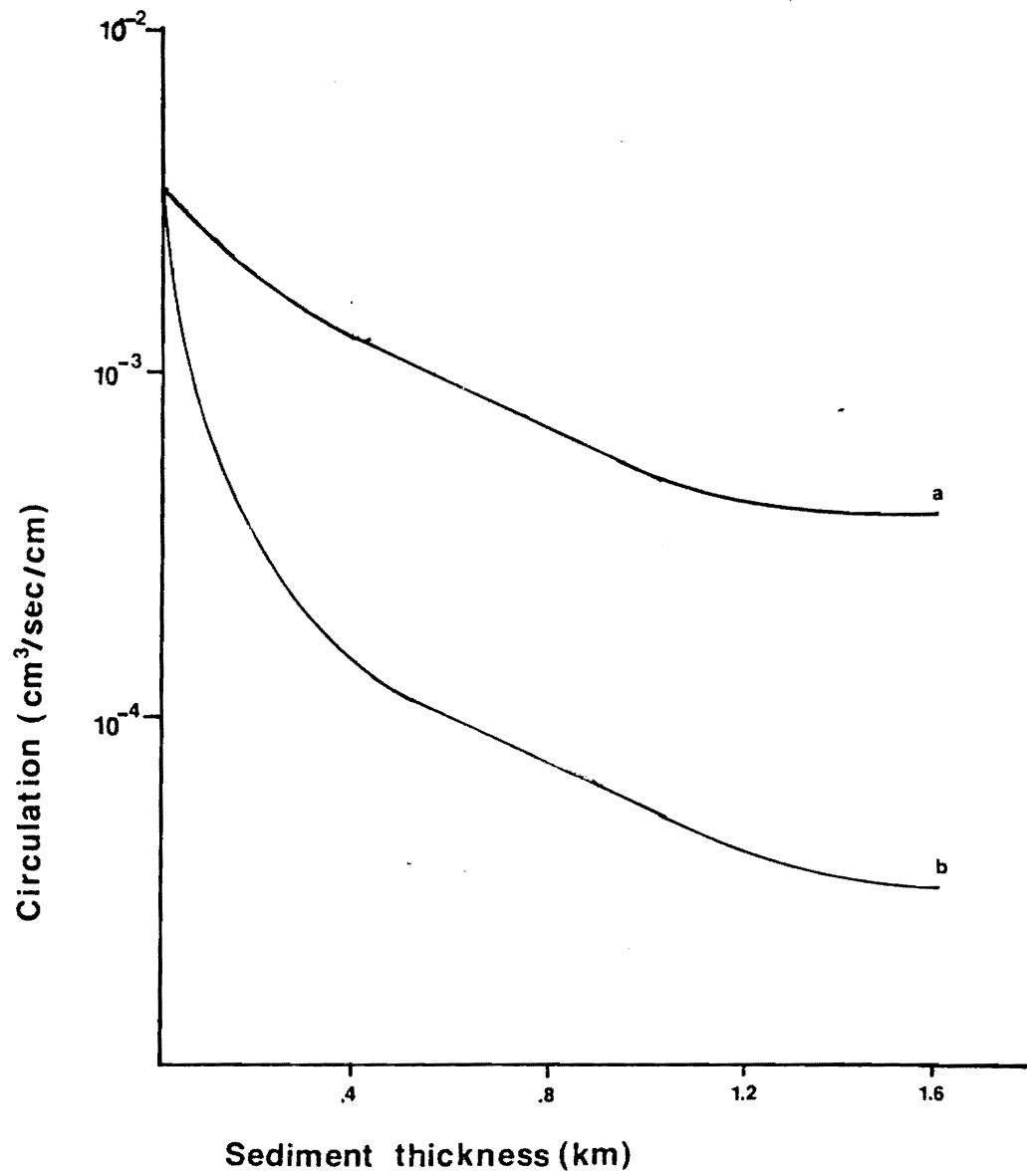


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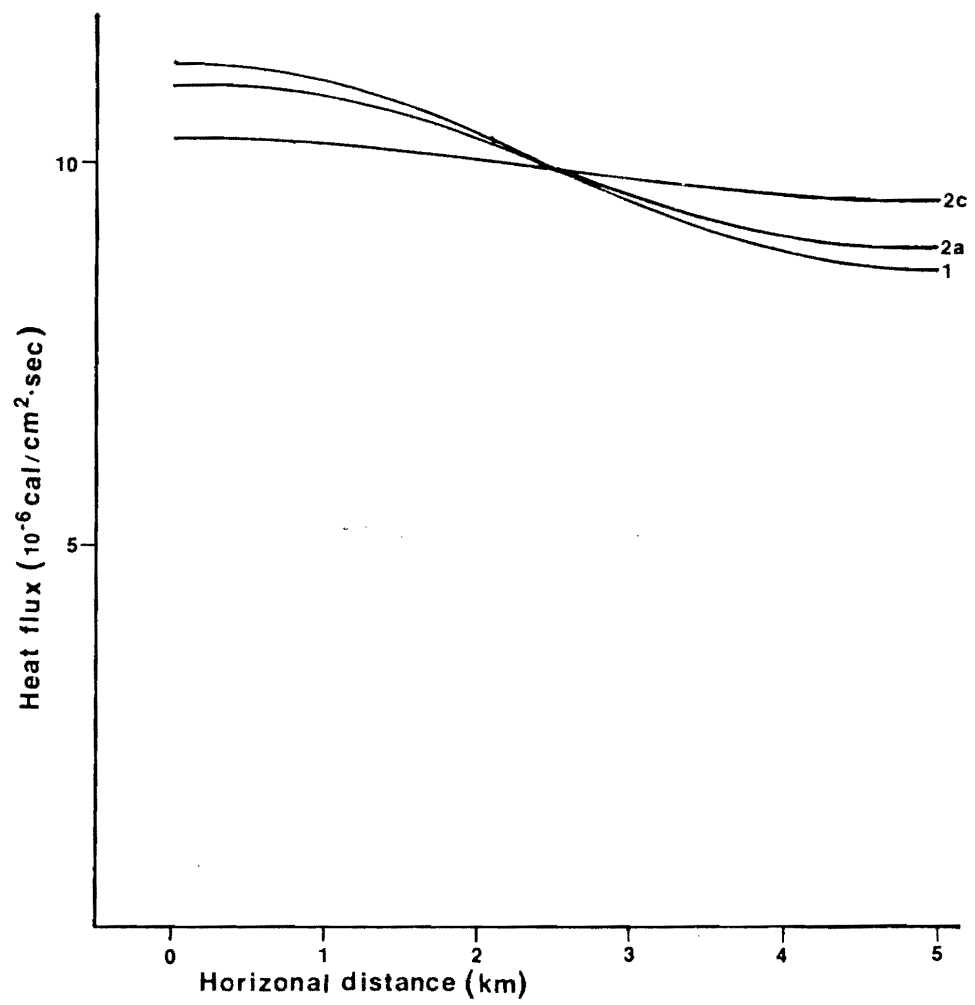


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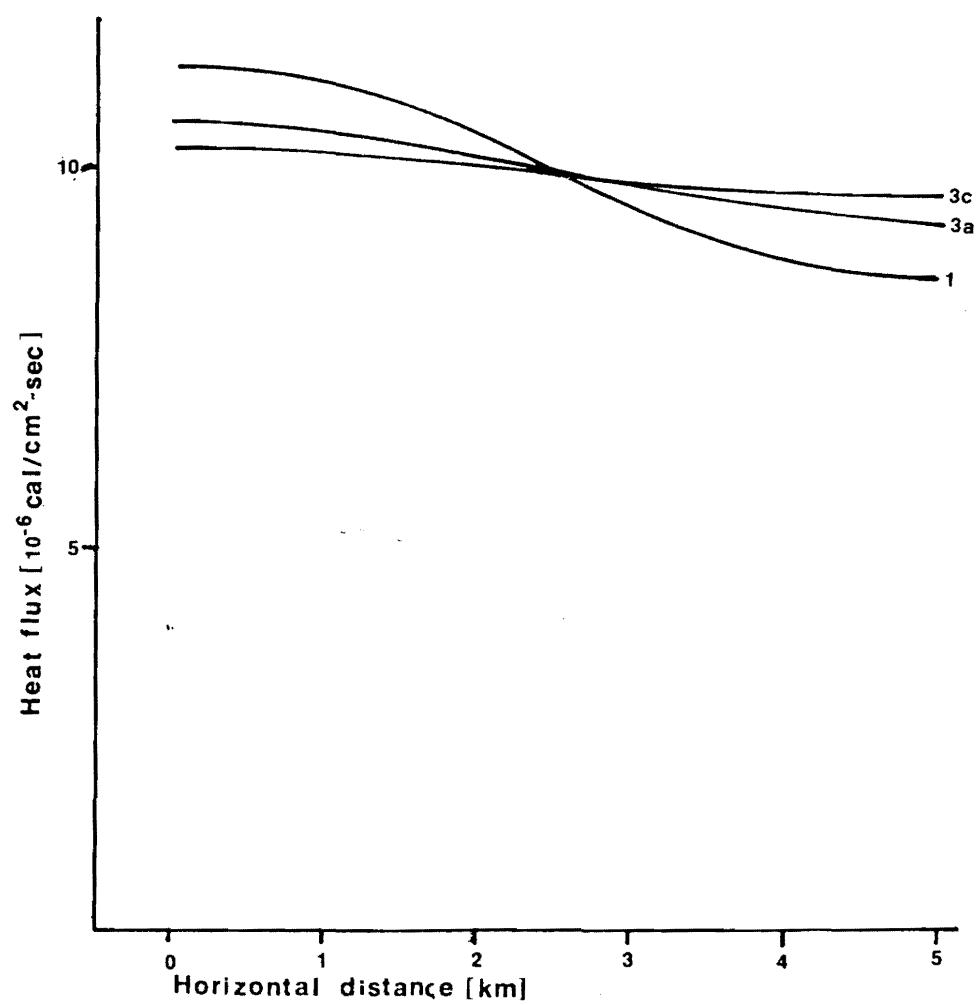


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Book

Rona, P.A. and R.P. Lowell, editors, Oceanic Spreading Centers: Hydro-thermal Systems, 1979, Dowden, Hutchinson and Ross, Stroudsburg, PA, (in press).

635-625

NATIONAL SCIENCE FOUNDATION Washington, D.C. 20550		<b>FINAL PROJECT REPORT</b> NSF FORM 98A		
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<b>PART I-PROJECT IDENTIFICATION INFORMATION</b>				
1. Institution and Address Georgia Institute of Technology 225 North Avenue Atlanta, Georgia 30332		2. NSF Program Submarine Geology and Geophysics 3. NSF Award Number OCE-76-81876 4. Award Period From 1/1/77 To 12/31/79 5. Cumulative Award Amount \$37,200		
6. Project Title Hydrothermal Circulation on Mid-Ocean Ridge Crests				
<b>PART II-SUMMARY OF COMPLETED PROJECT (FOR PUBLIC USE)</b>				
<p>The objective of this work has been to develop models of hydrothermal circulation in the oceanic crust. The models have all been based on Darcy flow in a porous medium and have involved both analytical and finite difference techniques. The research can be divided into four subtopics:</p> <p><u>Near axis convection - radiative upper boundary.</u> A finite-difference model of near axis convection which includes a radiative upper boundary shows that the convective heat transfer is small unless the permeability in the axial zone is considerably greater than <math>10^{-10}</math> cm<sup>2</sup>.</p> <p><u>Effect of sediment cover.</u> A finite difference model of convection in a porous block overlain by a layer of sediment of lower permeability shows that for a given permeability, the amount of fluid transfer through the sediment becomes independent of sediment thickness at large sediment thicknesses. A sediment with a permeability of <math>10^{-12}</math> cm<sup>2</sup> and thickness of 1 km reduces the circulation rate by about 98% compared to the sediment free case. The results indicate that even with the reduction of circulation in the sediment layer, circulation in the underlying basalt may yield an observable conductive heat flow anomaly.</p> <p><u>Subcritical topographically driven convection.</u> Linear perturbation analysis for low-amplitude, sinusoidal topography shows that in barren crust, the convective heat flux may be 15% or more of the conductive background and that the convective velocity is independent of topographic wavelength L for short wavelength topography, whereas for long wavelength topography, the flow depends on <math>(H/L)^2</math>, where H is the layer depth. In sediment covered crust, the flow is substantially reduced. The topography controls the location of the ascending and descending fluid.</p> <p><u>Galapagos Spreading Center model.</u> A series of numerical models have been developed for the hydrothermal circulation at Galapagos Spreading Center. The models extend from the axis to an age of <math>5.5 \times 10^6</math> m.y. anomaly. Models which give good agreement with the heat flow means indicate that the permeability in the axial zone is on the order of <math>10^{-9}</math>-<math>10^{-8}</math> cm<sup>2</sup> and the depth of fluid circulation is slightly less than 3.5 km. The transport of heat is controlled by short wavelength convection and does not involve significant horizontal redistribution of the heat flow anomaly.</p>				
<b>PART III-TECHNICAL INFORMATION (FOR PROGRAM MANAGEMENT USES)</b>				
1. ITEM (Check appropriate blocks)	NONE	ATTACHED	PREVIOUSLY FURNISHED	TO BE FURNISHED SEPARATELY TO PROGRAM
				Check (✓)      Approx. Date
a. Abstracts of Theses		X		X July, 1980
b. Publication Citations		X	X	X July, 1980
c. Data on Scientific Collaborators	X			
d. Information on Inventions	X			
e. Technical Description of Project and Results		X	X	
f. Other (specify)				
2. Principal Investigator/Project Director Name (Typed) Robert P. Lowell		3. Principal Investigator/Project Director Signature		4. Date <div style="font-size: 1.5em; font-family: cursive;">4/3/80</div>

## SUMMARY\*

In this study three models have been developed to study hydrothermal circulation in crust overlain by uniform sediment layers. The first model was an analytical model to examine the changes in the critical Rayleigh number as a function of sediment thickness. The second model was a two-dimensional, time dependent, numerical model. In each of these models the ocean bottom was assumed to be a radiative boundary. The third model was a two-dimensional, time dependent, numerical model. In this model the ocean bottom was assumed to be isothermal, precluding convective heat transfer through the ocean bottom.

Consideration of the radiative ocean bottom problems reveals that the critical Rayleigh number and corresponding semi-wavelength are not changed substantially from those for isothermal bottom cases. The thermal history of the oceanic crust is not altered by considering the ocean bottom to be radiative.

Investigation of the thick-sediment model reveals that relatively thin layers of a low permeability sediment will effectively seal the oceanic crust to fluid exchange. However, the predicted heat fluxes through the ocean bottom reveal the hydrothermal circulation that is occurring in the oceanic crust; however, the magnitude of the heat flux fluctuations have been damped.

\*Fulford, J. K., 1979, Thermal Convection in Porous Media with Application to Hydrothermal Circulation in the Oceanic Crust, M.S. Thesis, Georgia Institute of Technology, Atlanta, 54 p.

FINAL TECHNICAL LETTER REPORT

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School of Geophysical Sciences

GRANTEE: Georgia Institute of Technology

Atlanta, Georgia 30332

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## ABSTRACT

The objective of this work has been to develop models of hydrothermal circulation in the oceanic crust. The models attempt to deal with various aspects of the convection problem such as the effect of sediment cover, uneven surface topography, and a non-isothermal crust-seafloor interface. The models have all been based on Darcy flow in a porous medium and have involved both analytical and finite difference techniques.

The research can be divided into four subtopics:

1. Near axis convection - radiative upper boundary. An extension of earlier numerical work on near axis convection to include a radiative upper boundary (to allow for convective heat transfer to the ocean floor) shows that the convective heat transfer is small unless the permeability in the axial zone is considerably greater than  $10^{-10} \text{ cm}^2$ .
2. Effect of sediment cover. A finite difference model of convection in a porous block overlain by a layer of sediment of lower permeability shows that for a given permeability, the amount of fluid transfer through the sediment becomes independent of sediment thickness at large sediment thicknesses. A sediment with a permeability of  $10^{-12} \text{ cm}^2$  and thickness of 1 km reduces the circulation rate by about 98% compared to the sediment free case. The results indicate that even with the reduction of circulation in the sediment layer, circulation in the underlying basalt may yield an observable conductive heat flow anomaly.

3. Subcritical topographically driven convection. Linear perturbation analysis for low-amplitude, sinusoidal topography shows that in barren crust, the convective heat flux may be 15% or more of the conductive background and that the convective velocity is independent of topographic wavelength  $L$  for short wavelength topography, whereas for long wavelength topography, the flow depends on  $(H/L)^2$ , where  $H$  is the layer depth. In sediment covered crust, the flow is substantially reduced. The topography controls the location of the ascending and descending fluid.
4. Galapagos Spreading Center model. A series of numerical models have been developed for the hydrothermal circulation at Galapagos Spreading Center. The models extend from the axis to an age of  $5.5 \times 10^6$  m.y., the entire region of the heat flow anomaly. Models which give good agreement with the  $10^6$  y heat flow means indicate that the permeability in the axial zone is on the order of  $10^{-7}$ - $10^{-8}$   $\text{cm}^2$  and the depth of fluid circulation is slightly less than 3.5 km. The transport of heat is controlled by short wavelength, Lapwood type convection and does not involve significant horizontal redistribution of the heat flow anomaly.



## INTRODUCTION

This document represents the final technical report for National Science Foundation, Division of Ocean Sciences Grant No. OCE-76-81876 entitled "Hydrothermal Circulation on Mid-Ocean Ridge Crests". The work is funded as part of the Submarine Geology and Geophysics Program and represents the continuation of the effort initially supported under NSF Grant No. DES74-00513.

The work has involved both analytical and finite difference modeling. The principal achievements have been to: (1) investigate the effect of sediment cover on convection in the underlying porous slab; (2) investigate the effect of a radiation boundary condition at the crust-seawater interface; (3) investigate large spatial scale effects of convection in a porous crust of varying bottom heat flow and crustal permeability; (4) develop models of subcritical, topographically driven convection. The first two topics have been reported on in interim reports and the results will be merely summarized here. The third and fourth topics have been the main task of the past year or so, and they will form the bulk of this report. In addition to the research efforts, the Principal Investigator has also devoted some of his time to the preparation of a book entitled: Seafloor Spreading Centers: Hydrothermal Systems in conjunction with Dr. Peter A. Rona of NOAA. This volume will appear in the series Benchmark Papers in Geology, and it is hoped that this book will serve as a useful reference item in the field of hydrothermal circulation in the oceanic crust for years to come.

## OBJECTIVES OF PROPOSED RESEARCH

The objective of the research is to develop models of hydrothermal

circulation in the oceanic crust. The models attempt to deal with various aspects of the overall convection problem, such as the effect of sediment cover and uneven surface topography and are based on Darcy flow in porous media. The results of these models will be used to interpret observed patterns of conductive heat flow through the ocean floor. It is hoped that the models will provide insight into the magnitude of the convective flow as well as provide constraints on physical parameters - especially permeability.

## MODELS

### A. Near Axis Convection - Radiative Upper Boundary

Under the initial NSF grant we developed finite-difference models of near axis convection (Patterson, 1976; Patterson and Lowell, 1980). These models included a narrow, high temperature intrusive at the axis as well as heat flux from below. The upper boundary, however, was maintained at  $T = 0$  so that there was no convective heat loss across the seafloor. The effect of the circulation was to redistribute the conductive heat flux. Near the ridge axis, where fluid was ascending, the heat flow was higher than the theoretical; where fluid was descending the heat flux was lower than the theoretical.

We attempted to remedy this problem by applying a radiative boundary condition at the upper surface. The results showed that for a bulk permeability of  $10^{-10} \text{ cm}^2$  or less, the ratio of convective to conductive heat flux remains small. This suggests that near the axis the permeability must be substantially greater than  $10^{-10} \text{ cm}^2$  to have appreciable convective heat loss in the axial region (Lowell et al., 1977). Details of the calculations are given in Fulford (1979).

## B. Effect of Sediment Cover

We also considered the problem of a low permeability blanket of sediment overlying the basaltic crust. The questions to be answered were: (1) What sediment thickness/permeability ratios are required to prevent significant fluid exchange across the sea floor? (2) In the absence of significant fluid exchange, would convection in the underlying basalt be detectable in the conductive heat flow data obtained in the overlying sediments?

To answer these questions, the pertinent steady state heat and mass transfer equations were solved by finite differences in a two layer square porous block of dimension  $h$ . The upper surface was isothermal and overlain by a free-standing column of fluid; the bottom was rigid with a constant inward heat flux  $q = 10 \text{ cal/cm}^2\text{-s}$ ; the sides were rigid and insulated. The permeability of the basalt layer was assumed to be  $10^{-10} \text{ cm}^2$ , and the sediment layer was assumed to have a permeability of either  $10^{-11} \text{ cm}^2$  or  $10^{-12} \text{ cm}^2$ . The thickness of sediment was varied from 0.4 to 1.6 km, the basaltic layer decreasing in depth as sediment increased so that  $h$  remained at 5 km. The physical properties of the fluid, rock, and sediment were assumed to be constant. The cases modeled are listed in Table 1, and the pertinent results are shown in Figures 1, 2, and 3.

Figure 1 shows the reduction in fluid exchange across the sediment-water boundary as a function of sediment thickness for the two assumed values of sediment permeability. Both curves show a rapid decrease in the fluid exchange rate as thickness increases, the rate of decrease of fluid exchange gradually flattening out at large sediment thicknesses. The results show (a) the smaller the sediment permeability, the greater

Table 1. Cases Modeled

Case	NK	K <sub>1</sub>
1	0	
2a	.4	10 <sup>-11</sup>
2b	.8	
2c	1.2	
2d	1.6	
3a	.4	10 <sup>-12</sup>
3b	.8	
3c	1.2	
3d	1.6	

Explanation:

NK is depth of sediments in km.

K<sub>1</sub> is sediment permeability in cm<sup>2</sup>.

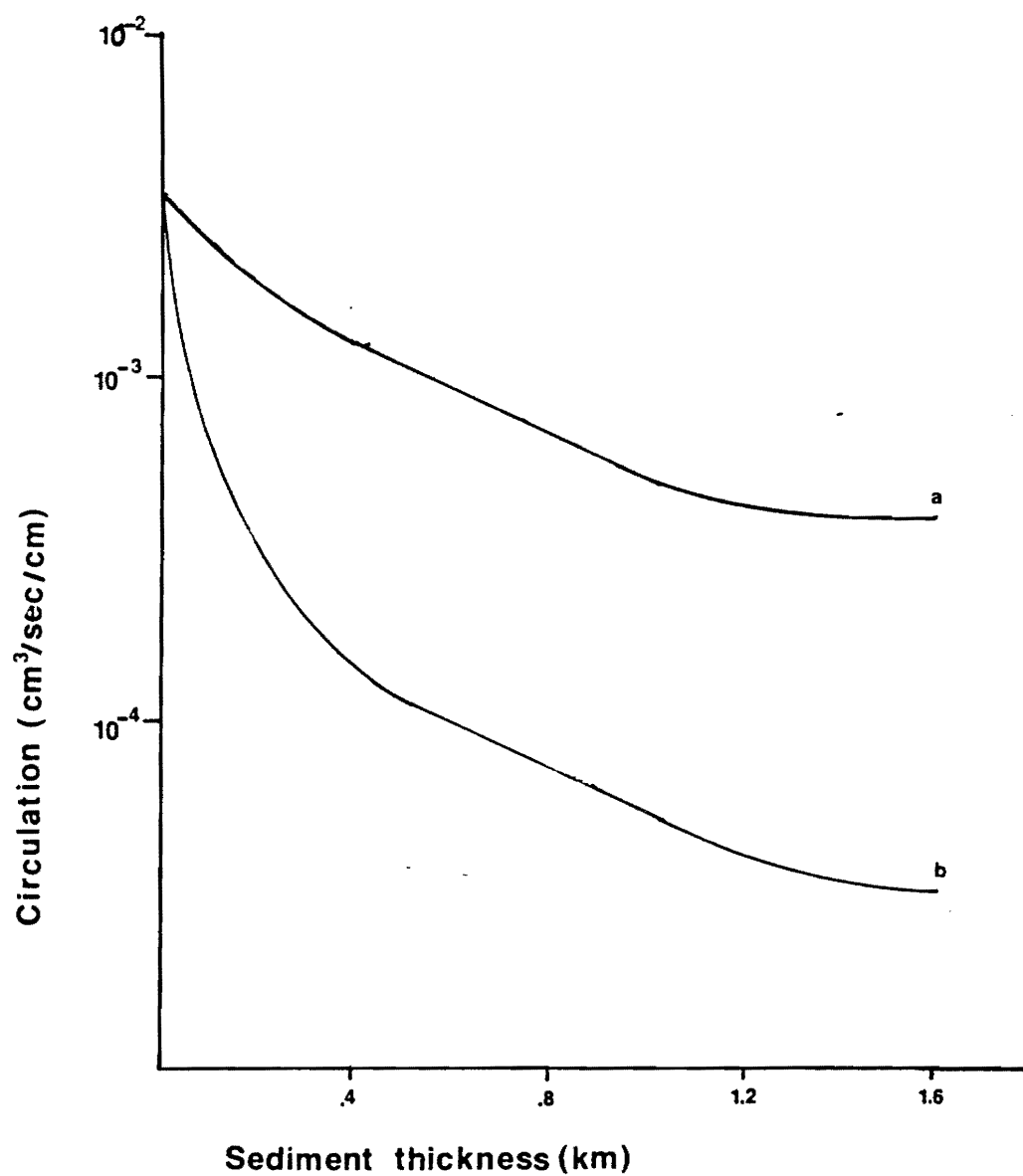


Figure 1. Circulation of fluid versus sediment thickness for sediment of permeability  $10^{-11}$  cm<sup>2</sup> (curve a), and for sediment of permeability  $10^{-12}$  cm<sup>2</sup> (curve b).

the reduction in fluid exchange, and (b) for a given permeability, the amount of reduction becomes independent of sediment thickness at large thicknesses. Result (b) is generally in accord with the result of Skilbeck and Anderson (1979) who derived the sealing condition

$$K_s/K_b \ll \tanh \lambda d$$

where  $d$  is the sediment thickness and  $\lambda$  is the horizontal wave number of the convection cell. Thus as  $d$  gets larger, the condition becomes independent of the sediment thickness. Curve (b) indicates that a sediment thickness of about 1 km and permeability  $10^{-12} \text{ cm}^2$  reduces the fluid exchange across the sea floor by almost two orders of magnitude (~98%).

Figures 2 and 3 show corresponding results for the smoothing of the horizontal variation in conductive heat flux over a cell wavelength. The principal result is that even though the fluid exchange is effectively curtailed, a horizontal heat flux variation is still perceptible. It must be pointed out, however, that the assumed heat flux is quite high and the sediment was assumed to have the same thermal conductivity as basalt. Modification in these parameters is likely to adversely affect the perceptibility of convection beneath a thick sedimentary cover.

Further details on the effects of sedimentary cover on convection are given in Fulford (1979).

### C. Subcritical Topographically Driven Convection

Lister (1972) first pointed out that irregular seafloor topography could control the positioning of convection cells within the oceanic crust near the Juan de Fuca Ridge. Moreover, recent measurements of non-linear temperature gradients in older, sediment covered crust (von

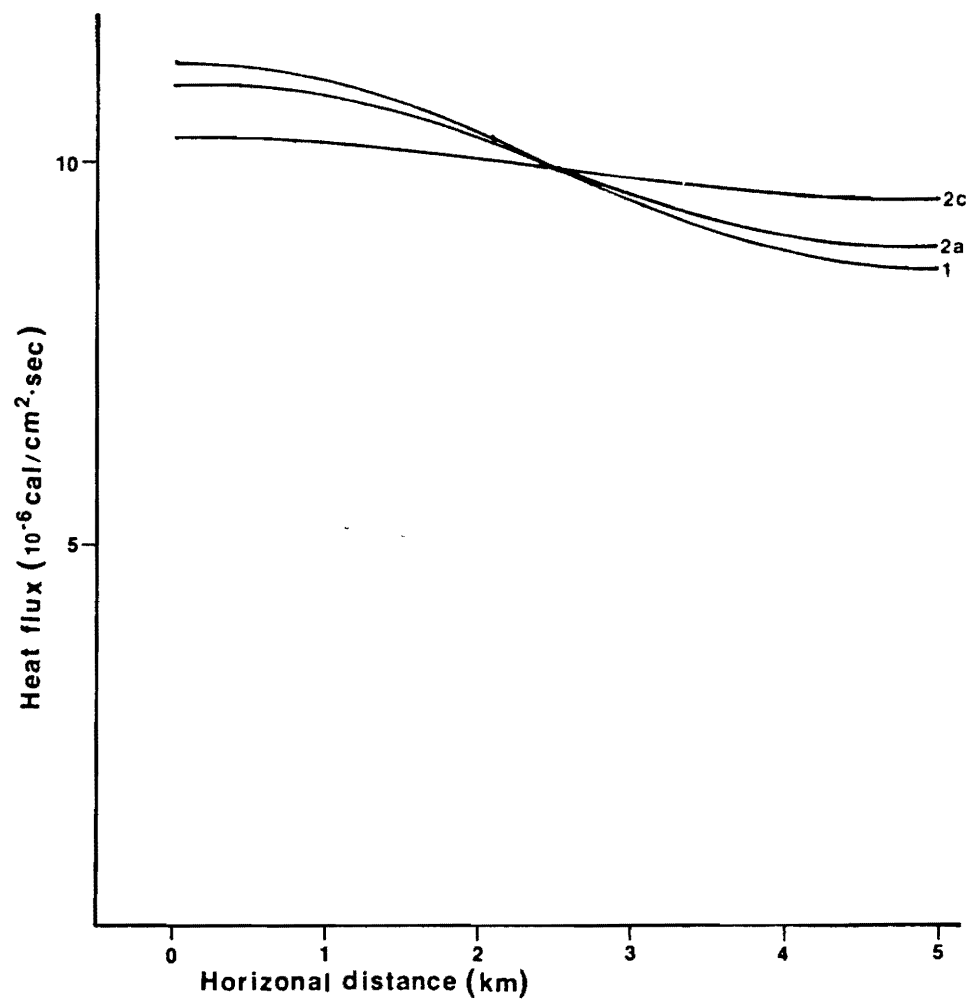


Figure 2. Comparison of surface conductive heat flux for case 2a, 2c, and 1.

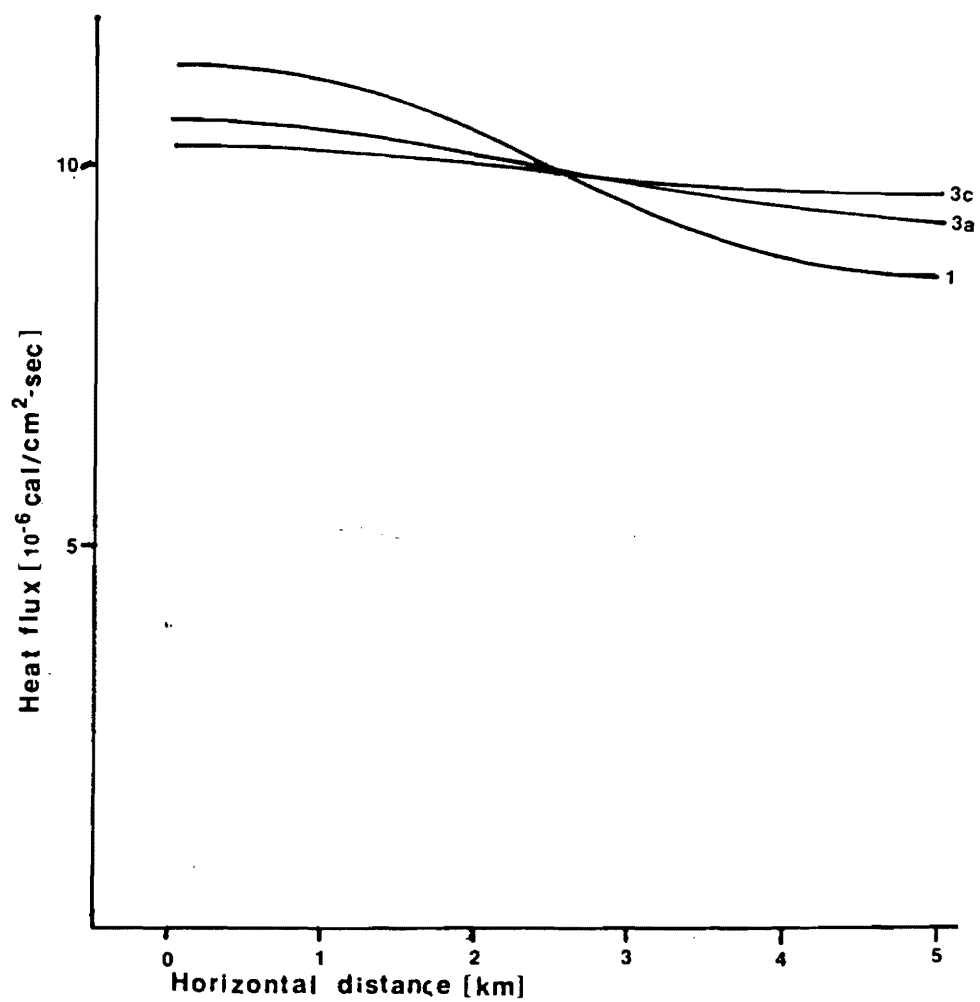


Figure 3. Comparison of surface conductive heat flux for case 3a, 3c, and 1.



Herzen et al., 1979; Anderson et al., 1979) indicate the possible occurrence of convection which is topographically induced, that is, convection driven by horizontal temperature gradients which occur due to irregular topography overlain by an infinite heat sink (the ocean). Under the action of such horizontal temperature gradients, the fluid is convectively unstable even if the Rayleigh number is subcritical, i.e., the fluid is stable with regard to convection driven by vertical temperature gradients.

We have used a linear perturbation analysis to estimate the magnitude of the vertical convective velocity driven by low amplitude, sinusoidal topography, assuming subcritical conditions. Both the case of barren topography as well as that of sediment covered topography were examined. The main results are: (1) In barren crust the maximum vertical velocity is roughly  $10^{-10}$  m/sec for a permeability of  $10^{-14}$  m<sup>2</sup> and a topographic wavelength of  $10^3$  m; the convective heat flux is roughly 15% of the conductive background; the fluid ascends at topographic highs and descends at topographic lows; the convective velocity is independent of the topographic wavelength-layer depth ratio  $L/H$  if  $L < H/2$ , but for  $L \gg H$ , the flow depends on  $(H/L)^2$ . (2) In sediment covered crust, the convective flow is substantially reduced, perhaps by several orders of magnitude; the fluid descends at topographic highs and ascends at topographic lows; in order for the observed non-linear gradient of von Herzen et al., (1979) to be attributable to subcritical topographically driven convection or sediment permeability of roughly  $10^{-15}$  m<sup>2</sup> or greater is required.

These results are currently in press (Lowell, 1980). The complete manuscript is attached as an Appendix to this report.

## D. Galapagos Spreading Center Model

### D.1 Model Definition and Solution

A series of numerical models have been developed for hydrothermal circulation in the upper oceanic lithosphere at the Galapagos Spreading Center. The models involve the entire region of the heat flow anomaly for that spreading center, and some predict conductive heat-flow means for  $10^6$  year intervals in accord with empirical data.

Figure 4 diagrams the basic model. It represents a cross-section of the upper crust perpendicular to the rift axis (the z axis). The x axis points toward the center of the earth and the y axis in the direction of spreading. The yz plane represents the ocean bottom, separating the ocean from the lithosphere. The model is two-dimensional, allowing for no variations in the z direction.

The crust is assumed permeable to depth h, where  $h = 3.5$  km, and for horizontal distance e, where e is varied. The model extends for horizontal distance d, where  $d = 192.5$  km, which corresponds to a crustal age of  $5.5 \cdot 10^6$  years for a spreading velocity of 3.5 cm/yr.

Included in Figure 4 are the boundary conditions for temperature and fluid Darcy velocity. (See Table 2 for symbol identification.) The bottom temperature boundary condition is derived from Parker and Oldenburg's (1973) theoretical model for conductively cooling lithosphere. The top temperature boundary condition assumes the conductive flow of heat from the crust is related to the temperature difference between the crust and ocean (assumed to be at  $T = 0^\circ\text{C}$ ) by a heat transfer coefficient  $\hat{h}(y)$ . All fluid entering the crust is assumed to be at  $T = 0^\circ\text{C}$ , while fluid leaving the crust is assumed to be at the surface crustal temperature.

# *Model for Hydrothermal Circulation in Young Oceanic Crust*

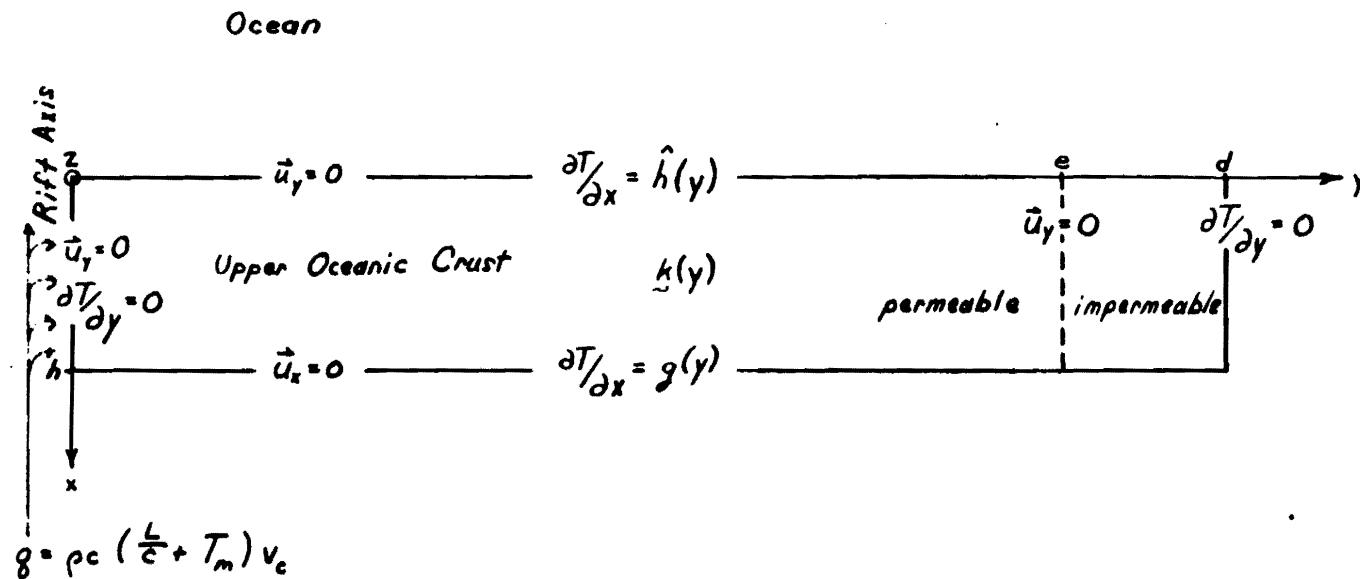


Figure 4. Model for Hydrothermal Circulation in Young Oceanic Crust.

Table 2.: Symbols

## Fluid:

$\vec{u}$	Darcy velocity
$P$	Pressure
$\rho_f$	density
$\nu$	kinematic viscosity ( $0.01 \text{ cm}^2/\text{s}$ )
$c_f$	specific heat ( $1 \text{ cal}/^\circ\text{C-gr}$ )
$\rho_{f0}$	density at $T = 0$ ( $1 \text{ gr}/\text{cm}^2$ )
$\alpha$	coefficient of thermal volume expansion ( $1.6 \cdot 10^{-4}/^\circ\text{C}$ )

## Other:

$\vec{g}$	acceleration of gravity ( $980 \text{ cm}/\text{s}^2$ )
$\underline{k}$	permeability tensor
$T$	crustal and fluid temperature
$T_m$	intrusion temperature ( $1200^\circ\text{C}$ )
$\rho$	crustal density ( $3 \text{ gr}/\text{cm}^2$ )
$c$	crustal specific heat ( $0.25 \text{ cal}/^\circ\text{C-gr}$ )
$L$	crustal latent heat ( $100 \text{ cal/gr}$ )
$v_c$	crustal spreading velocity ( $3.5 \text{ cm/yr}$ )
$K$	crustal thermal conductivity ( $0.005 \text{ cal}/^\circ\text{C-cm-s}$ )
$t$	time
$q$	axis heat addition due to intrusion
$\hat{h}$	heat transfer coefficient

The basic equations for the model are:

$$\vec{\nabla} \cdot \vec{u} = 0 \quad (1)$$

$$-\vec{\nabla} P + \rho_f \vec{g} - \rho_f \nu k^{-1} \cdot \vec{u} = 0 \quad (2)$$

$$k \nabla^2 T - \rho_f c_f \vec{u} \cdot \vec{\nabla} T - \rho c \frac{\partial T}{\partial y} v_c = \rho c \frac{\partial T}{\partial y} \rightarrow 0 \quad (3)$$

$$\rho_f = (1 - \alpha T) \rho_{f0} \quad (4)$$

Equation (1) is for the conservation of fluid mass for a homogeneous and incompressible fluid; equation (2) is Darcy's law for the conservation of fluid momentum; equation (3) is for the conservation of thermal energy, assuming the fluid and rock to be in thermodynamic equilibrium; and equation (4) is the equation of state for the fluid. The solution of these equations was simplified by assuming constant fluid viscosity and the Boussinesq approximation. The equations were non-dimensionalized and a stream function  $\psi$  was introduced based on equation (1). The resulting equations are:

$$Rk_x \frac{\partial T}{\partial y} + \frac{k_x}{k_y} \frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} - \frac{1}{k_x} \frac{\partial k_x}{\partial y} \frac{\partial \psi}{\partial y} = 0 \quad (5)$$

$$u_x = \partial \psi / \partial y \quad (6)$$

$$u_y = \partial \psi / \partial x \quad (7)$$

$$\frac{\partial T}{\partial t} = \nabla^2 T - \vec{u} \cdot \vec{\nabla} T - v_c \frac{\partial T}{\partial y} \quad (8)$$

For simplicity, the same symbols have been used here for the dimensionless quantities as for dimensional quantities. Equation (5) allows for permeability anisotropy and permeability variations in the y direction.

These equations were represented in conservative finite-difference forms and were solved on a 5 x 56 array of grid points. The method of solution was as follows:

Set: bottom boundary temperature gradient,  $g_j$

lateral extent of permeable region,  $e$

permeability distributions,  $k_{xj}$  and  $k_{yj}$

heat transfer coefficient,  $\hat{h}_j$

Method of Computation:

0. Define initial temperature field,  $T_{i,j}^{(\ell)}$ , where  $\ell = 0$  at time  $t = 0$ .

1. Solve iteratively by successive overrelaxation for stream function,  $\psi_{i,j}^{(\ell)}$ , as a function of  $k_{xj}$ ,  $k_{yj}$ ,  $T_{i,j+1}$ ,  $T_{i,j-1}$ , and surrounding values of  $\psi^{(\ell)}$ .

2. Solve for velocity  $u_{x,i,j}^{(\ell)}$  and  $u_{y,i,j}^{(\ell)}$  as function of  $\psi^{(\ell)}$ .

3. Determine size of time step,  $\Delta t^{(\ell+1)}$  acceptable for stability as function of  $u_{x,i,j}$ ,  $u_{y,i,j}$ ,  $\Delta x$ ,  $\Delta y$ , and  $v_{\text{crust}}$ .

4. Solve for temperature,  $T^{(\ell+1)}$ , at time  $t = \sum_{p=1}^{\ell+1} \Delta t^{(p)}$ , where

$$T_{i,j}^{(\ell+1)} = T_{i,j}^{(\ell)} + \Delta t^{(\ell)} [\text{function of } t^{(\ell)} \text{ and } u^{(\ell)}].$$

5. Test for steady-state:

if  $\left\{ \begin{array}{l} \max / T_{i,j}^{(\ell+1)} - T_{i,j}^{(\ell)} / \leq .001 \text{ and} \\ \Sigma \text{ heat out of model} / \Sigma \text{ heat into model} = 1.000 \end{array} \right.$

Yes

No

$\ell = \ell + 1$  PRINT RESULTS

Further details of the numerical procedure are given in Patterson (1980).

## D.2 Results

Table 3 summarizes 10 models and some results. The first three lines of the table with headings, " $v_c$ ", " $\hat{h}(y)$ ", and " $k(y)$ ", describe the unique input properties of the models. The remaining lines describe some output properties of the models.

If  $v_c = 0$  for the model, crustal movement is neglected, no heat is added at the axis, and at the bottom boundary

$$\frac{\partial T}{\partial x} = \frac{q_T(0,y)}{K},$$

where Parker and Oldenburg (1973) define heat flow at depth  $x$  and distance  $y$  from the ridge axis to be:

$$q_T(x,y) = q_T(0,y)e^{-.416x^2/y}$$

For these models the total rate of heat addition is 159 cal/cm-s. If  $v_c = 3.5$  cm for the model, 47 cal/cm-s are added at the ridge axis and at the bottom boundary 121 cal/cm-s according to the formula:

$$\frac{\partial T}{\partial x} = q_T(h,y)e^{-.416 h^2/y}.$$

An exception to the above is model M9 where  $v_c = 0$  but heat is added at the axis and bottom as for models with  $v_c = 3.5$  cm/yr.

The heat transfer coefficient function for the top boundary is assumed either to be constant or to vary as a function of sediment depth as shown in Figure 5, where:

$$\hat{h}(y) = \frac{1}{\hat{h}_w^{-1} + \frac{\text{sed. depth } (y)}{k \text{ sed.}}}$$

Table 3: Models and Results

MODEL	F8b	M9	F28	F12	F6b	F8	M16	M20	M16b	M19
$v_c$ (cm/yr)	0	0	3.5	0	0	0	3.5	3.5	3.5	3.5
$\hat{h}(y)$ ( $\frac{\text{cal}}{\text{cm}^2\text{-s-}^\circ\text{C}}$ )	$10^{-6}$	$10^{-6}$	$10^{-6}$	$10^{-7}$	$10^{-6}$	$10^{-6}$	--	--	-See Fig. 5 --	
$k(y)$	-----See Figure 6-----				Fig. 9 $k_y = 10k_x$	Fig. 9 $k_y = 2k_x$	Fig.11	Fig. 11	Fig. 10	Fig.
avg. $\lambda$ (km)	7.8	8.8	8.8	7.8	10.5	10	8.8	10	8.8	--
surface $T_{\max}$ ( $^\circ\text{C}$ )	23 $^\circ$	46 $^\circ$	46 $^\circ$	29 $^\circ$	23 $^\circ$	28 $^\circ$	61 $^\circ$	130 $^\circ$	13 $^\circ$	21 $^\circ$
$T_{\max}$ ( $^\circ\text{C}$ )	97 $^\circ$	52 $^\circ$	53 $^\circ$	97 $^\circ$	86 $^\circ$	88 $^\circ$	150 $^\circ$	314 $^\circ$	21 $^\circ$	204 $^\circ$
$VX_{\max}$ ( $10^{-6}$ cm/s)	3.4	5.2	5.2	3.4	4.7	3.1	3.7	1.1	11.6	3.6
$VY_{\max}$ ( $10^{-6}$ cm/s)	4.1	5.1	5.1	4.1	5.9	5.9	3.6	1.1	11.5	3.6
circulation rate $10^8$ ( $\text{cm}^3/\text{yr-cm}$ )	3.24	3.08	3.08	3.25	3.39	2.64	0.79	0.20	1.96	0.56
circ. efficiency (cal/cm <sup>3</sup> fluid)	8.7	10.2	10.1	13.7	9.1	10.5	37.6	72.8	14.3	21.2
avg. $\lambda$ (km)	7.9	7.95	7.95	7.95	9.93	9.21	10.7	11.9	10.5	
greatest dist. for hor. ht. transfer (km)	7	7	7	--	7	14	--	--	7	--
surface $T_{\max}$ where UX is +	.03	.07	.10	.01	.07	.25	1.09	4.43	2.28	4.59



Figure 5.

# Heat Transfer Coefficient at Top Boundary

Heat transfer coefficient (cal/cm<sup>2</sup>s.c)

$$\hat{h} = \frac{1}{\frac{1}{h_w} + \frac{\text{sed. depth}}{K_{\text{sed.}}}}$$

sediment depth = 50m/10<sup>6</sup> yrs.

$K_{\text{sed.}} = 1.8 \cdot 10^{-3}$  cal/cm.s

Models M16b & M19

Models M16 & M20

Distance from ridge axis (km)

10<sup>-8</sup>

10<sup>-7</sup>

10<sup>-6</sup>

10<sup>-5</sup>

10<sup>-4</sup>

35

70

105

140

175

$\hat{h}_w$  is the heat transfer coefficient in the absence of sediments and is dependent on ocean flow and ocean bottom roughness characteristics. Texts on heat transfer give order of magnitude estimates of  $\hat{h}_w$  to exceed  $10^{-4}$  cal/°C-cm-s (Whitaker, 1977), whereas Ribando et al. (1976) use values on the order of  $10^{-6}$  cal/°C-cm-s. In this formula the sediments are treated as a thin skin of a poor conductor (Carslaw and Jaeger, 1959).

The permeability distributions for the models,  $k(y)$ , are included in Figures 6, 9, 10 and 11. The first four models have the same permeability distribution. The next two, F66 and F8, have anisotropic permeabilities with horizontal permeability  $k_y$ , greater than vertical permeability,  $k_x$ . Models M20 and M19 have 0.1 times the permeability of Models M16 and M16b respectively. The next five lines of Table 3 give results for crust of age  $0-10^6$  years. The fourth line of Table 3 gives the average wavelength of the hydrothermal convection for this age range. The next line gives the maximum surface crustal temperature, and the next line the maximum crustal temperature to depth  $h$ . The lines labeled " $v_x$  max" and " $v_y$  max" give the maximum vertical and horizontal Darcy velocities of the fluid.

The last five lines of Table 3 give results involving the entire model, i.e., for crust of age  $0-5.5 \cdot 10^6$  years "circulation rate" is the volume of fluid that enters and leaves the crust per year per cm. of ridge. "Circulation efficiency" is the total rate of convective heat removal divided by the circulation rate. "Avg  $\lambda$ " is the average wavelength of hydrothermal circulation for the entire model. The "greatest dist. for hor. heat transfer" is the maximum horizontal distance

that heat travels within the permeable region of the model. The last line of Table 3 gives the maximum surface temperature of crust in which fluid is flowing down from the ocean into the crust.

Figure 6 shows four curves of conductive heat flow means for  $10^6$  year age intervals of crust. The curve labeled "theoretical" is derived from the standard bottom boundary condition for models with  $v_c = 0$  (excepting M9). The curve labeled "empirical" is derived from actual data as shown in Figure 7. The other two curves are the mean values of heat flow for models F8b and F12.

Figure 7 (from Anderson and Hobart, 1976) shows a composite of conductive heat flow values as a function of crustal age for the Galapagos Spreading Center. The dashed curve connects the  $10^6$  year means for this data. These means are used as constraints for the upper conductive heat flow means of the models of this study. Corliss et al. (1979) give more detailed heat flow data for crustal age  $10^5$  to  $10^6$  years. This data has a mean conductive heat flow of around 8 HFU and is approximately periodic perpendicular to the ridge axis with a wavelength around 7 km.

Figure 8 shows the bottom boundary heat flow curve for models with  $v_c = 3.5$  cm/year. If the heat flowing in at the axis is averaged over a  $10^6$  year interval, the first value on the curve is raised an additional 13.3 HFU. Also shown are the heat flow means for models M9 and F28.

Figure 9 through 11 show the permeability distributions and heat flow means for the remaining models.

### Discussion

Heat flow means for Models F8b (Figure 6), F8 (Figure 9), M16 (Figure 10), and M16b (Figure 11) show good agreement with means

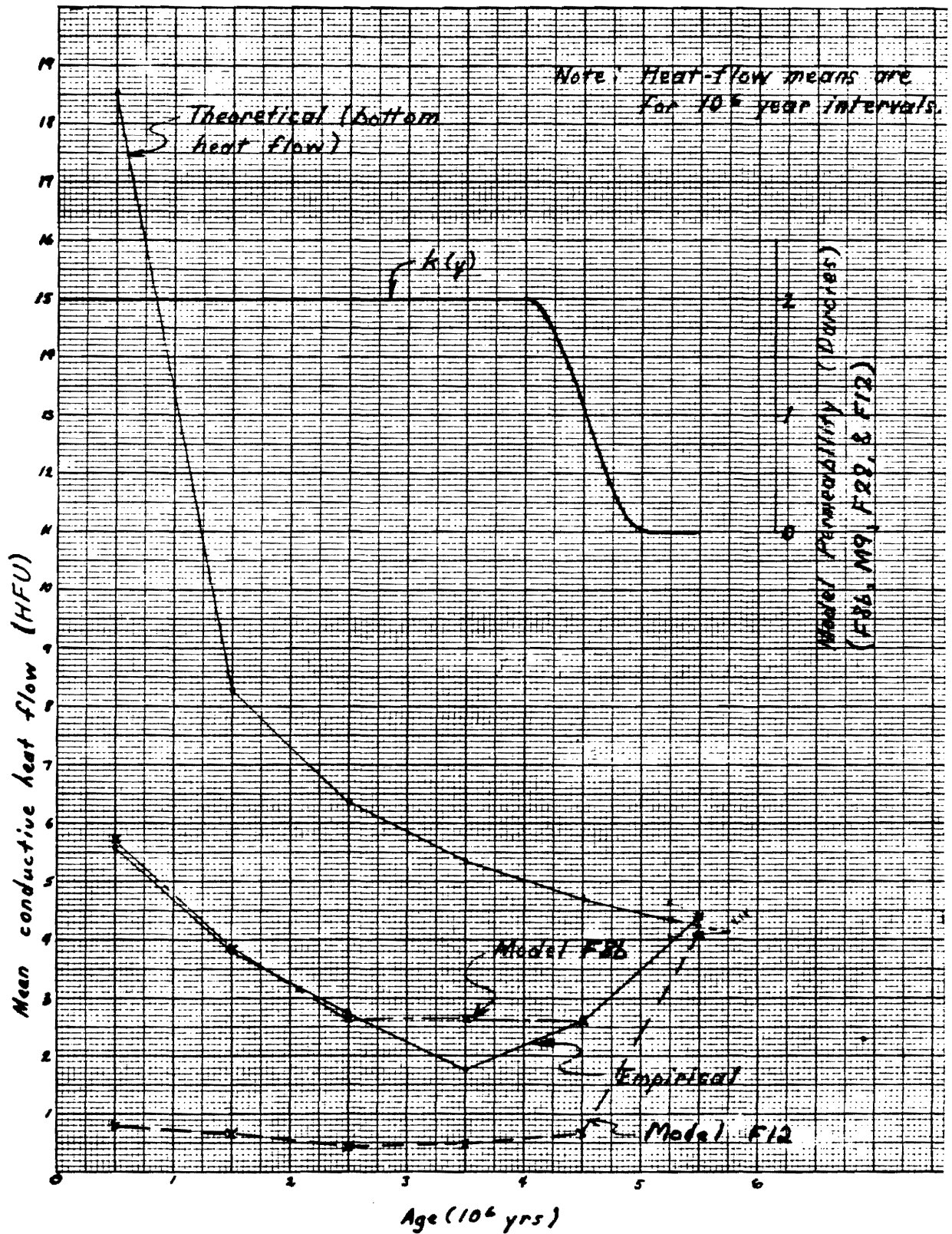
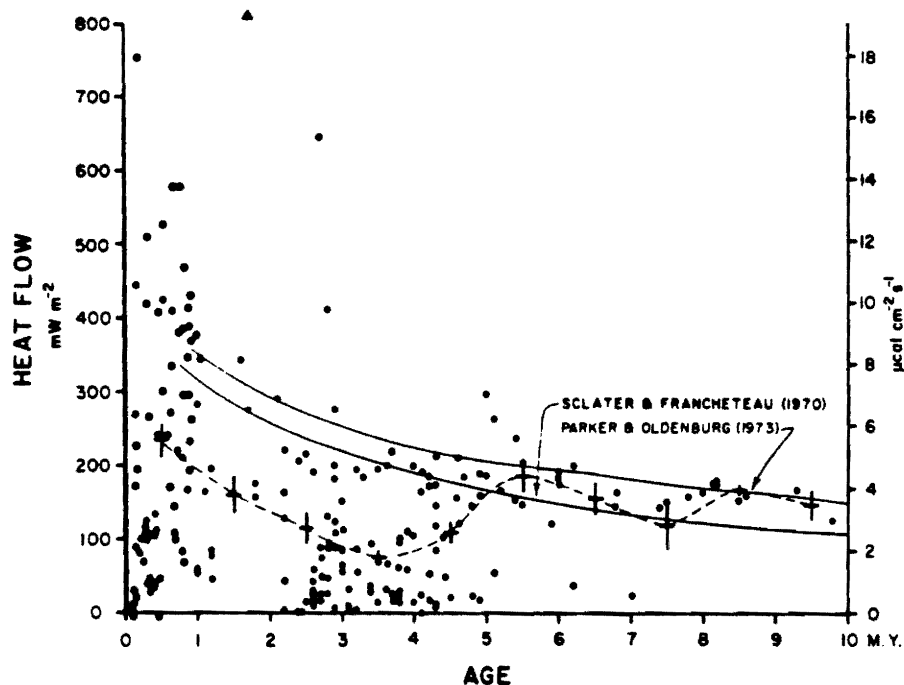


Figure 6. Models F8b and F12



Heat flow values plotted versus age on Galapagos Spreading Center as in Figure 1. Only those values from Figure 2 and 3 which are on oceanic crust of well-defined age were used for this plot (see box in Figure 2). Solid dots are heat flow values. Triangle represents off-scale values; crosses are 1-m y. means and standard error bars. Bottom theoretical curve is from the Sclater and Francheteau [1970] lithospheric plate model with thickness equal to 80 km and intrusive temperature equal to 1200°C (Sclater et al. [1974, Figure 8]). Top curve is from Parker and Oldenburg [1973]. (from Anderson & Hobart, 1976)

Figure 7. Heat Flow on Galapagos Spreading Center.

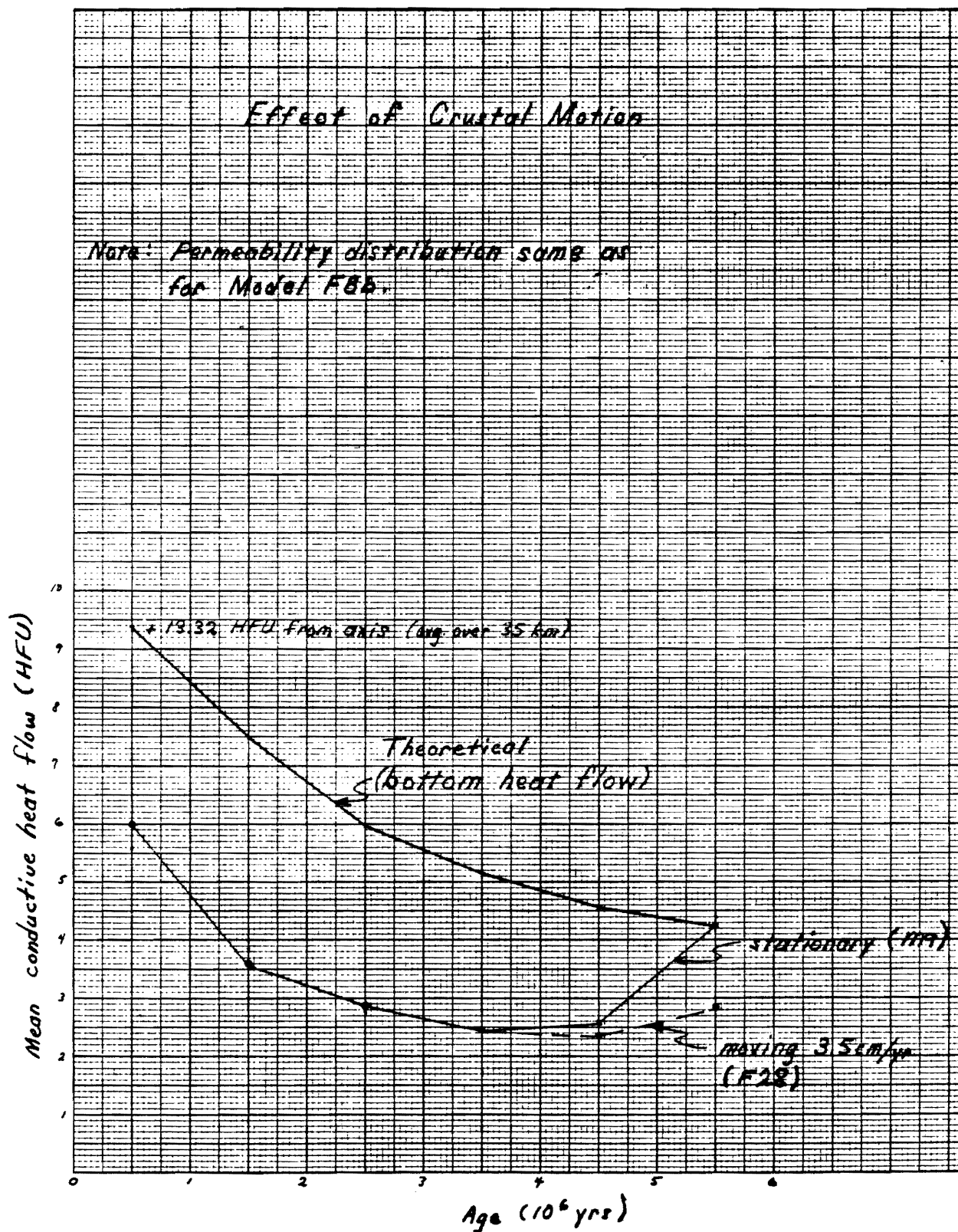
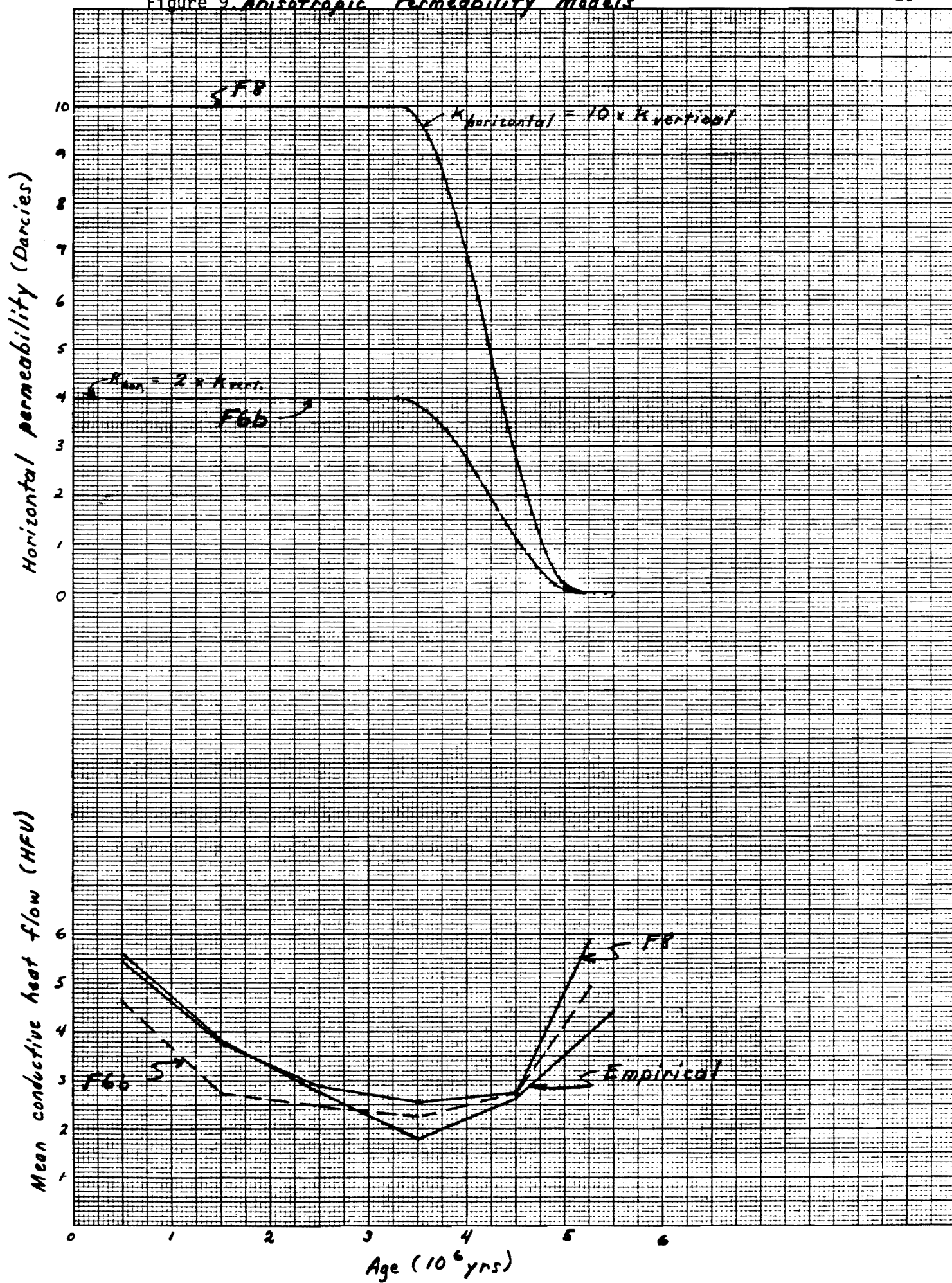


Figure 8. Effect of Crustal Motion.

Figure 9. Anisotropic Permeability Models





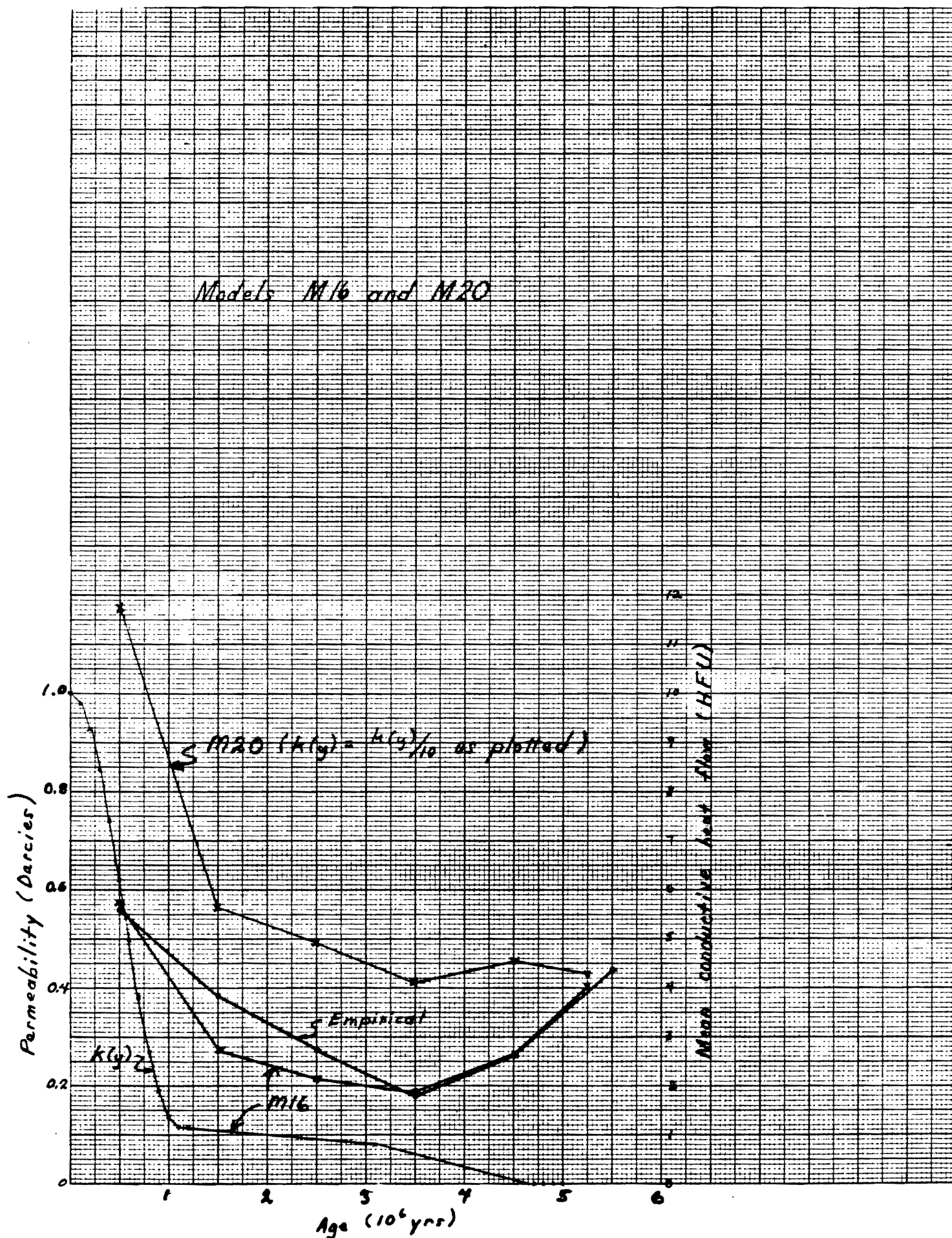


Figure 10: Models M16 and M20.



## Models M16b and M19

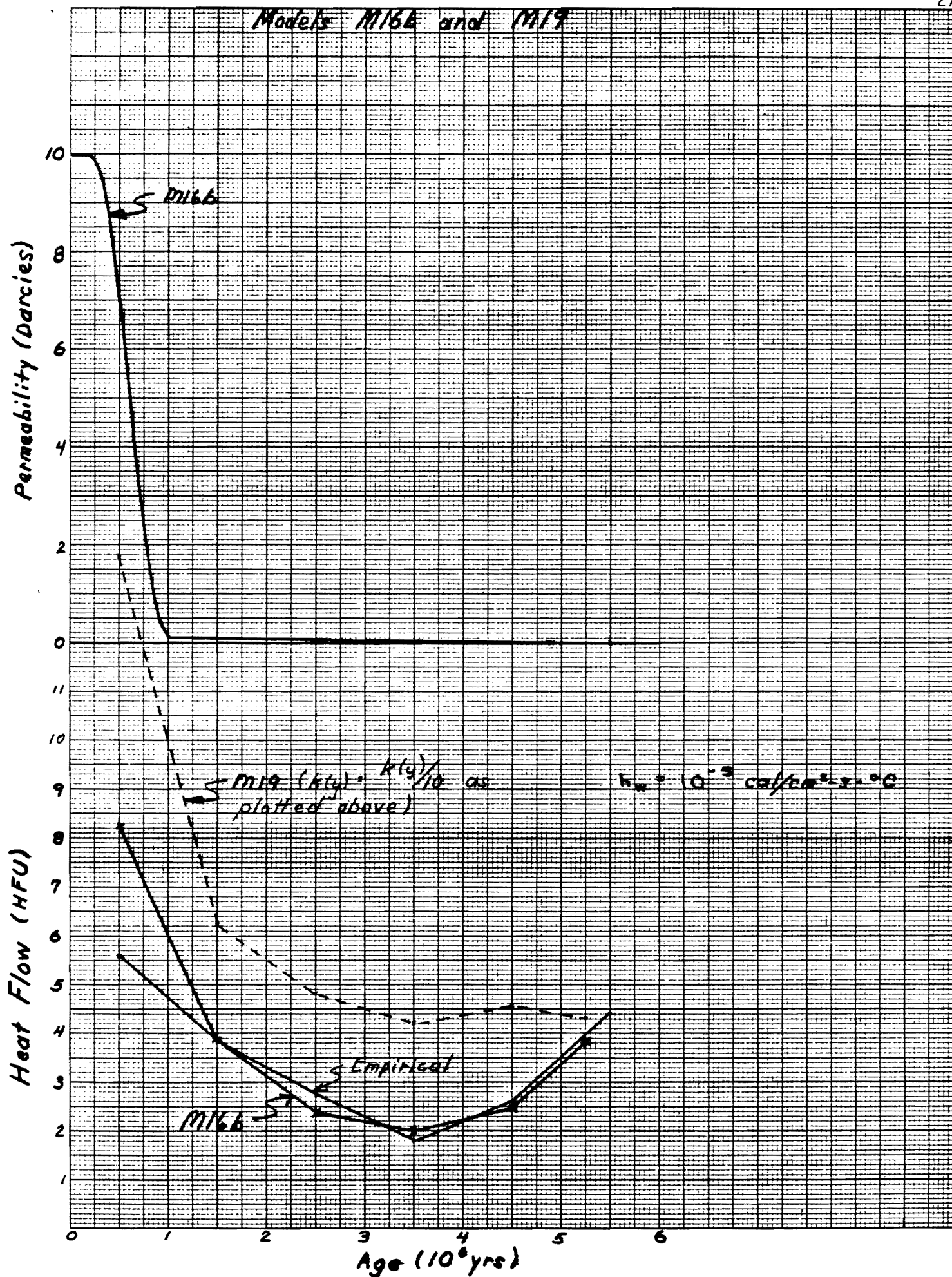


Figure 11. Models M16b and M19

calculated from empirical data. If crustal motion were considered for F8b (see Figure 8), the impermeable region would have to be expanded to include younger crust so that a sharper permeability transition at  $4 \times 10^6$  years would be required. Decreasing the heat transfer coefficient of F8b by a factor of 10 moves the heat flow down to curve F12 (Figure 6). Lower permeability values are required to move the heat flow means for F12 up to the empirical means. Thus the lower the heat transfer coefficient, the lower the required crustal permeability.

If crustal motion were considered for Model F8, the heat flow means (Figure 9 and compare Figure 8) would be brought into good agreement with the empirical means. To match the empirical means, model F6b requires lower permeabilities for the first  $2 \times 10^6$  years, implying an unrealistic increase in permeability with crustal age.

Models M16 (Figure 10) and M16b (Figure 11) use the heat transfer coefficient functions shown in Figure 5. Their permeability distributions are roughly proportional to these functions where  $\frac{\text{permeability in Darcies}}{\text{heat transfer coefficient}} \approx 10^6$  for crust younger than  $4 \cdot 10^6$  years. Model M8b obeys this approximation also. Models M20 (Figure 10) and M19 (Figure 11) show the effect of decreasing the permeabilities of models M16 and M16b by factors of 10. The upward displacements of the heat flow means are approximately equal to the downward displacement of the means for F8b when the heat transfer coefficient is increased by a factor of 10 (compare F8b and F12 in Figure 6).

The permeability to vertical fluid flow could be expected to be given by a function similar in form to that for the heat transfer function in Figure 5. For layers of permeability  $k_i$  and thickness  $\Delta_i$  in series, the overall permeability is:

$$k_v = \frac{\sum \ell_i}{\sum \ell_i / k_i} \quad (\text{Wooding, 1976}).$$

If the vertical extent of crustal permeability, crustal permeability  $k_c$  and sediment permeability  $k_s$  are assumed to remain constant with time, the overall vertical permeability as a function of sediment depth in kilometers,  $d$ , is

$$k_v = \frac{3.5 + d}{\frac{3.5}{k_c} + \frac{d}{k_s}} \approx \frac{1}{\frac{1}{k_c} + \frac{d/3.5}{k_s}}$$

If this value of permeability is used in the observed relationship between permeability and heat transfer coefficient:

$$\left(\frac{1}{\hat{h}_w} + \frac{d \cdot 10^5}{1.8 \cdot 10^{-3}}\right) \left(\frac{1}{k_c} + \frac{d/3.5}{k_s}\right)^{-1} \approx 10^6$$

a value of  $k_s = 0.005$  Darcies is obtained.

The crustal permeability values predicted by the models are high, on the order of 1-10 Darcies at the ridge axis. Such high values were predicted by Lister (1974) in his fracture propagation models for cooling oceanic crust. Lower values of permeability would be predicted by models with fluid circulation depths greater than 3.5 km or with lower heat transfer coefficients.

Models with greater circulation depths, however, would also have greater wavelengths for the convection cells. The average values of wavelength in crust younger than  $10^6$  years for the models are slightly greater than those of around 7 km observed in Corliss et al. (1979). Better agreement would be obtained if the depth of circulation were decreased. Close to the axis, such a decrease might be associated with a shallow magma chamber, so that the crustal temperatures would be above the cracking temperature.

It would also be difficult to justify a decrease in the heat transfer coefficient. Bodvarsson et al. (1967) measured the eddy conductivity,  $k_{\text{eddy}}$ , in the ocean bottom boundary layer to be  $\sim 0.1$  cgs. Based on  $k_{\text{eddy}}$  a boundary layer thickness,  $\delta$ , can be estimated for a given  $h$ :

$$k_{\text{eddy}} \frac{\Delta T}{\delta} \sim \hat{h}_w \Delta T \rightarrow \delta = \frac{k_{\text{eddy}}}{\hat{h}}$$

where  $\Delta T$  is the temperature drop across the layer. For  $\hat{h}_w = 10^{-5}$  cgs,  $\delta = 100$  m. The minimum  $k_{\text{eddy}}$  measured was 0.04. Generously assuming  $k_{\text{eddy}} = 0.01$  gives  $\delta = 10$  m for  $\hat{h}_w = 10^{-5}$ . Moreover, the lowest value of  $\hat{h}$  for water flow obtained from a text on heat exchanger theory is  $10^{-4}$  cgs (Whitaker, 1977). It seems that the assumption of  $\hat{h}_w = 10^{-5}$  cgs is rather generous.

The crustal circulation patterns for the models are approximately periodic. Horizontal temperature gradients generated by the influx of heat at the bottom boundary and at the axis initially generate a single cellular convecting system with fluid flowing down everywhere but at the axis. Unevenness of flow within this system in turn generates short wavelength circulation cells, and in steady-state there is only this one scale of convective flow. The horizontal influx of heat at the axis produces longer cellular wavelengths near the axis than when all heat enters vertically (compare Models F8b and M9 in Table 2). Anisotropies in permeability with  $k_y > k_x$  also produce increased wavelength at the axis. The average wavelength for models with low permeability is greater than for those with higher permeability (compare M16 with M20). In general the circulation produces no large scale horizontal transport

of heat. The transport in the convecting regions follows the fluid motion.

The maximum values of surface temperature for crust up to  $10^6$  years old (see Table 3) occur at the model ridge axis and are on the order of temperatures of hydrothermal fluids ( $7^\circ$  to  $17^\circ\text{C}$ ) measured at the Galapagos (Corliss et al., 1979). Quartz and magnesium solubility curves derived from measurements in the same fluids suggest  $300^\circ\text{C}$  as the temperature for seawater-rock interactions (Corliss et al., 1979). The temperatures at depth for the models are considerably lower than this. It must be remembered, however, that these are steady-state models and do not give details on the smaller time scale, episodic effects that are certainly associated with the crustal spreading process (Patterson, 1976, Patterson and Lowell, 1980).

### Conclusions

Porous media models can account for the heat flow anomaly at the Galapagos Spreading Center. For reasonable values of heat transfer coefficient at the ocean bottom, permeabilities on the order of 1-10 Darcies and depths of fluid circulation slightly less than 3.5 km are predicted at the ridge axis. Hydrothermal circulation continues for almost  $5 \cdot 10^6$  years and in crust younger than  $4 \cdot 10^6$  years the ratio between crustal permeability in Darcies and heat transfer coefficient in  $\text{cal}/^\circ\text{C-cm-s}$  is approximately  $10^6$ . The transport of heat is controlled by the convecting fluid and does not involve significant horizontal redistribution of the heat flow anomaly.

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#### STUDENTS SUPPORTED

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Ms. P. L. Patterson is currently completing her Doctoral dissertation under this grant.

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## APPENDIX

Topographically Driven Subcritical Hydrothermal  
Convection in the Oceanic Crust

by

Robert P. Lowell  
School of Geophysical Sciences  
Georgia Institute of Technology  
Atlanta, Georgia 30332

### Abstract

A simple analytical model for investigating topographically induced subcritical hydrothermal convection in either barren or thickly sedimented oceanic crust is developed. The results show that for unsedimented, low amplitude, wave-like topography, the maximum topographically induced vertical convective flow may be of the order of  $10^{-10}$  m/sec for a bulk crustal permeability of  $10^{-14}$  m<sup>2</sup> and topographic wavelength of  $10^3$  m.

The fluid ascends under topographic highs and descends at topographic lows. The convective heat flux is about 15% of the conductive background. The magnitude of the convective flow is independent of the topographic wavelength-layer depth ratio  $L/H$  if  $L \leq H/2$ , but for  $L \gg H$ , the convective flow depends on  $(H/L)^2$ .

If the crustal topography is completely covered with sediment of lower permeability, the convective flow is substantially reduced, perhaps by several orders of magnitude in some cases. Because the thermal conductivity of the sediment is less than that of the crust, the fluid descends at topographic highs and ascends at topographic lows.

Since the actual oceanic crustal topography is quite irregular, with a number of different amplitude and wavelength scales, the actual topographic convection pattern may be much more complicated than the model results given here. This may be especially true in regions where large amplitude outcrops occasionally protrude through a moderately thick sediment blanket and if supercritical Rayleigh convection is also present.

## Introduction

The occurrence of thermal convection in the oceanic crust was first hypothesized on the bases of conductive heat flow data [1 - 3] and alterations of dredged oceanic basalts [4]; however, there now exists rather extensive geochemical and geophysical data from the TAG hydrothermal field on the Mid-Atlantic Ridge [5 - 6] and from the Galapagos Spreading Center [7 - 10]. In fact, direct observations of hot water emerging from the Galapagos Ridge crest have been made from the submersible Alvin [11 - 12]. Although most of the data has been acquired near ocean ridge crests, heat flow measurements indicate that thermal convection may still be occurring in old oceanic crust in great distances from active spreading centers [13]. Moreover, the presence of non-linear temperature gradients in the upper few meters of sediment in older, thickly-sedimented oceanic crust has been attributed to thermal convection [14 - 15].

As the data has pointed more and more convincingly to the importance of convective processes in the oceanic crust several attempts have been made to develop theoretical models which account for the observations. For the most part, these models have been numerical in nature and have been based upon the standard Lapwood [16] model of convection in a porous slab, driven by vertical temperature gradients (e.g., [12]). Some numerical work, however, has also included the effect of horizontal temperature gradients due to intrusions at the ridge axis [18 - 19]. Models of convection based on widely-spaced discrete fractures [20 - 21] and on water penetration into hot rock [22] have also been developed.

An interesting aspect of thermal convection in the oceanic crust which has received comparatively little attention concerns the effect of irregular topography on the flow regime. Lister [23] first pointed out that heat flow across the Juan de Fuca Ridge correlates with topography in a manner opposite to the expected from topographic refraction of conductive heat flux. He suggested the importance of topographic control on the location of ascending and descending fluid and indicated schematically how the interplay between sediment cover and basement topography might determine the fluid convection patterns and conductive heat flow anomalies. The recent measurements of non-linear temperature gradients in older, sediment covered crust [14 - 15] also points to the possible importance of topographically induced convection.

Since these measurements have been made far from active ridge axes, the effect of intrusions and high heat flux from the base of the lithosphere should be minimal. The fluid may, in fact, be stable with regard to convection driven by vertical temperature gradients. Irregular basement topography, however, gives rise to horizontal temperature gradients and a fluid is automatically unstable under the action of such gradients. Thus, topographically driven convection may be a principal mechanism for fluid motions in regions of old, sediment covered oceanic crust, as well as being a significant factor in crust near active spreading centers.

The purpose of this paper is to examine some relatively simple models of convection in the oceanic crust driven by irregular topography, both in the case of young, barren oceanic crust as well as in the case of old, sediment covered crust. Hartline et al. [23] have

done some Hele-Shaw cell experiments on low Rayleigh number, topographically driven convection.

### Convection Driven by Irregular Topography-Simple Models

Let a saturated porous layer in which the upper surface is wave-like (Figure 1) represent the oceanic crust. In the case of unsedimented topography, the layer is bounded above by the ocean which, in effect, acts as a perfect heat sink so that the temperature at the seawater rock interface is  $T = 0$ . Moreover, the interface is assumed to be permeable so that seawater can enter and exit the porous layer. This condition is different from the impermeable boundary used in the Hele-Shaw cell experiments of Hartline *et al.* [23].

It is assumed that the temperature increases linearly with depth in the porous layer. Thus, on a horizontal plane within the layer, the temperature beneath the topographic highs is greater than beneath the topographic lows. The surface topography gives rise to horizontal temperature gradients which drive fluid convection in the porous layer. For unsedimented, or thinly sedimented crust, the fluid descends at topographic lows and ascends beneath topographic highs; consequently, the conductive heat flux will be lowered in regions of depressed topography and raised in regions of elevated topography as observed by Lister [3]. It will be seen that the flow pattern reverses in the case of crustal topography buried under a thick layer of sediment.

#### A. Boundary conditions and equations

The principal difficulty in treating the convection problem

described above stems from trying to satisfy the boundary condition  $T = 0$  on the wave-like upper boundary. To simplify the matter, and to keep the boundary condition in accord with a linearized approach to the problem, it is assumed that the topography is two-dimensional, of uniform wavelength  $L$  and amplitude  $d$  and that the topography is of low amplitude, such that  $d/L \ll 1$ . These assumptions permit the upper boundary to be represented by a simple trigonometric function. Moreover, the temperature boundary condition may be transformed from a condition  $T = 0$  at the surface to a condition of varying temperature on a horizontal boundary chosen to represent the actual surface.

Let a two-dimensional Cartesian coordinate system be situated with its origin beneath the point of greatest topographic height; the  $x$ -axis is horizontal and the  $z$ -axis is directed positively downwards such that the plane  $z = 0$  coincides with the point of lowest topography. Let the base of the porous layer be horizontal plane at depth  $z = H$ , and a uniform temperature gradient  $\beta$  be maintained across the layer. Then, neglecting heat flow refraction effects, the temperature condition at the upper boundary becomes

$$T(x,0) = (\beta d/2)(1+\cos kx) \quad (1)$$

where  $k$  is the wave-number of the topography,  $k = 2\pi/L$ .

Under steady state conditions, the periodically varying surface temperature (1) gives rise to a non-uniform temperature distribution within the porous layer, which, in turn, generates the convective instability. This instability occurs even if the Rayleigh condition for convectional instability due to the applied vertical gradient Lapwood [16] is not met. The possible interactions between

topographically driven convection and Rayleigh instability may be quite complicated and are beyond the scope of this paper. Only Rayleigh numbers less than critical will be assumed here.

In the subcritical regime, the convective flow is expected to be small so that a perturbation - iteration approach will be used to solve the coupled equations of heat and mass transfer. The steady state heat transfer equation for the perturbed temperature field is

$$\vec{v} \cdot \nabla T = a \nabla^2 T \quad (2)$$

where  $\vec{v}$  is the Darcian fluid velocity, and  $a$  is the "effective" thermal diffusivity given by the thermal conductivity of the rock divided by the heat capacity of the fluid. The perturbation equation for the fluid flow is given by Darcy's Law:

$$-\nabla P - (\eta/K)\vec{v} - \rho\alpha T\vec{g} = 0 \quad (3)$$

where  $P$  is the pressure,  $\eta$  the dynamic viscosity,  $K$  the permeability,  $\rho$  the fluid density,  $\alpha$  the thermal expansion coefficient of the fluid and  $\vec{g}$  the gravitational acceleration. Operating on (3) with  $\nabla \times \nabla \times$  and assuming the fluid to be incompressible yields

$$\nabla^2 w = -(\alpha g K / \nu) \partial^2 T / \partial x^2 \quad (4)$$

where  $w$  is the vertical velocity component and  $\nu$  is the kinematic viscosity  $\eta/\rho$ .

Equations (2) and (4) represent coupled partial differential equations for the velocity and temperature fields. These will be solved by an iteration technique which involves linearization and decoupling of the temperature and velocity fields. The first order temperature solution is found by assuming the velocity is zero in (2). This temperature solution is then substituted into (4) and the first order



velocity field is found. The second order temperature field is found using the first order velocity field, etc. A somewhat similar approach to convection driven by horizontal gradients has been given by Domenico and Palciauskas [24] and Allan et al. [25]. Linearization means that

$$\vec{v} \cdot \nabla T \rightarrow w\beta$$

Thus the iteration equations become

$$\nabla^2 T_n = \beta/a w_{n-1} \quad (5a)$$

$$\nabla^2 w_n = -(\alpha g K / \nu) \partial^2 T_n / \partial x^2 \quad (5b)$$

$$n = 1, 2, \dots \text{ and } w_0 = 0$$

Equations (5) are to be solved subject to the boundary conditions

$$T_n(x, 0) = T_n(x, H) = 0 \quad (6)$$

$$\partial w_n(x, 0) / \partial z = w_n(x, H) = 0$$

except that  $T_1(x, 0)$  is given by (1). The perturbed fields are then

$$T = \sum_{n=1}^p T_n$$

$$w = \sum_{n=1}^p w_n$$

## B. Sediment-free upper surface.

### 1. First order solution

The first order solutions are found in a rather straight forward manner.

$$T_1(x,z) = \beta d/2(1 + \cos kx) \frac{\sinh k(H-z)}{\sinh kH} - z/H \quad (7)$$

$$w_1 = - (\alpha g K \beta d / 4 \nu \sinh kH) \cos kx [1 + kH \tanh kH] \sinh k(H-z) \quad (8)$$

$$- k(H-z) \cosh k(H-z)$$

Equation (8) shows that the fluid is descending at topographic lows and ascending beneath topographic highs as expected. Moreover, the first order results show that the vertical velocity is proportional to the topographic amplitude whereas the convective heat flux  $Q_{c,1} = \rho s w_1 T_1$  is proportional to the amplitude squared. These results are in agreement with the observations of Hartline et al. [23].

It is also worthwhile to examine the magnitude of  $w$  at the surface  $z = 0$  as a function of wavelength - depth ratio  $kH$ .

$$w_1(x,0) = -(\alpha g \beta K d / 4 \nu) \cos kx [1 - 2kH \operatorname{csch} 2kH] \quad (9)$$

which for  $kH \ll 1$  yields

$$w_1(x,0) = - \frac{2\pi^2}{3} \frac{\alpha g \beta K d H^2}{\nu L^2} \cos kx \quad (10a)$$

whereas for  $kH \gg 1$

$$w_1(x,0) = - (\alpha g \beta K d / 4 \nu) \cos kx \quad (10b)$$

Thus the vertical velocity and convective heat flow become independent of topographic wavelength and layer depth for topographic wavelengths which are short in comparison to the layer depth.

## 2. Higher order terms

Before estimating the magnitude of the vertical velocity and convective heat flux, it is necessary to investigate the importance of higher order terms. To obtain the second order temperature terms,  $w_1$  is substituted in to (5a). It is clear that  $T_2(x,z) \propto \cos kx$ ; and from (5b) then,  $w_2(x,z) \propto \cos kx$  also. For all  $n$ , the  $\cos kx$  factor appears which indicates that in the linear theory, the topography controls the cell pattern. But more importantly, this feature allows separation of variables

$$T_n(x,z) = \theta_n(z) \cos kx \quad (11)$$

$$W_n(x,z) = \omega_n(z) \cos kx$$

Substituting (11) into (5), writing  $z^* = kz$ , and combining the resulting equations, one obtains a single equation for  $n$

$$\Omega^2 \omega_n(z^*) = \frac{\alpha g K \beta}{a \nu k^2} \omega_{n-1}(z^*) \quad (12)$$

where  $\Omega = D^2 - 1$ , and  $D^2$  represents  $d^2/dz^{*2}$ . Thus the  $n^{\text{th}}$  order velocity may be found from  $(n-1)^{\text{st}}$ . Moreover, successive applications of  $\Omega^2$  on (12) allows one to obtain an equation for  $\omega_n$  in terms of  $\omega_1$ . Thus

$$\Omega^{2(n-1)} \omega_n = A^{n-1} \omega_1 \quad (13)$$

where

$$A = \alpha g K \beta / a \nu k^2 \quad (14)$$

A similar equation may be derived for  $\theta(z^*)$ .

The second order velocity term will be derived assuming  $kH \rightarrow \infty$ . Then

$$\omega_1(z^*) = C (z^* + 1) e^{-z^*} \quad (15)$$

where

$$C = - \alpha g K \beta d / 4 \nu \quad (16)$$

Substituting (15) into (13) one obtains

$$\omega_2 = \frac{AC}{2} [1 + z^* + z^{*2}/2 + z^{*3}/12] e^{-z^*} \quad (17)$$

and the maximum upward vertical velocity, to second order is:

$$\begin{aligned} \omega(0) &= \omega_1(0) + \omega_2(0) \\ &= C(1 + A/2) \end{aligned} \quad (18)$$

and since the higher order  $\theta_n$  terms are zero at  $z = 0$ , the maximum second order convective heat transport is

$$Q_c = \rho s \beta d C (1 + A/2) \quad (19)$$

The result (18) and the form of the equation (13) suggests that

$$\omega(0) \propto \sum_{n=1}^p A^{(n-1)}$$

and convergence of the iteration procedure is possible if  $A < 1$ . But, since the critical Rayleigh number,  $R_c$ , for convection in a slab with uniformly heated, plane horizontal boundaries is  $4\pi^2$ ,  $A$  is simply the ratio  $R/R_c$ , where  $R$  is the Rayleigh number defined on the basis of topographic wavelength. Therefore, if  $R \ll R_c$ , the maximum velocity and heat flux through the upper boundary are approximately given by the first order results, whereas if  $R = R_c$ , even second order results give an increase of about 50%. Thus the flow rate and heat transfer due to topographically driven convection increase markedly as the Rayleigh number approaches the critical number. This result is in agreement with the observations of Hartline et al. [23]. An essentially similar result would be expected for a finite layer except that the velocity and convective heat flux would be modulated by the dimensionless scale  $kH$ .

### 3. Numerical example

To obtain a numerical estimate let

$$\alpha = 5 \times 10^{-4} / ^\circ\text{C}; \quad g = 10 \text{ m/sec}; \quad \beta = 0.1^\circ\text{C/m}; \quad \nu = 10^{-6} \text{ m}^2/\text{sec}; \quad d = 100 \text{ m}$$

Continuing with the assumption  $kH \gg 1$  (in reality  $L < 2H$  satisfies the criterion reasonably well); and assuming  $L = 10^3 \text{ m}$  and  $a = 0.5 \times 10^{-6} \text{ m}^2/\text{sec}$  requires that  $K < 4 \times 10^{-14} \text{ m}^2$  in order to have  $R < R_c$ . Using this value of  $K$  gives, to second order

$$\omega_2(0) = 7.5 \times 10^{-10} \text{ m/sec} \quad (20)$$

$$Q_{c,2}(0) = 30 \text{ mW/m}^2$$

A temperature gradient of  $\beta = 0.1^\circ\text{C/m}$  gives a background conductive heat flux of about  $200 \text{ mW/m}^2$ ; thus topographically driven convection may modify the heat output by more than 15%, in young, unsedimented oceanic crust - even assuming a subcritical Rayleigh number.

It should be mentioned that the results (20) are valid only for topographic wavelengths in the range  $d \ll L < 2H$ , which in the present example requires  $L$  to be between a few hundred meters and a few kilometers. Equation (20) is derived assuming a median value of  $L$ . If  $L$  is taken to be a little smaller the estimates of heat flux and velocity increase somewhat (as  $K$  is allowed to increase). If  $L$  is taken to be larger, the effect of finite layer depth becomes important and the estimated heat flux and velocity decrease, both because (1)  $K$  must be smaller to satisfy the assumption of subcritical convection and (2) because  $w_1 \propto (kH)^2$  as  $kH$  becomes small.

#### C. Sediment covered topography

If the topography is completely covered with a layer of sediment (i.e. no outcrops) of thickness  $h$  (Figure 2), then the boundary conditions must be modified somewhat. The heat transport and fluid flow

equations (2) and (4) must be solved separately in the sediment layer and crustal layer and joined at the crust-sediment interface, which is still designated  $z = 0$  in the small amplitude approximation. Let the sediment layer be designated  $s$  and the oceanic crust be designated  $c$ . Only first order solutions will be obtained. Moreover the topographic wavelength-crustal thickness ratio will be assumed to satisfy  $kH \gg 1$ .

Assuming the sediment-ocean interface to be a horizontal plane, the boundary conditions are:

$$T_s = 0 \quad (21)$$

$$z = -h$$

$$\partial w_s / \partial z = 0$$

In the crust, as  $z$  approaches infinity, the conditions are

$$T_c = 0 \quad (22)$$

$$z \rightarrow \infty$$

$$w_c = 0$$

At the crust-sediment interface, the conditions are

$$T_s = T_c = T_0 (1 + \cos kx) + \beta_s h \quad (23)$$

where  $T_0 = (\beta_c - \beta_s) h/2$ , and  $\beta_s$ ,  $\beta_c$  are the temperature gradients in the sediment and crust, respectively; and

$$w_s = w_c \quad \text{at } z = 0 \quad (24)$$

$$(1/K_s) \partial w_s / \partial z = (1/K_c) \partial w_c / \partial z$$

With these conditions, the sediment and rock temperature distributions are found to be

$$T_s = [T_0(\cos kx)] \frac{\sinh k(z+h) + (T_0 + \beta_s h)(1+z/h)}{\sinh kh} \quad (25)$$

$$T_c = [T_0(\cos kx)] \exp(-kz) + T_0 + \beta_s h \quad (26)$$

the vertical velocity at the sediment-seawater interface is found to be

$$w_s(-h) = \frac{\alpha g K_c \beta_c d \cos kx (\beta_s / \beta_c - 1)}{4 \nu} \left\{ \frac{1 - K_c / K_s}{(K_c / K_s \sinh kh + \cosh kh)} + \frac{(K_s / K_c) kh}{\sinh kh} \right\} \quad (27)$$

Except for a minus sign, the first factor in (27) is identical to the vertical velocity in the sediment-free case discussed above. The terms in parentheses and in brackets denote the modifications to the velocity brought about by the temperature gradient contrast and the permeability contrast between the sediment and crust, respectively. The sign of the vertical velocity is particularly significant because it indicates that the flow pattern is reversed from its direction in the sediment-free case. The reason for this reversal is that in the sediment-covered case, the low thermal conductivity of the sediments gives rise to the highest temperatures at the sediment-crust interface in regions of low topography. Thus, in sediment covered crust, the fluid ascends at

regions of low topography and descends at regions of high topography whereas the reverse flow pattern was deduced for sediment free crust. This expected reversal in flow pattern was first pointed by Lister [3].

Since the ratio of the thermal conductivity in the sediment to basalt is typically 1:2.5, then

$$(\beta_s/\beta_c - 1) \sim 1.5$$

The magnitude of the term in brackets, depends upon the permeability ratio and on the sediment thickness-topographic wavelength ratio. Figure (3) shows the factor in brackets, denoted  $F(K_s/K_c, kh)$ , as a function of  $kh$  for several values of  $K_s/K_c$ .

Figure (3) shows that  $F$ , and hence the vertical flow rate  $w_s(-h)$  at the sediment-seawater interface, falls off rapidly as the ratio of sediment thickness to topographic wavelength increases. Moreover, as the ratio of sediment permeability to crustal permeability decreases, the decline in flow rate is markedly rapid. But it is emphasized that the model holds only for completely covered crustal topography. Thus extremely small values of  $kh$  are physically meaningful only if the topographic height/wavelength ratio is also correspondingly small. To give a physically meaningful example, therefore, let  $kh = 1.0$ . Then the flow rate at the sediment-seawater interface is reduced by: 0.23; 0.026; 0.003 for  $K_s/K_c = 0.1$ ; 0.01; 0.001, respectively (and assuming  $\beta_s/\beta_c - 1 = 1.5$ ). The convective heat flux across the interface is reduced in a similar manner.

### Discussion and Conclusions

Recent conductive heat flux measurements in well-sedimented oceanic crust show the presence of non-linear temperature gradients in the upper several meters of the sediment layer [14, 15, 26]. These non-linear



gradients are attributed to vertical water flow through the sediment at rates ranging from roughly  $10^{-10}$  m/sec [15] to  $10^{-7}$  m/sec [26]. Von Herzen's [15] data further shows a correlation of heat flow with topography which suggests that the convective flow is topographically forced. It is clear from the subcritical models developed here that topographically driven convection of  $10^{-10}$  m/sec may occur in barren, or thinly sedimented, young oceanic crust; however, a high permeability contrast may cause a marked decrease in the convective flow in regions of thickly sedimented older crust. Thus if the convective flow postulated to account for the observed non-linear gradients [15] is driven by subcritical, topographically driven convection. Figure 3 indicates that the sediment permeability must not be much more than an order of magnitude smaller than the underlying crustal material (i.e.  $K_s \sim 10^{-15} \text{ m}^2$ ). This is a somewhat high, but not totally unreasonable value. The high velocity of  $10^{-7}$  m/sec [26], would seem to indicate convection that is in the supercritical regime and hence beyond the realm of applicability of the models presented here.

The situation of intermediate sedimentary cover, that is, incomplete coverage of basement topography, has not been considered. This is a somewhat more complicated problem than the end-member cases considered here for both thermal and mechanical reasons. First, the incomplete sediment blanket may or may not give rise to temperature maxima at topographic lows and minima at topographic highs, so the sense of the flow pattern is not entirely clear. Secondly, with only partial sediment cover, seawater still has direct access to the relatively highly permeable oceanic crust. Thus there will be a tendency for fluid to be channeled through the crust from outcrop to outcrop, with little

flow in the overlying sediment. In fact, since there is a somewhat irregular range of amplitudes and topographic wavelengths, with the highest amplitude topography protruding the sediment, topographic convection may exist on two spatial scales. One scale might reflect flow driven by small and moderate amplitude, buried topography, whereas a larger spatial scale flow, which reflects a channeling effect from outcrop to outcrop, might be superimposed upon the small scale convection.

Thus, it seems that topographically forced convection may be important in the oceanic crust, even in moderately and thickly sedimented region's provided the permeability contrast is not too great; however, the details of the flow patterns and the resulting non-linear temperature gradients may be difficult to analyze for any particular region on the basis of existing data. Measurements of sediment and crustal permeabilities and thermal conductivities are needed, as is an accurate determination of the topographic spatial scales and amplitudes. Moreover, the interaction between topographic effects and supercritical Lapwood-Rayleigh convection may be important.

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Figure 1. Model for sediment-free, low amplitude, wave-like crustal topography.

Figure 2. Model for sediment covered, low amplitude, wave-like crustal topography.

Figure 3. The vertical velocity reduction factor  $F(K_s/K_c; kh)$  as a function of  $kh$  ( $kh = 2\pi h/L$ ) for several sediment-crust permeability ratios.

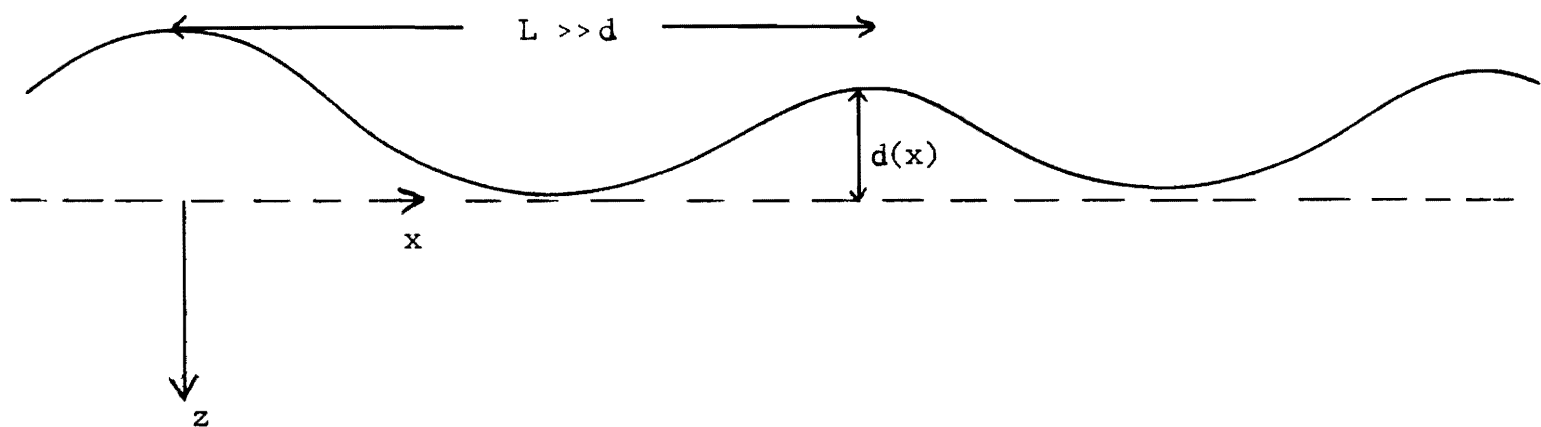


Figure 1.

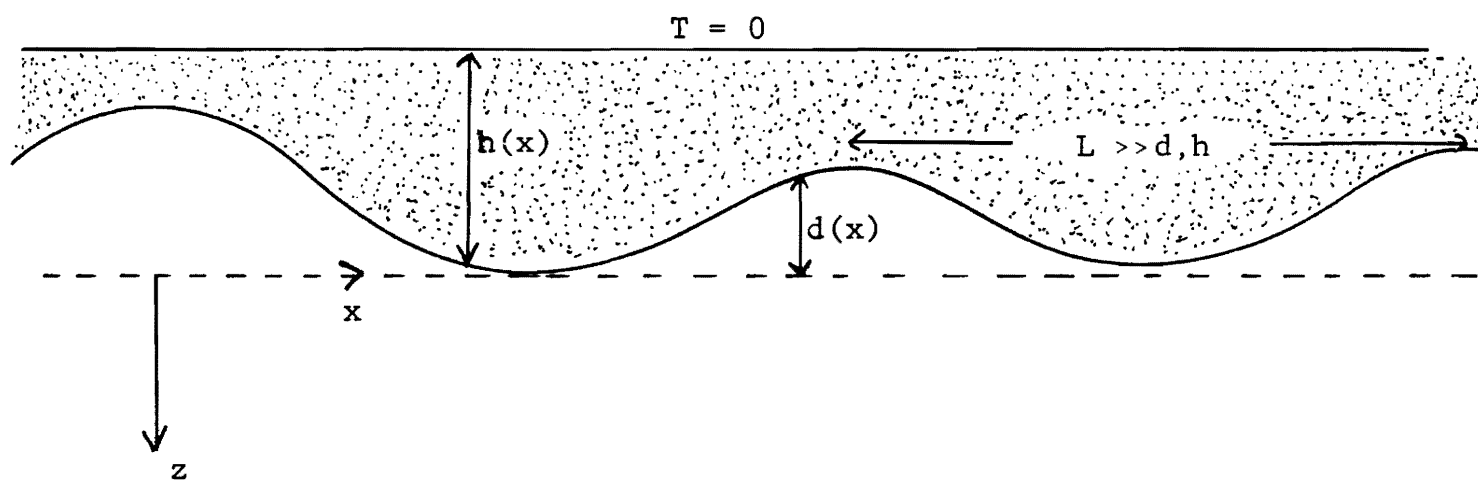


Figure 2.



