

# Dynamic Assemblies of Soft Colloids

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CCNE

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# Nanoscience and Colloids

Colloidal media have occupied a critical place in the history of “nanoscience”...

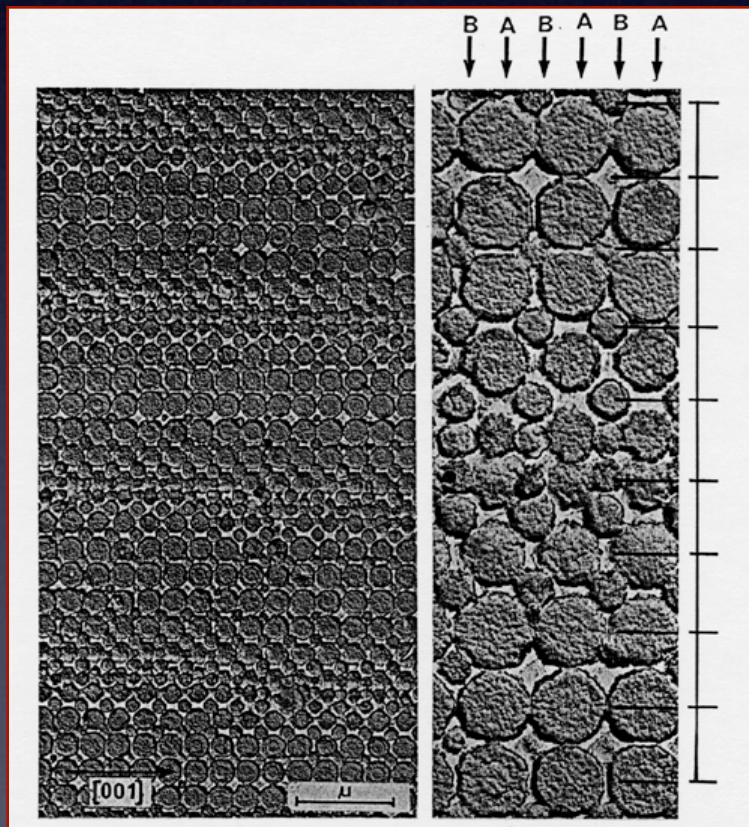
- Quantum confinement:
  - Semiconductor nanoparticles/clusters
- Plasmonics:
  - Metal nanoparticles
- Nanocomposites for reinforcement:
  - Carbon nanotube dispersions



# Colloidal Dispersions

...while colloidal dispersions/assemblies have existed far longer than “nano”.

Sanders, J. V. *Phil. Mag. A* 1980, 42, 705-720.



Royal Institution of Great Britain





# Colloidal Energetics/Dynamics

How do colloidal assemblies differ from atomic/molecular assemblies?

- Number Density

- $\sim 10^{13} \text{ cm}^{-3}$  (colloidal) vs.  $\sim 10^{22} \text{ cm}^{-3}$  (atomic).

- Stability

- because “strength”  $\propto$  density, colloidal crystals are  $\sim 1$  billion times weaker than atomic crystals.

- Dynamics (Relaxation Time)

- $\sim 10^{-2} \text{ s}$  (colloidal) vs.  $\sim 10^{-11} \text{ s}$  (atomic)



# Hard- and Soft-Sphere Phases



# Hard Sphere Phases



0.637

0.621

0.595

0.578

0.553

0.528

0.512

0.502

0.478

Glass  
Mainly

Crystal  
Heterogeneous

Fully  
crystallized

Coexistence

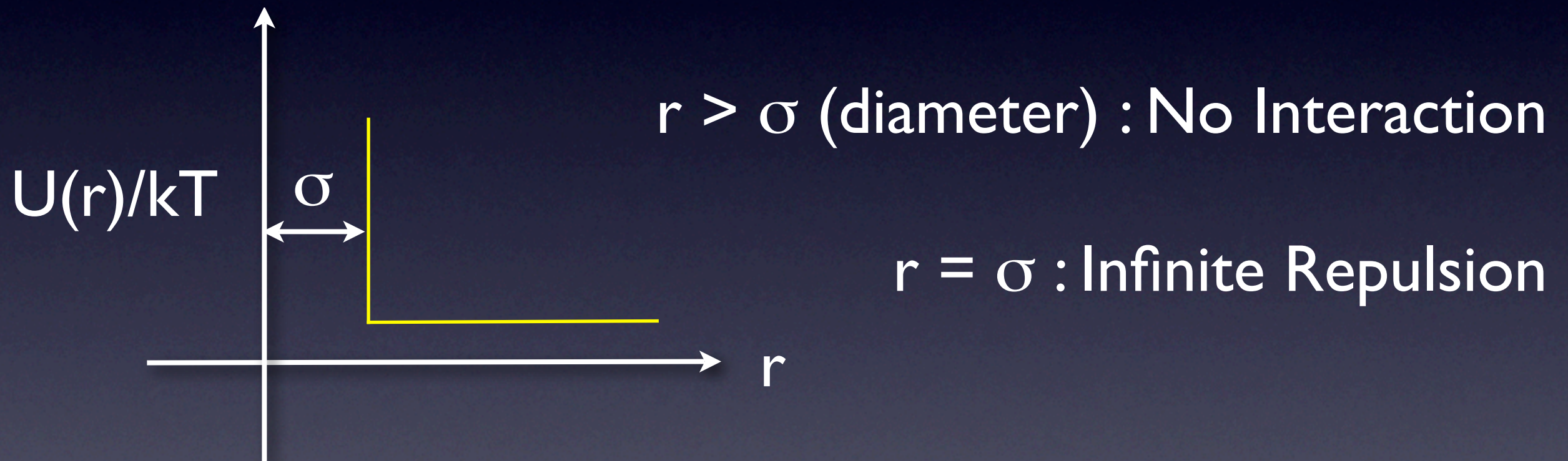
Liquid

Pusey, P. N.; van Megan, W. *Nature* **1986**, 330, 340-342.



# Interparticle Interactions

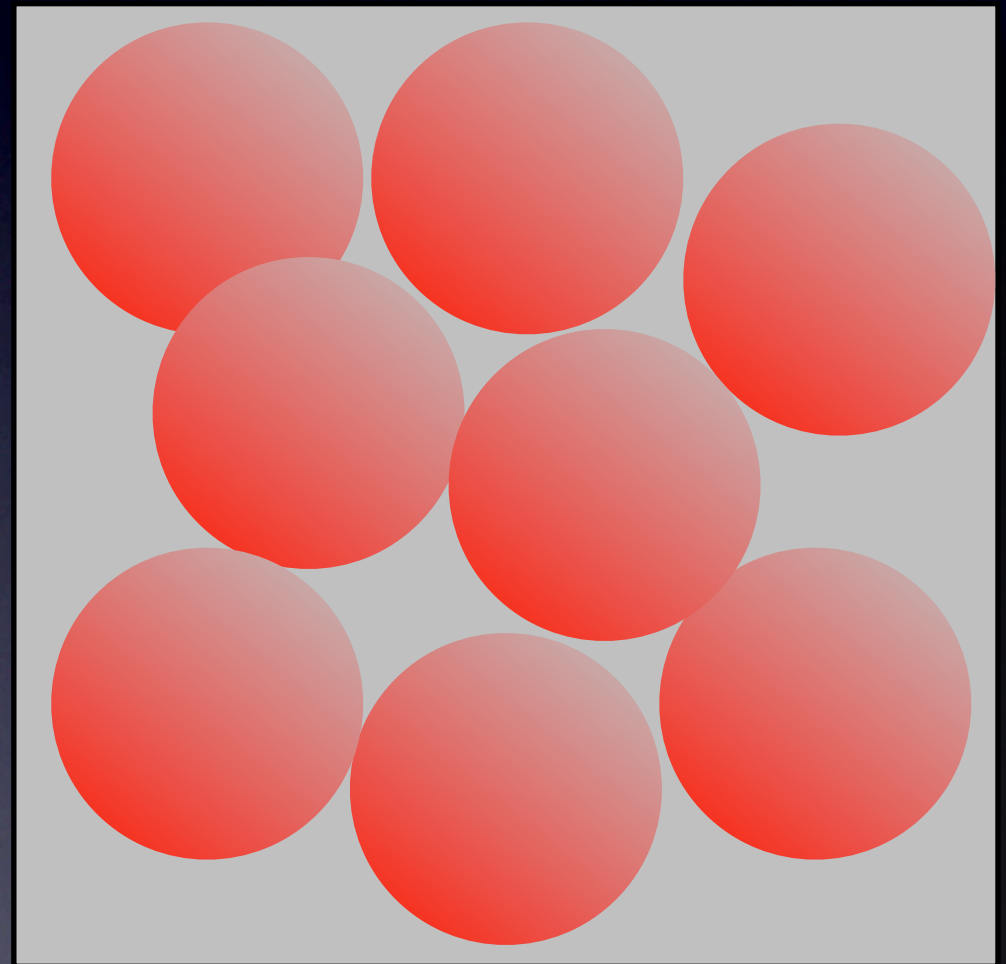
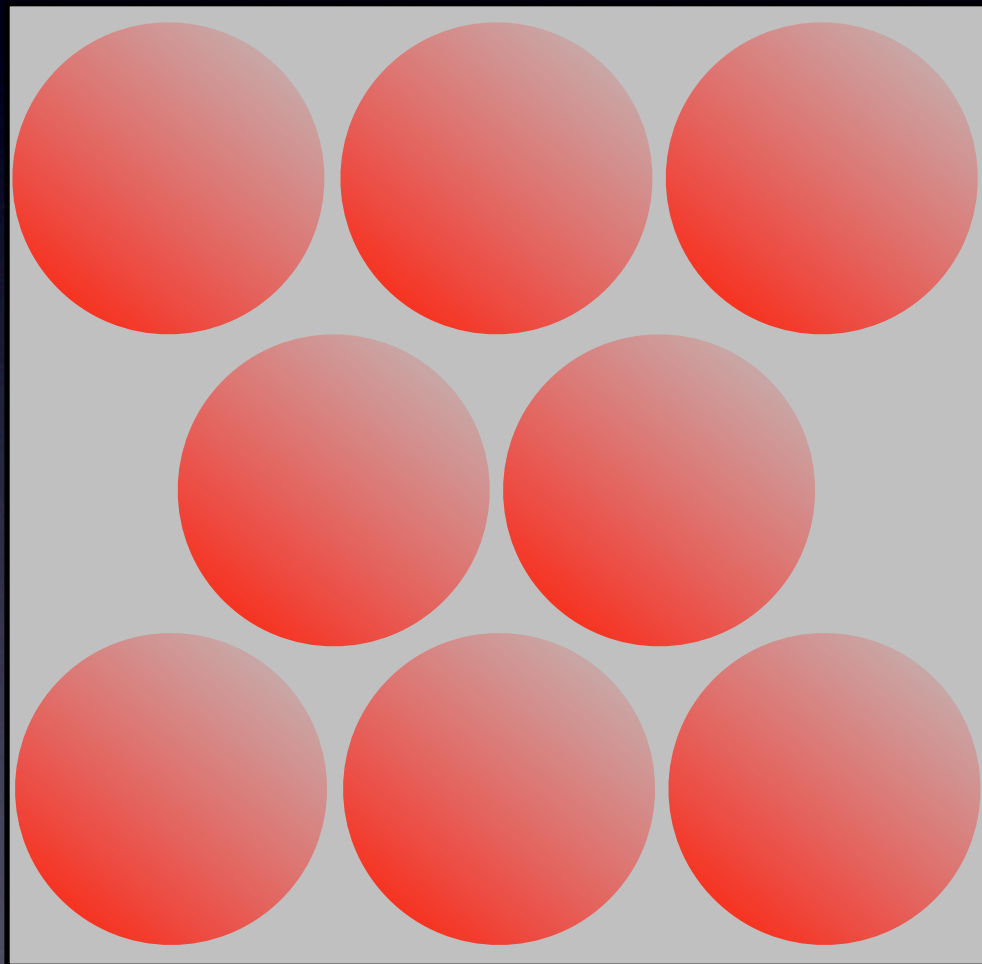
Repulsive hard sphere interactions can be modeled as a square potential.





# Entropic Crystallization

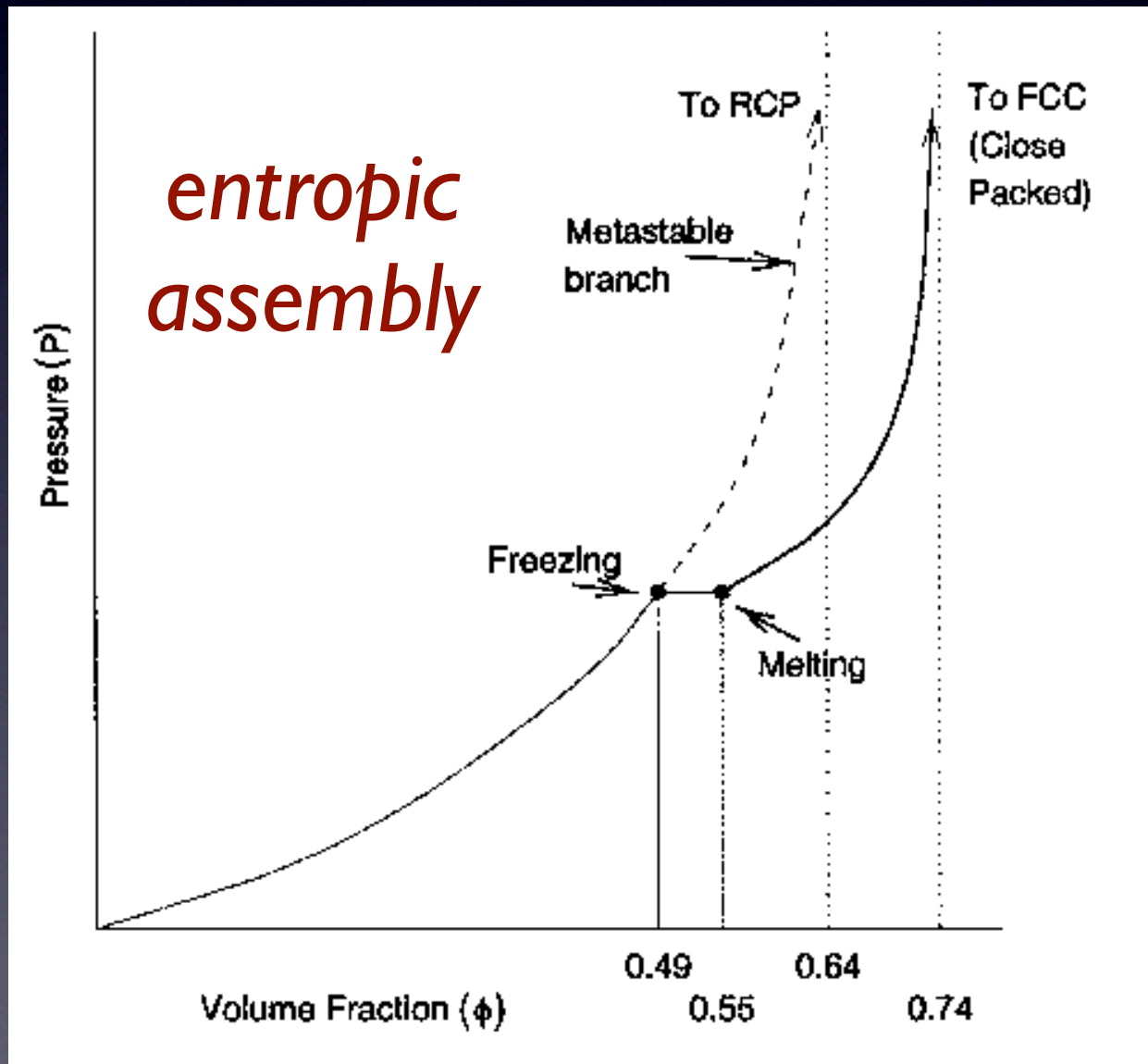
Hard spheres self-organize to maximize entropy.



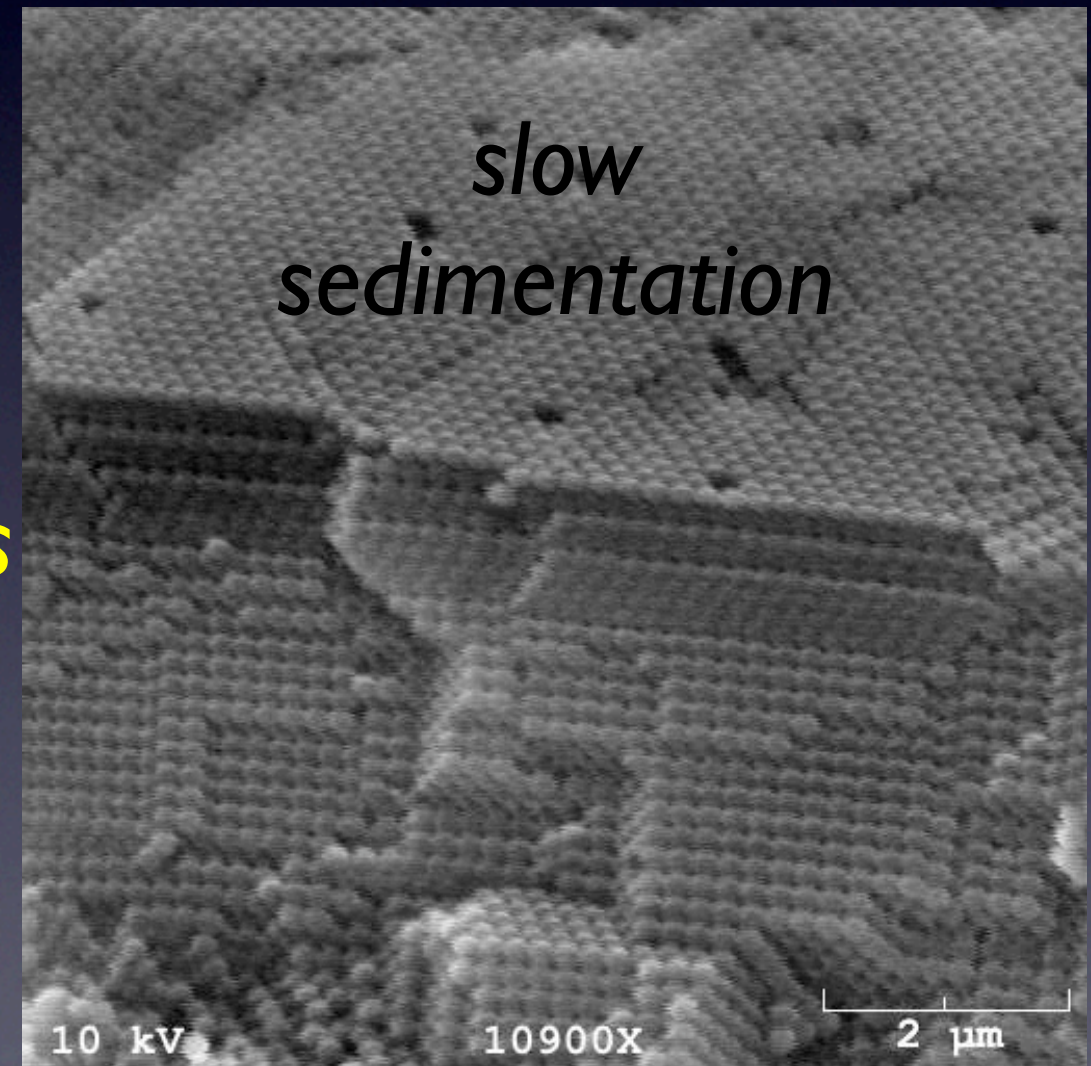


# Hard Sphere Assembly

From a practical standpoint, energetically-minimized, close-packed phases of hard spheres cannot be easily prepared.



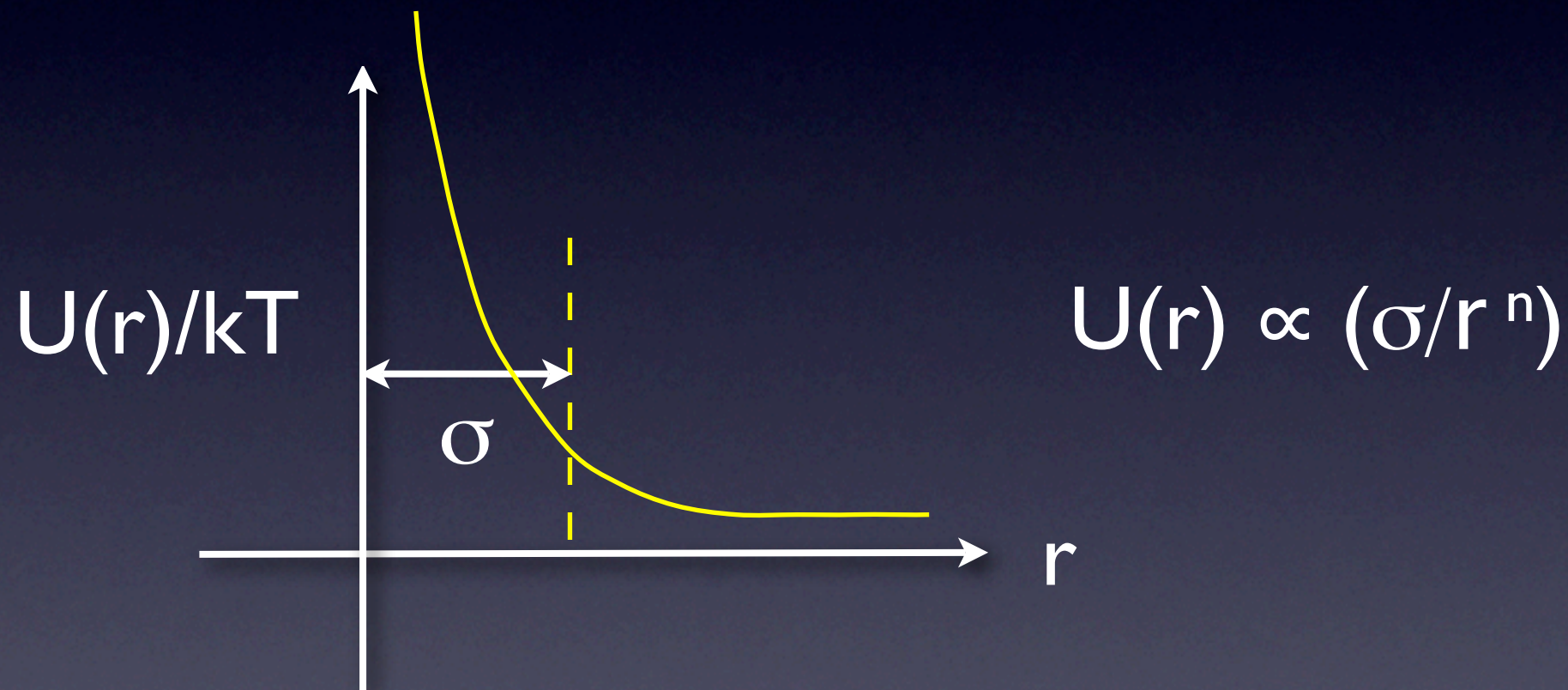
*versus*





# What about Soft Interactions?

A power law potential can be used describe interpenetrating or deformable spheres.





# Soft Colloidal Phases

How does *particle softness* manifest itself...

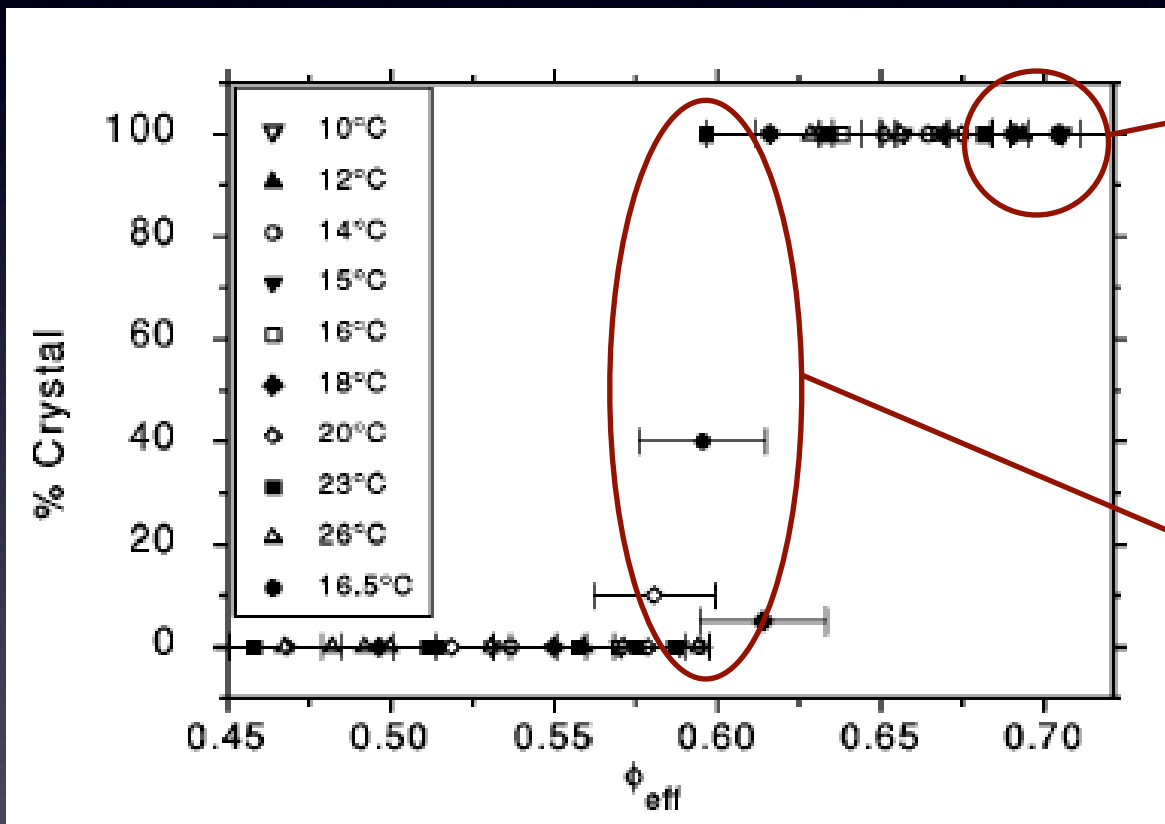
- ▶...in the phase behavior?
- ▶...in the optical properties?
- ▶...in defect healing?
- ▶...in the assembly's dynamics?

What are the appropriate tools to study phenomena in soft assemblies?



# Soft Colloidal Phases

Some evidence (experimental and theoretical) of softness impacting the phase behavior.



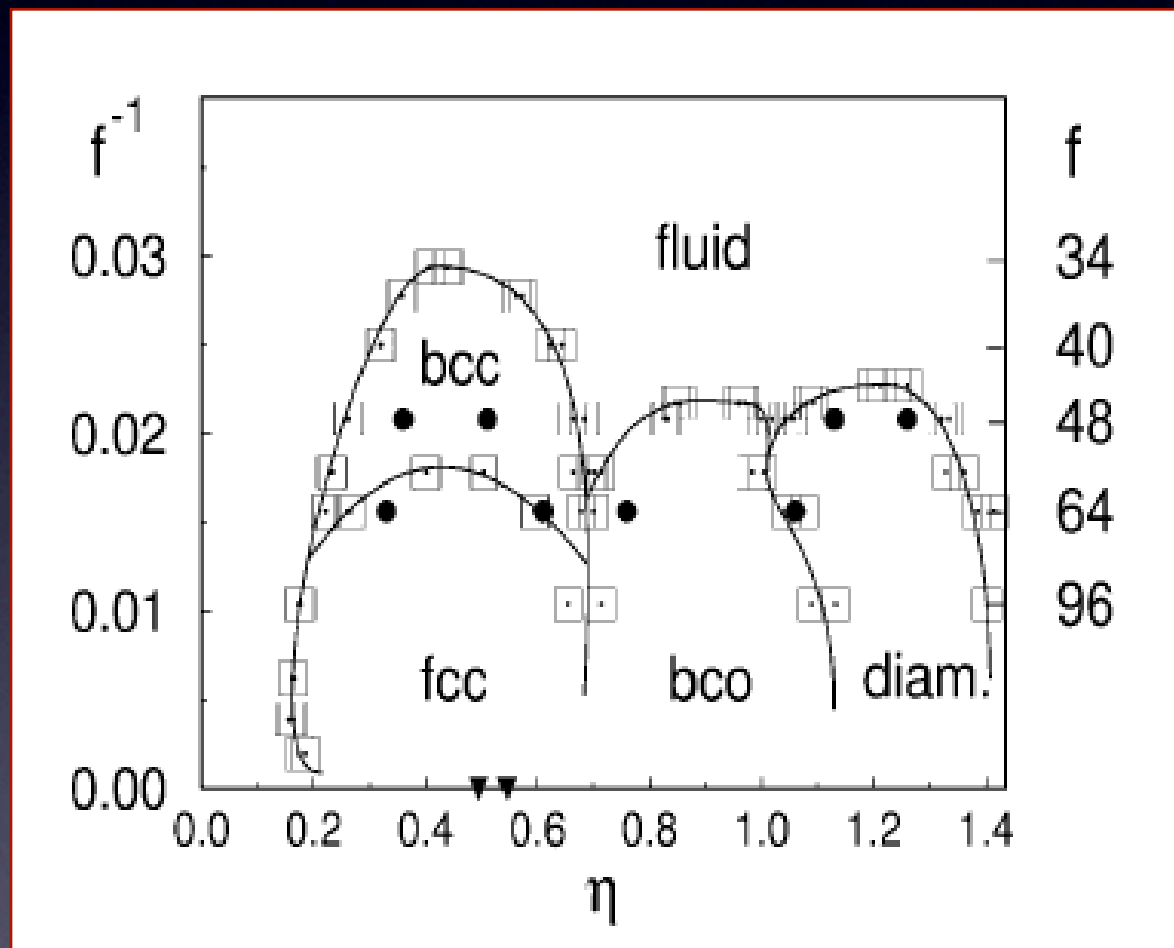
“True” thermodynamic close-packed phases can be prepared.

Liquid-to-crystal transition for hydrogel particles occurs at higher volume fractions and over a more narrow concentration range than for hard spheres.



# Soft Colloidal Phases

Some evidence (experimental and theoretical) of softness impacting the phase behavior.



Unusual non-close packed and anisotropic phases predicted.

M. Watzlawek, et al., *Phys. Rev. Lett.* **1999**, 82(26), 5289.

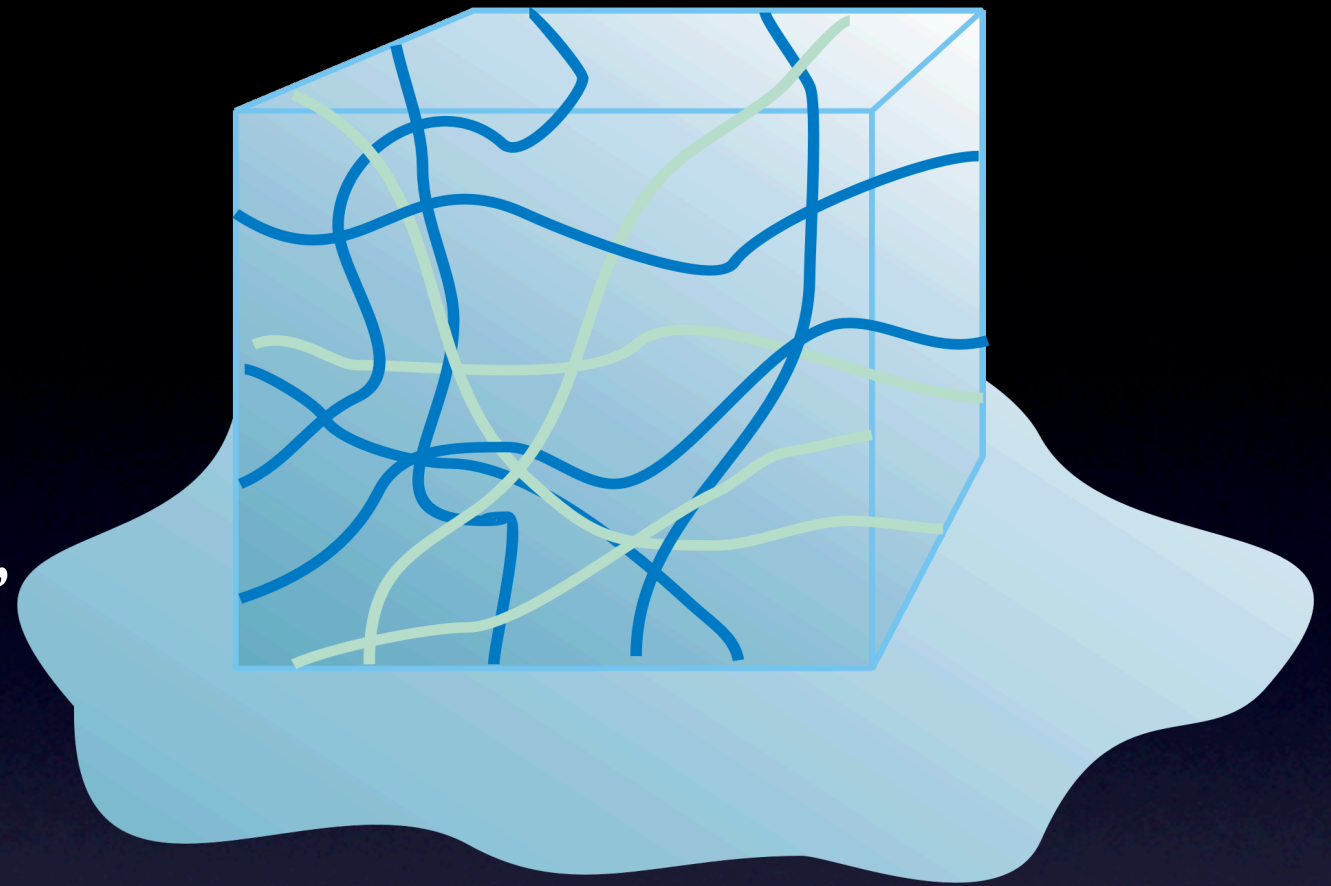


# Microgels as a Soft Sphere Model System



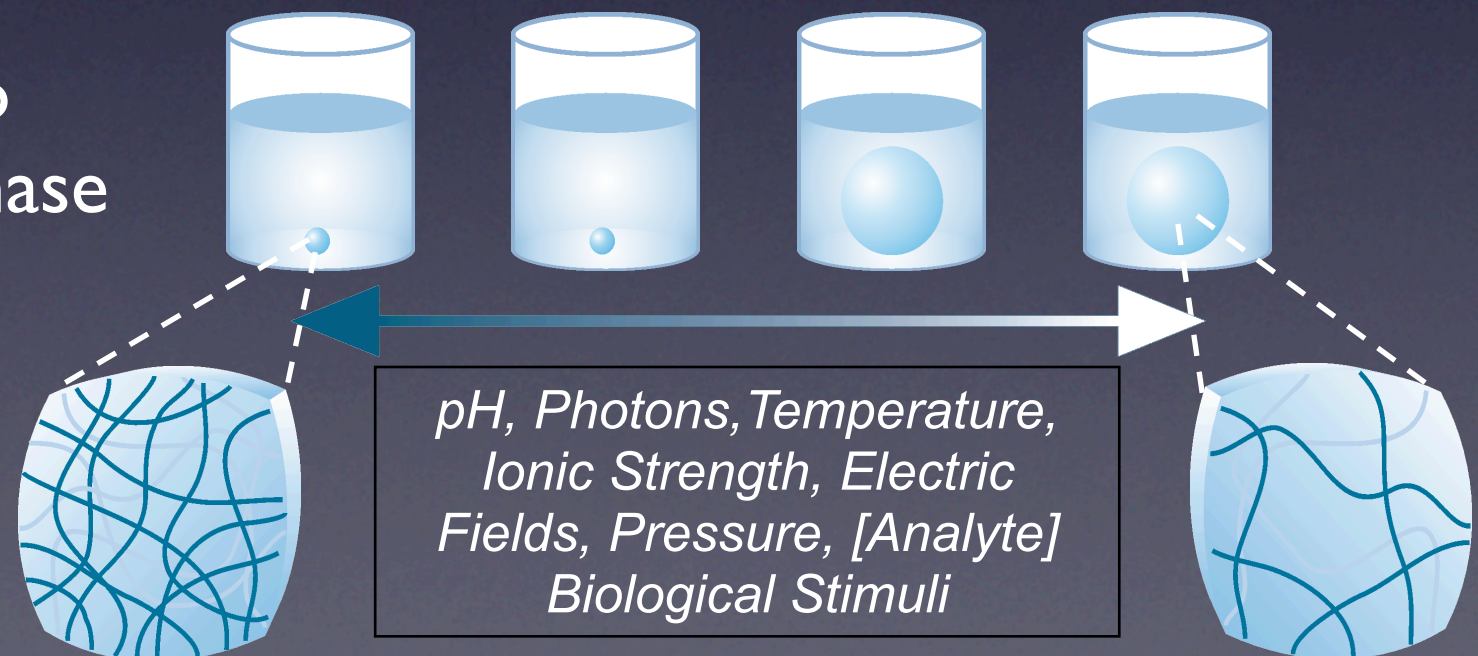
# Hydrogels

- Cross-linked water soluble polymers - a physically restricted, dimensionally-stable, polymer solution.



## Responsive Hydrogels

- Polymeric gels that undergo environmentally initiated phase separation events (**volume phase transition**)

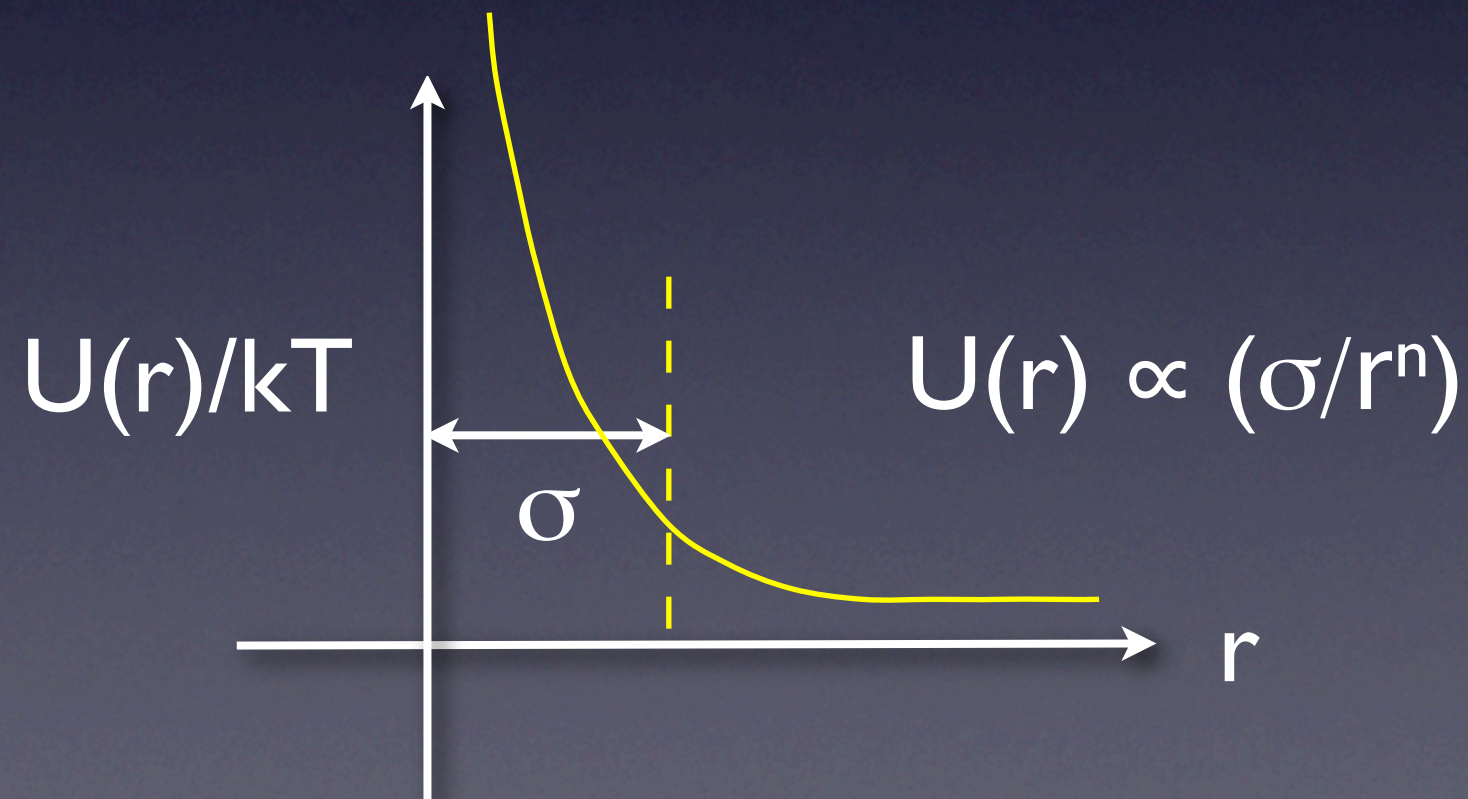




# Gel Swelling Thermodynamics

Gel swelling includes contributions from the free energy of mixing and chain elasticity.

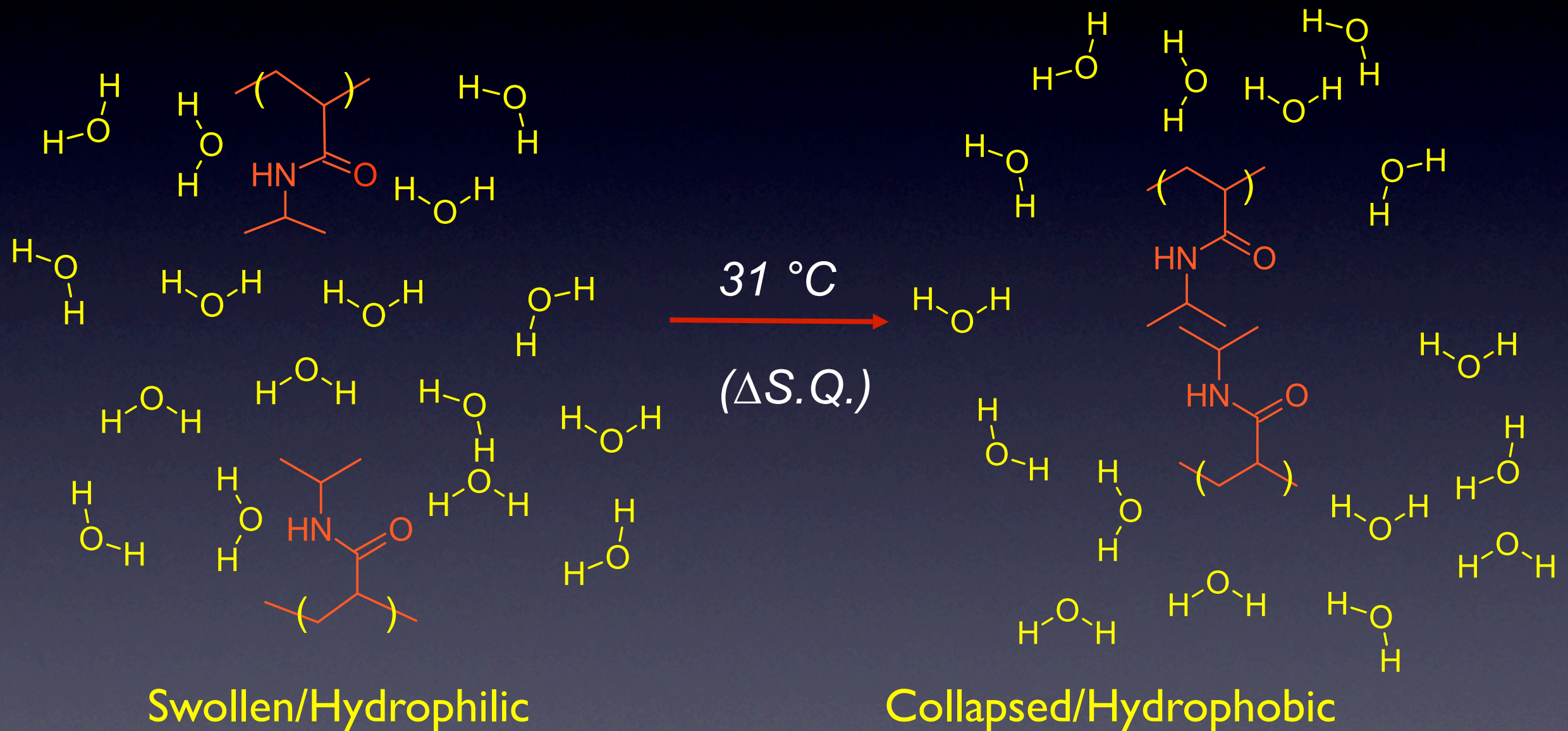
$$\frac{\pi}{k_B T} = \frac{\pi_{el} + \pi_M}{k_B T} = \frac{n_0}{N_x} \left[ \frac{1}{2} \left( \frac{n}{n_0} \right) - \left( \frac{n}{n_0} \right)^{\frac{1}{3}} \right] - \frac{1}{v} \left[ \ln(1 - nv) + nv + \chi n^2 v^2 \right]$$





# Responsive Polymers

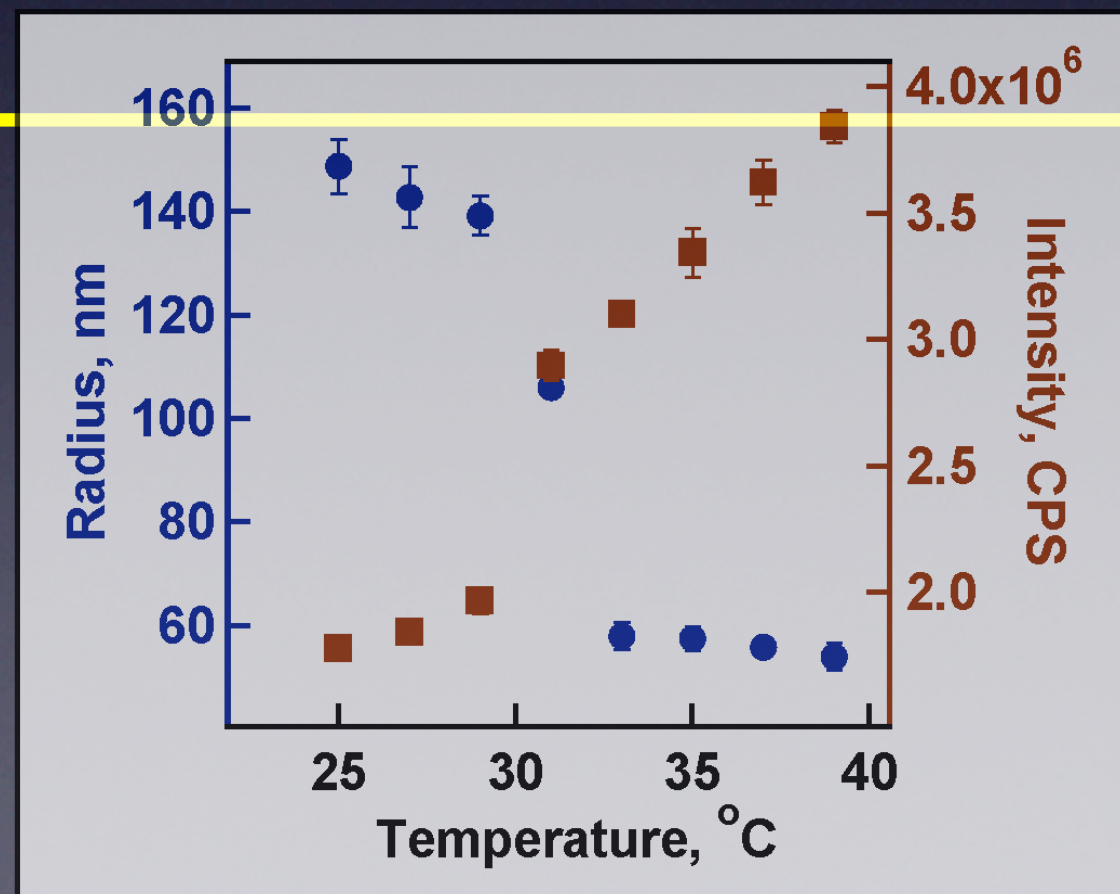
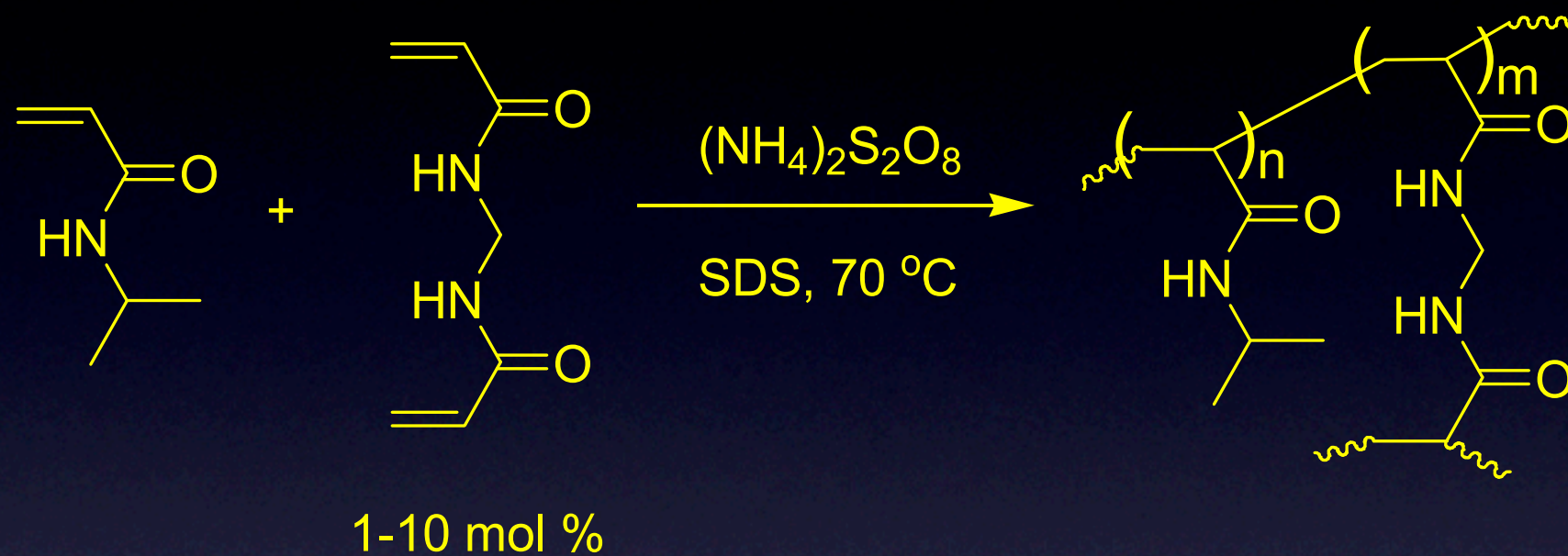
*poly(N-isopropylacrylamide)* (pNIPAm)



Heskins, M.; Guillet, J. E., *J. Macromol. Sci. Chem.* **1968**, A2, 1441-1455.  
Tanaka, T., *Phys. Rev. Lett.* **1978**, 40, 820-823.  
Annaka, M.; Tanaka, T., *Nature* **1992**, 355, 430-432.

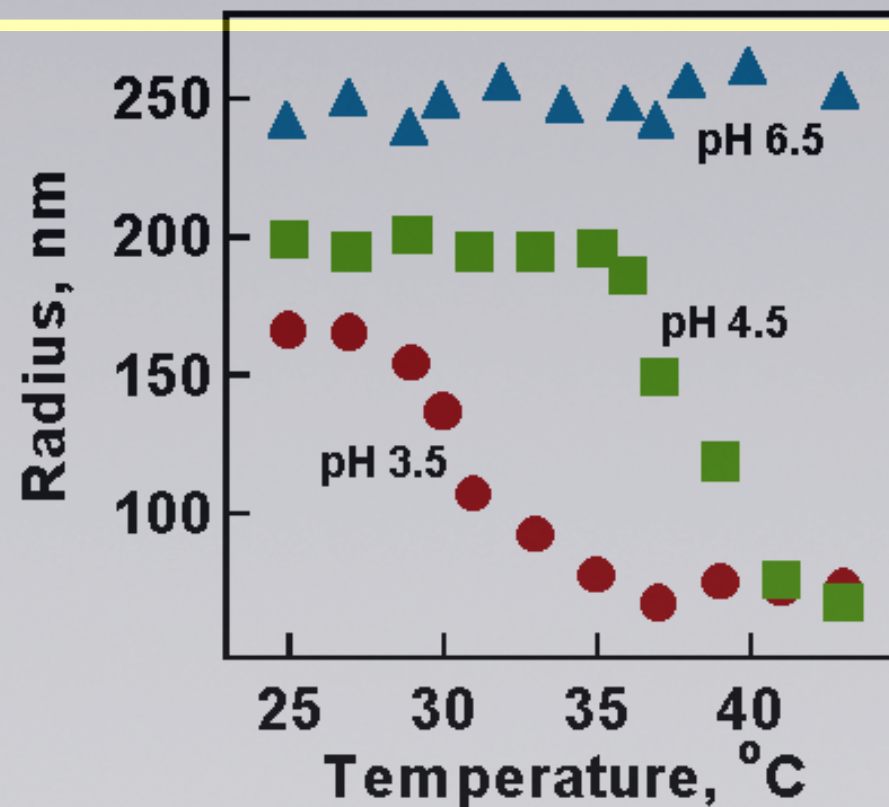
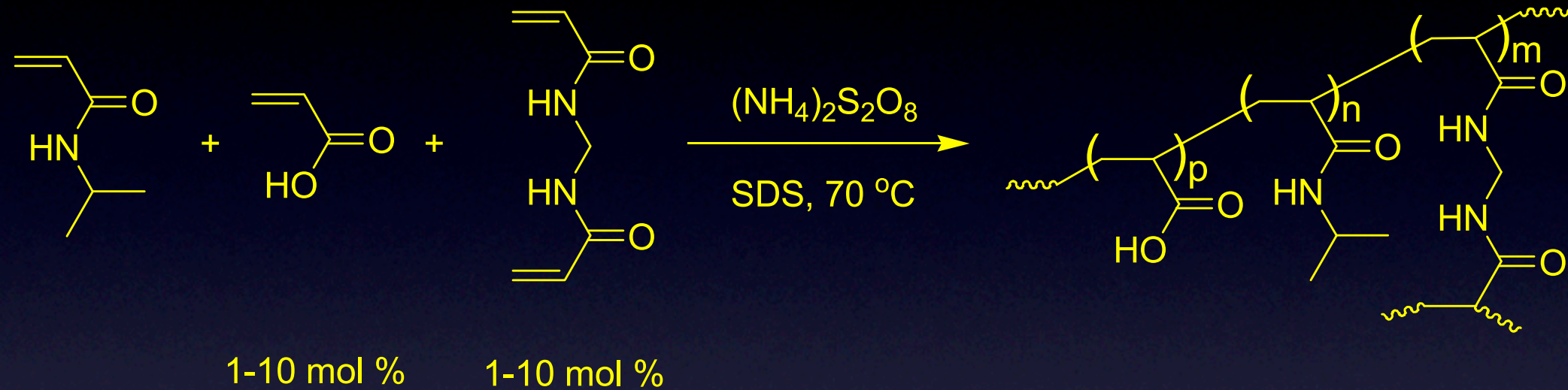


# Hydrogel Synthesis





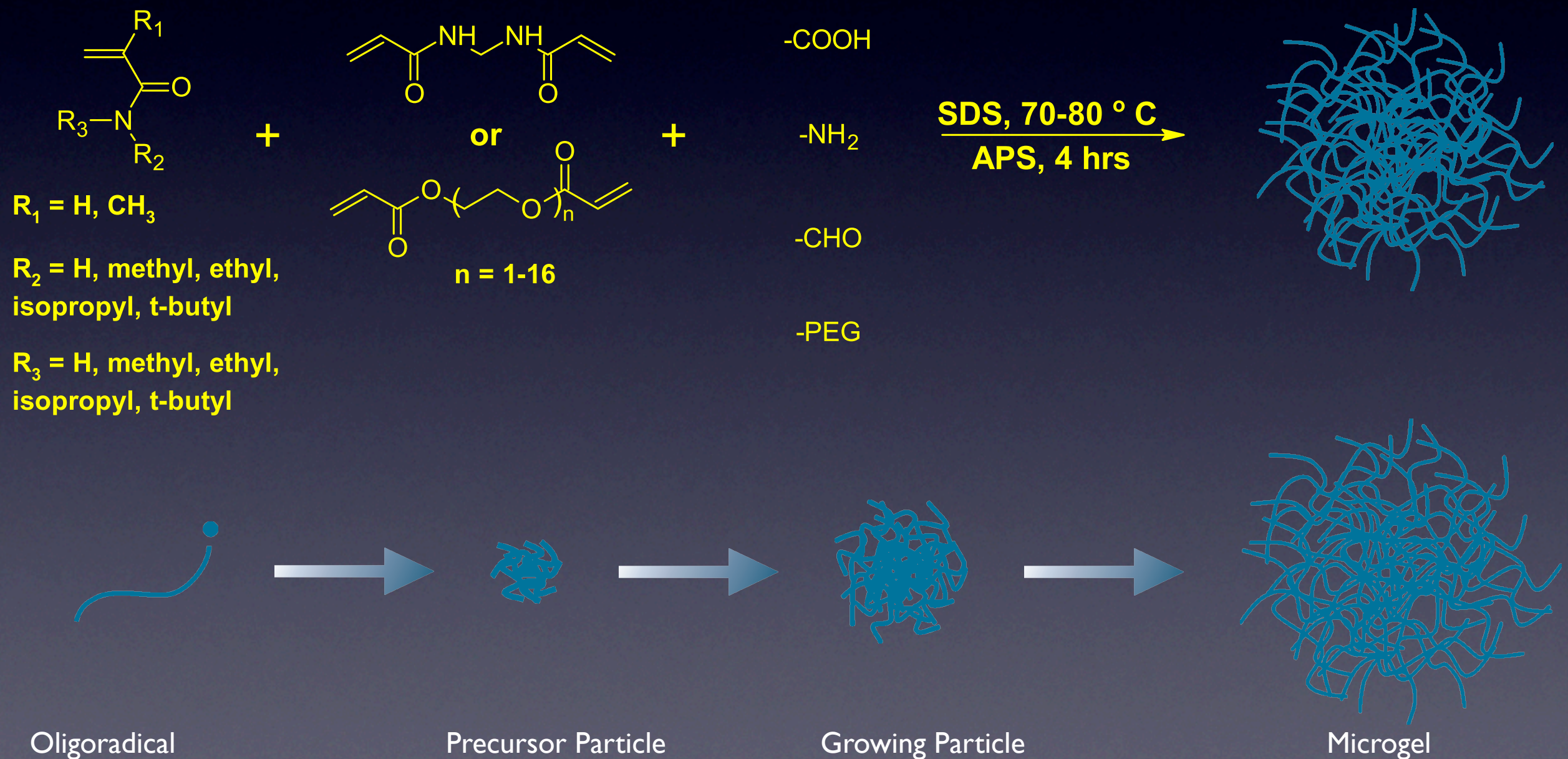
# “Multiresponsive” Hydrogels





# Hydrogel Nano/Microparticles

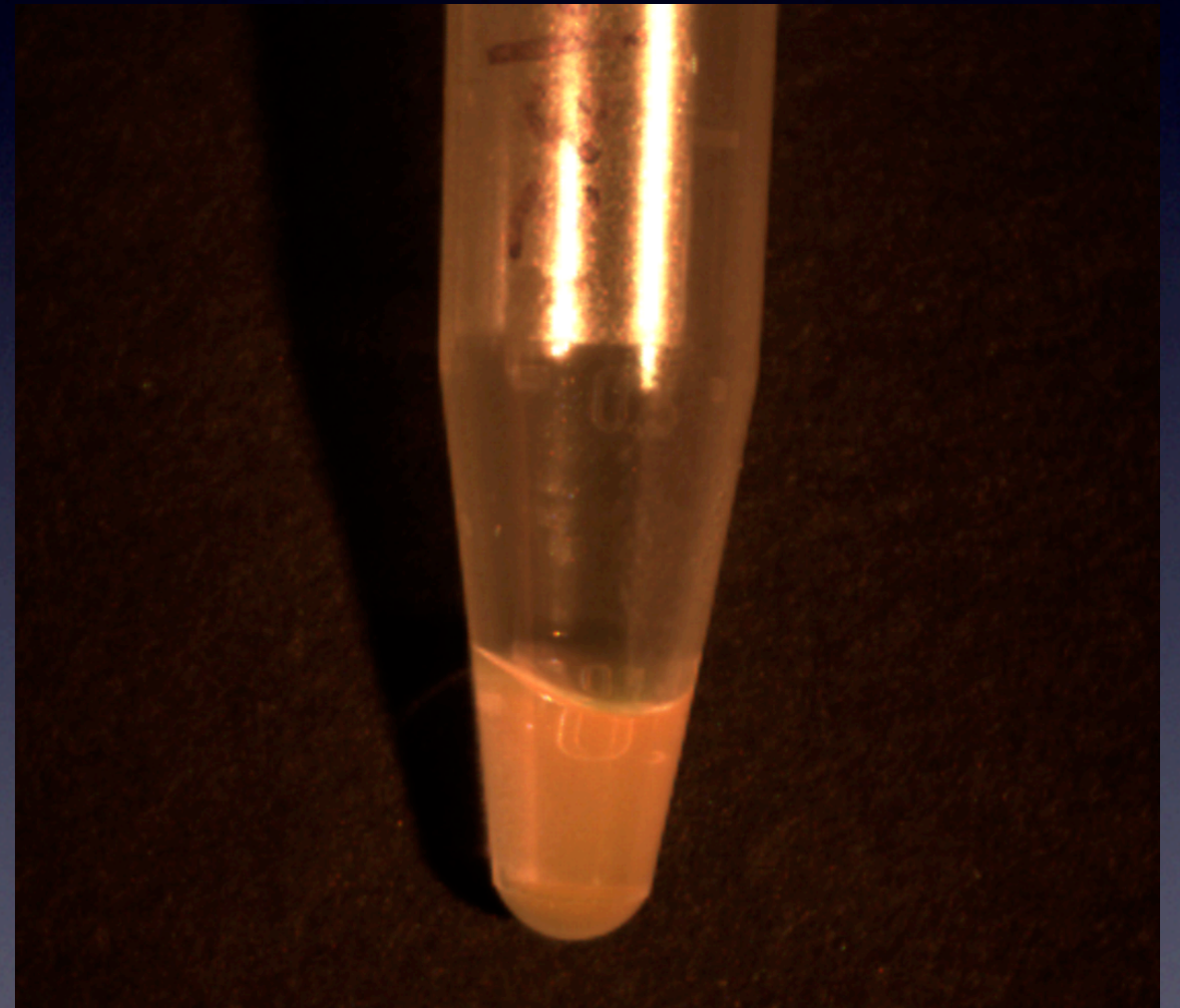
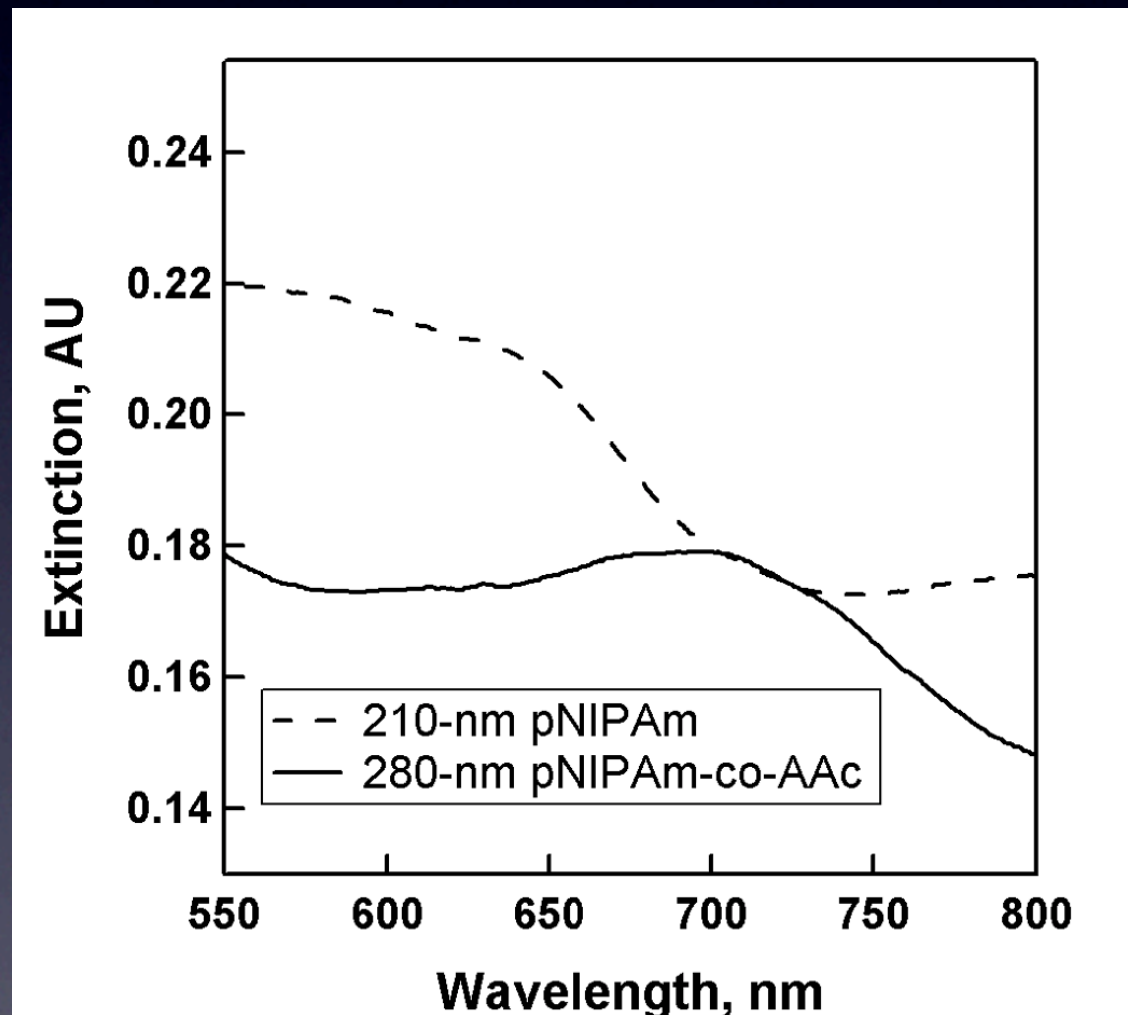
Thermoresponsivity as a route to well-defined colloidal materials.





# Microgel Assemblies

Centrifugal sedimentation ( $16,000 \times g$ ) of microgels yields an amorphous glassy phase.

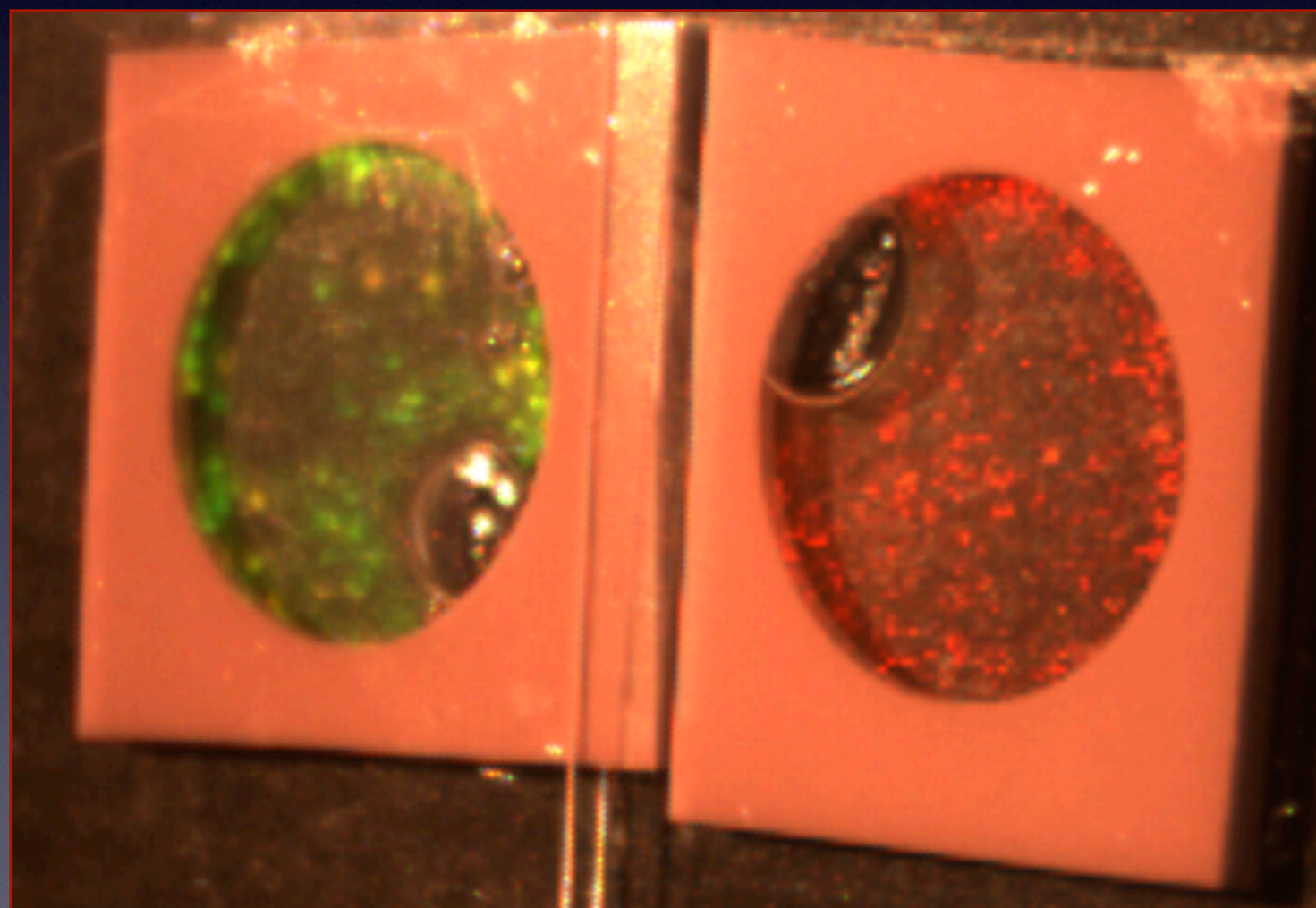
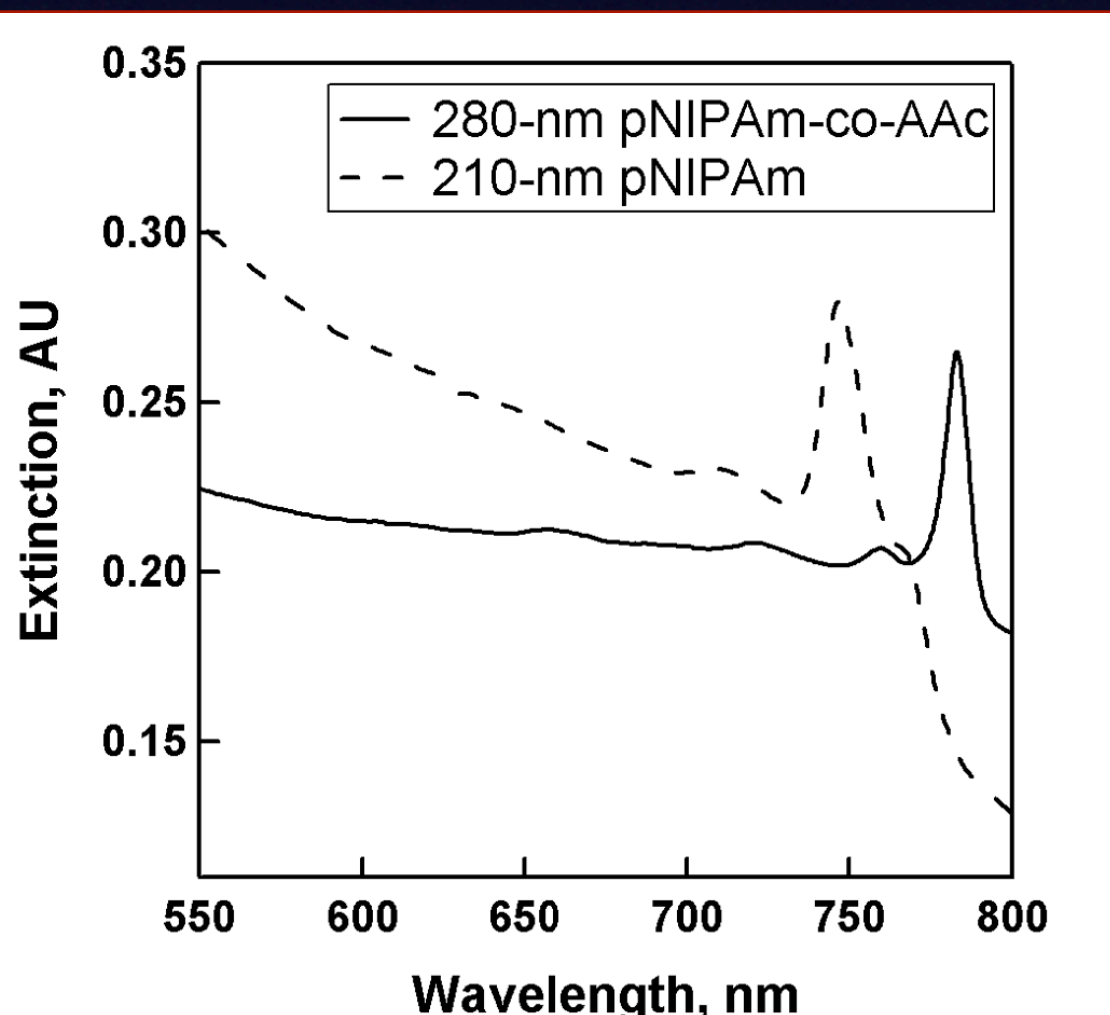




# Thermal Annealing

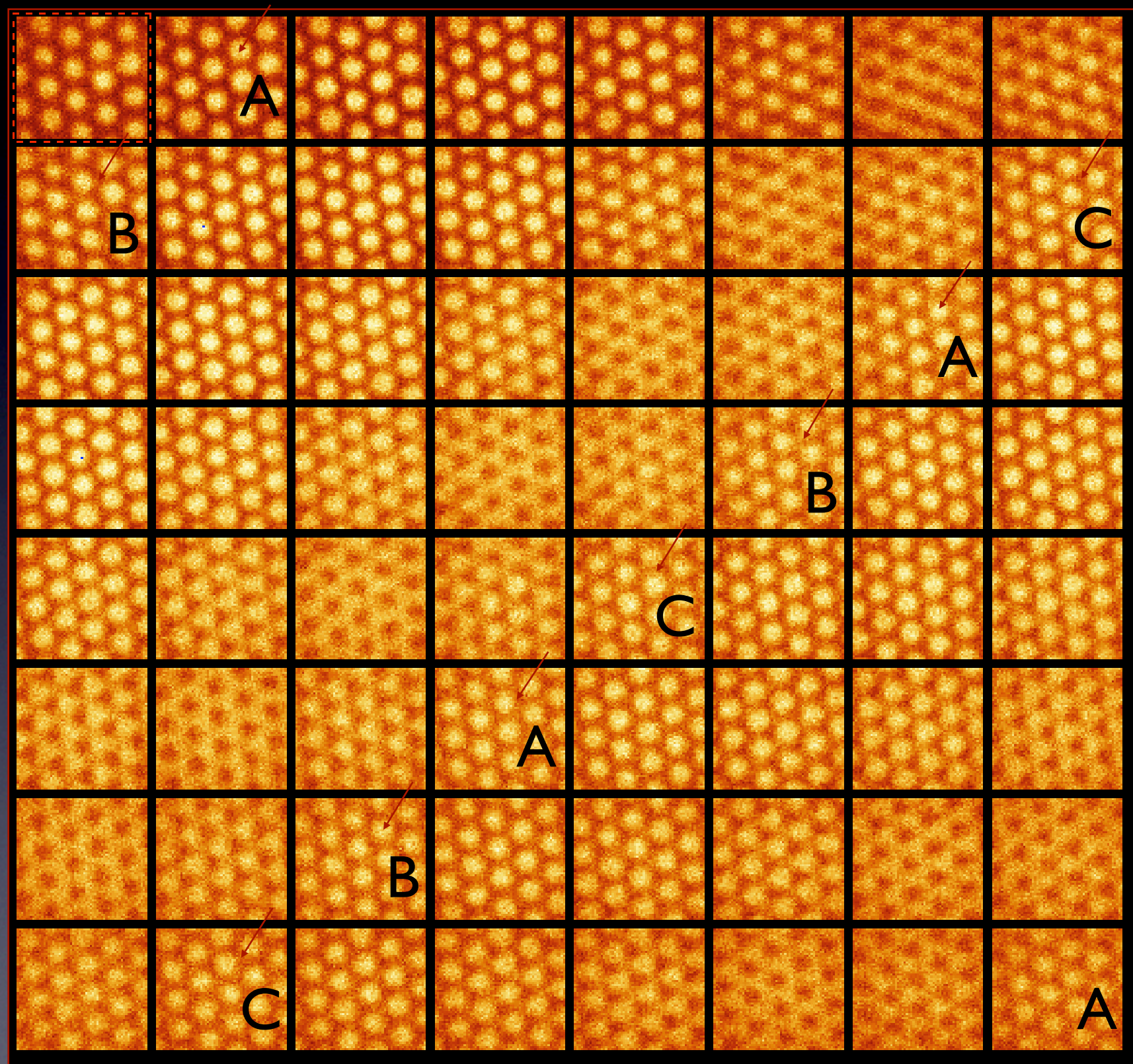
Thermal cycling across the *particle volume phase transition temperature* yields the thermodynamically preferred crystal.

Temperature tunes the volume fraction.





# 3-D Structure



Confocal Microscopy  
~810-nm diam.  
particles

Regular A-B-C-A  
packing - FCC crystal  
structure

Thermodynamics  
more controlled than  
in sedimented hard  
sphere crystals; High  
volume fractions  
accessible



# Colloidal Gel Phases

How does *particle softness* manifest itself...

- ▶...in the phase diagram?
- ▶...in the optical properties?
- ▶...in defect healing?
- ▶...in the assembly's responsivity?

What are the appropriate tools to study phenomena in soft assemblies?

How do we quantitatively measure these phenomena?



# Problem #1: Determine the Volume Fraction

It is non-trivial to calculate the volume fraction of a dispersion of spheres if there is uncertainty in the particle:

size

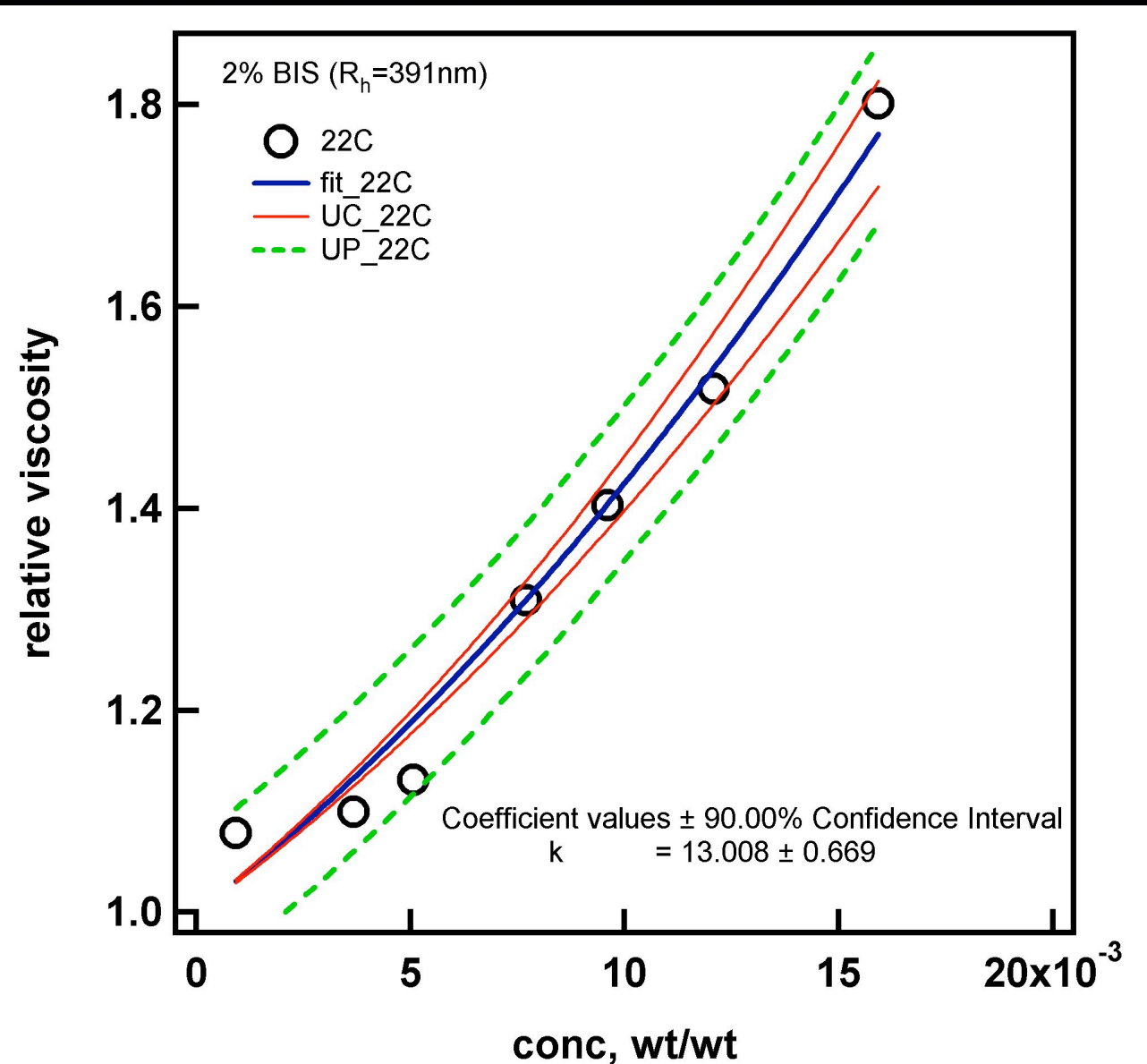
density

structure/topology

number density



# Solution: Relative Viscosities



At low concentrations, soft spheres behave “hard”. The Batchelor equation relates the viscosity to the hard sphere volume fraction.

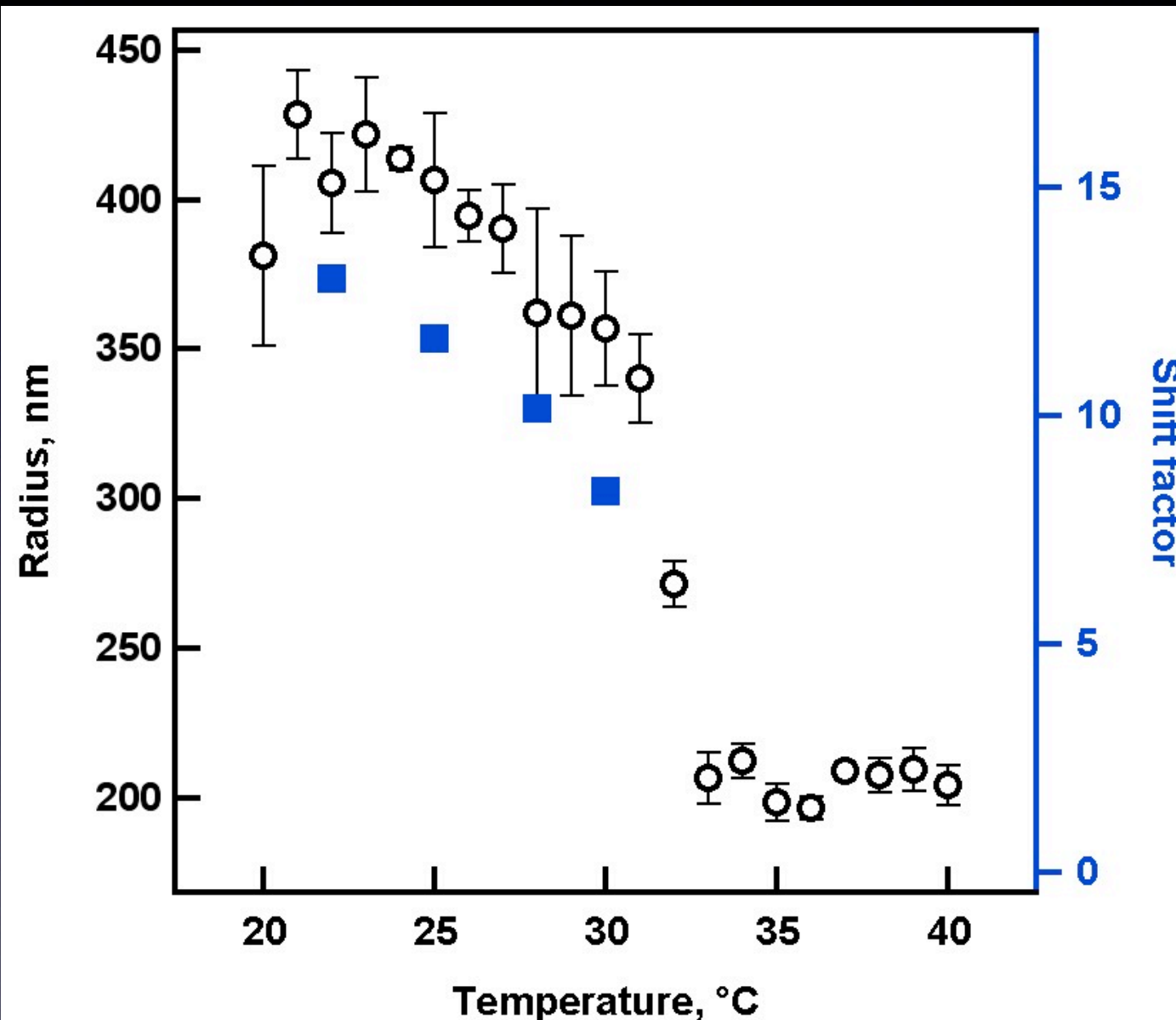
$$\phi_{eff} = kc$$

$$\eta = 2.5\phi_{eff} + 5.9\phi_{eff}^2 + \dots$$

H. Senff and W. Richtering, *J. Chem. Phys.* **1999** 111, 1705.  
Batchelor, *Journal of Fluid Mechanics* **1976** 74, Pt. 1, 1.

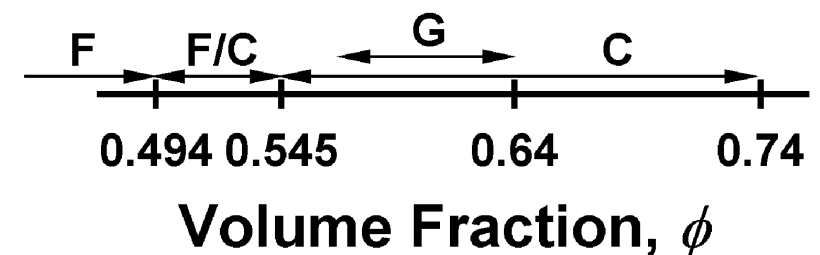


# Correlation with the VPT



Direct relationship  
between volume  
deswelling (DLS) and  
shift factor (viscosity).

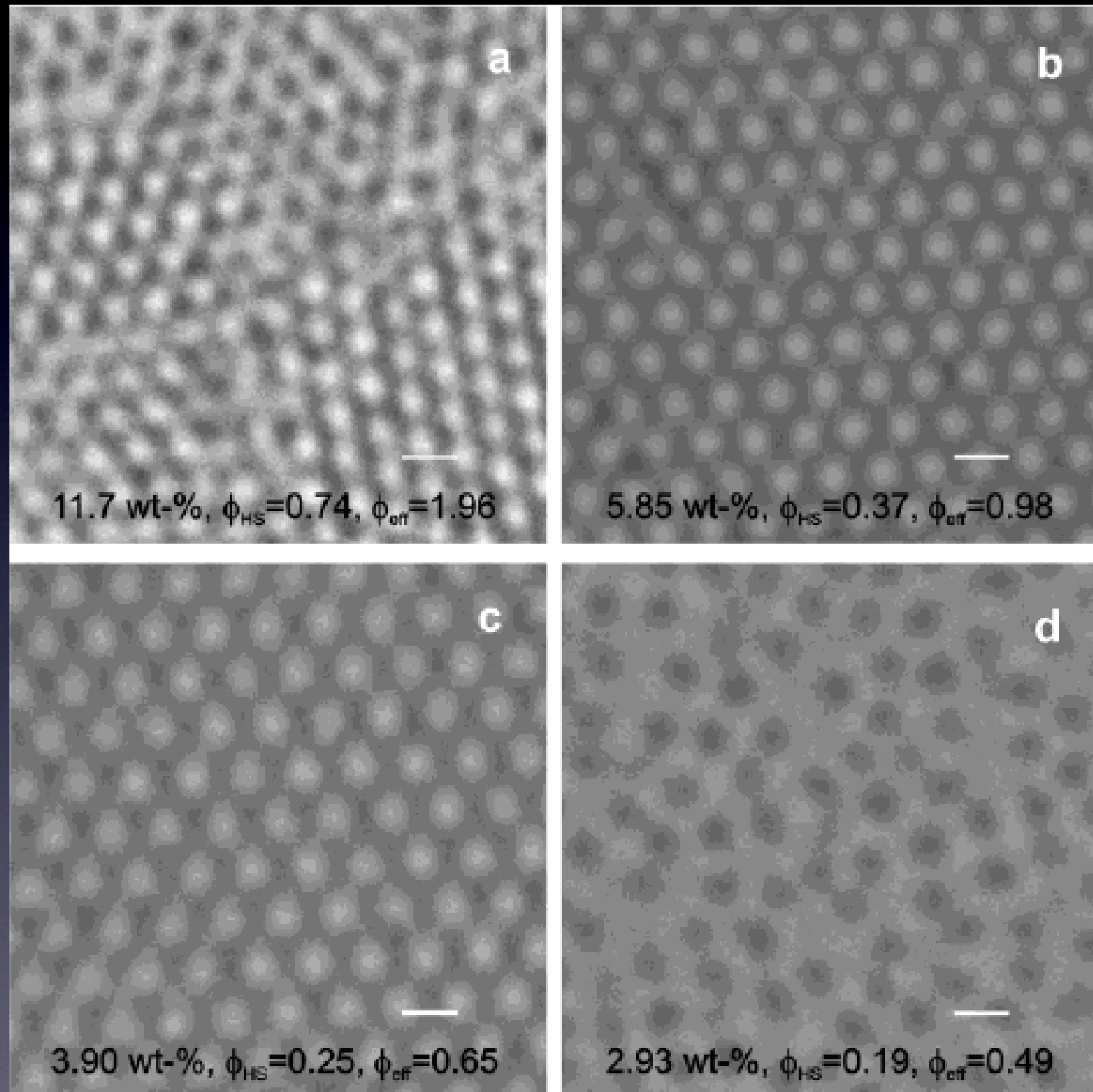
*Temperature tunes the  
volume fraction.*





# Soft Particle Overpacking

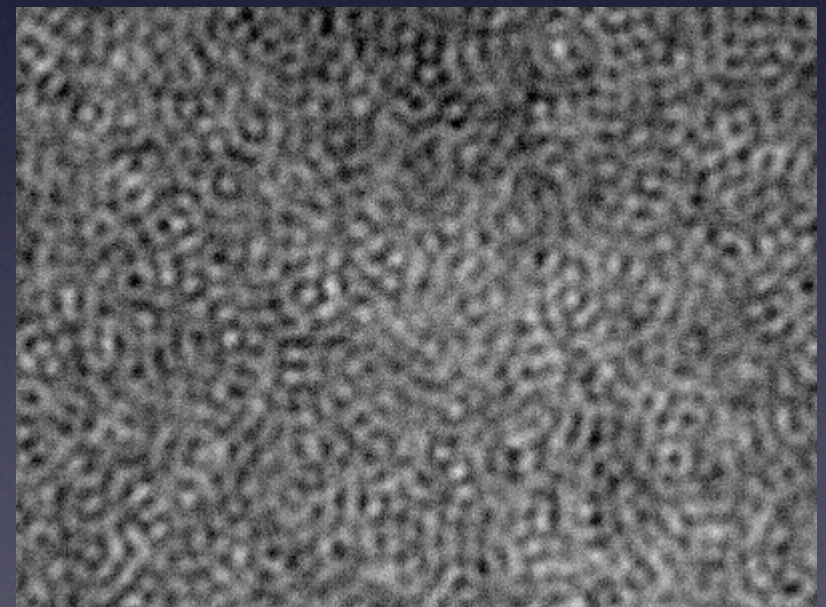
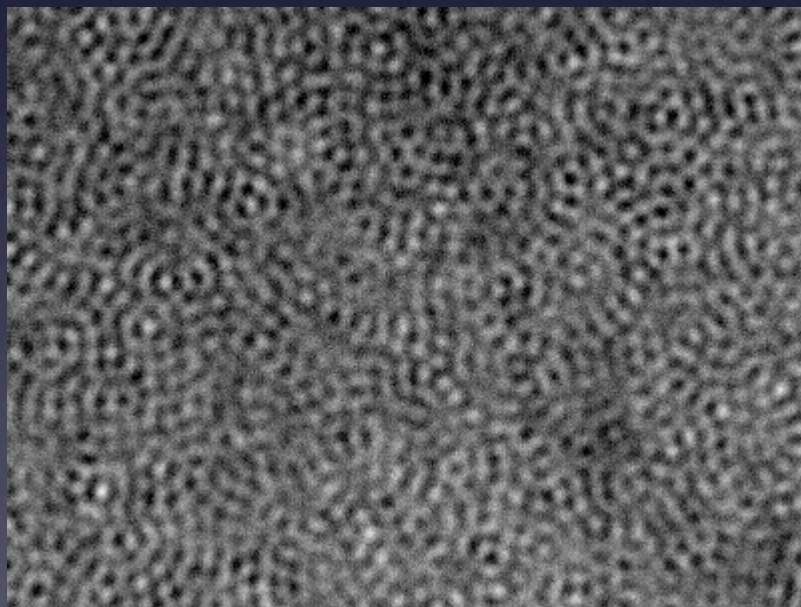
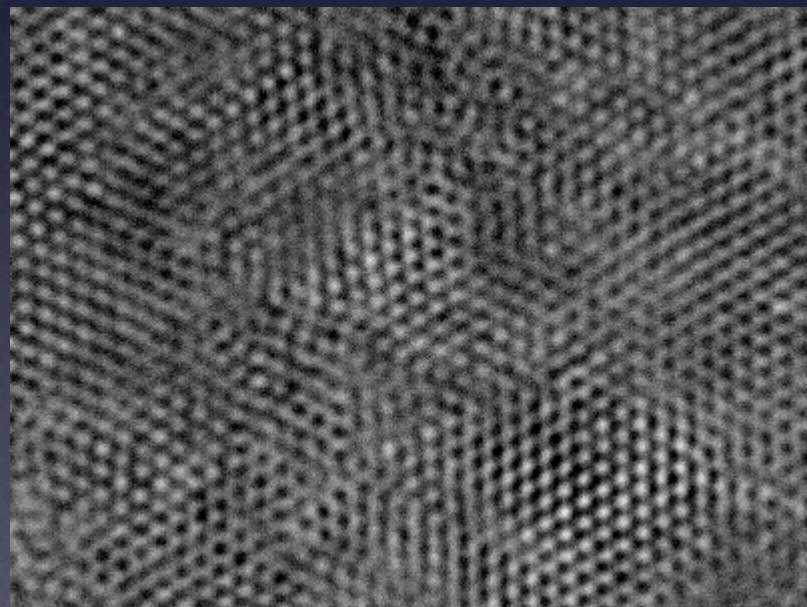
Soft particles can be packed into crystals in a deswollen, “overpacked” form via thermal annealing.





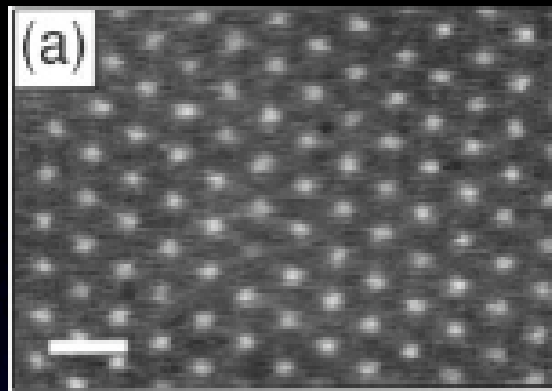
# Problem #2: Objective Determination of the Phase

Is there a method (besides visual inspection) that  
will permit quantitative analysis of the assembly  
motif?

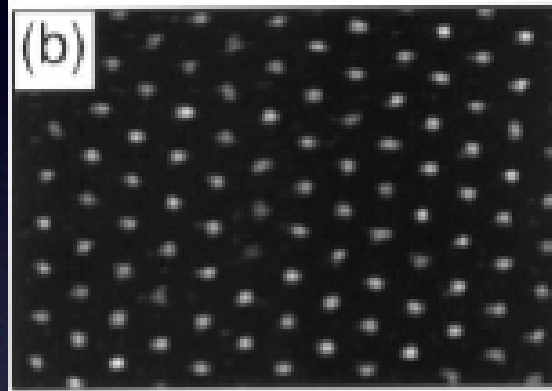




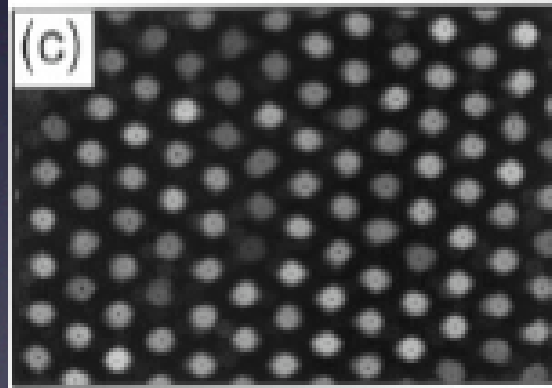
# Solution: Image Analysis



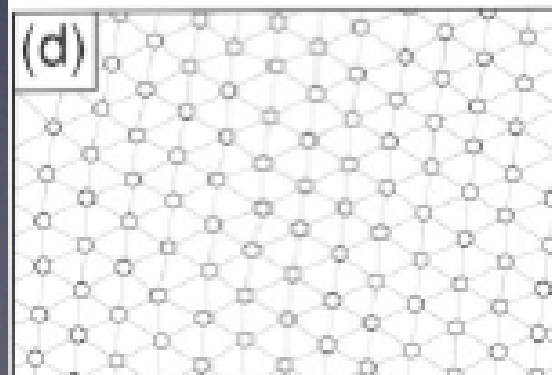
→ Original microscopic image



→ Filtered microscopic image  
after reducing the noise



→ Gray-scale dilation of  
the microscopic image



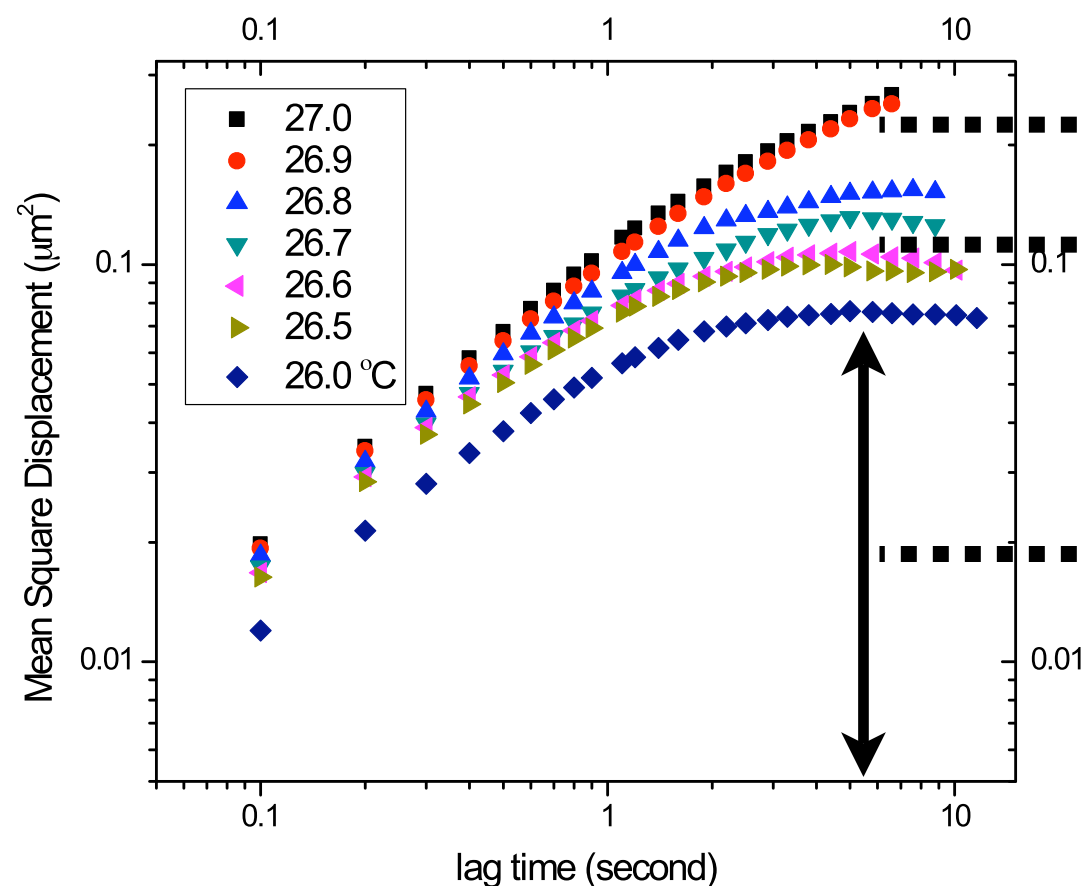
→ Particle location estimation



# Particle Tracking: Dynamics

By measuring all particle positions over time, one can calculate the Mean Square Displacement (MSD)

$$\text{MSD} = \langle |r_i(t) - r_i(0)|^2 \rangle \text{ or } \langle |\Delta r_i(t)|^2 \rangle$$



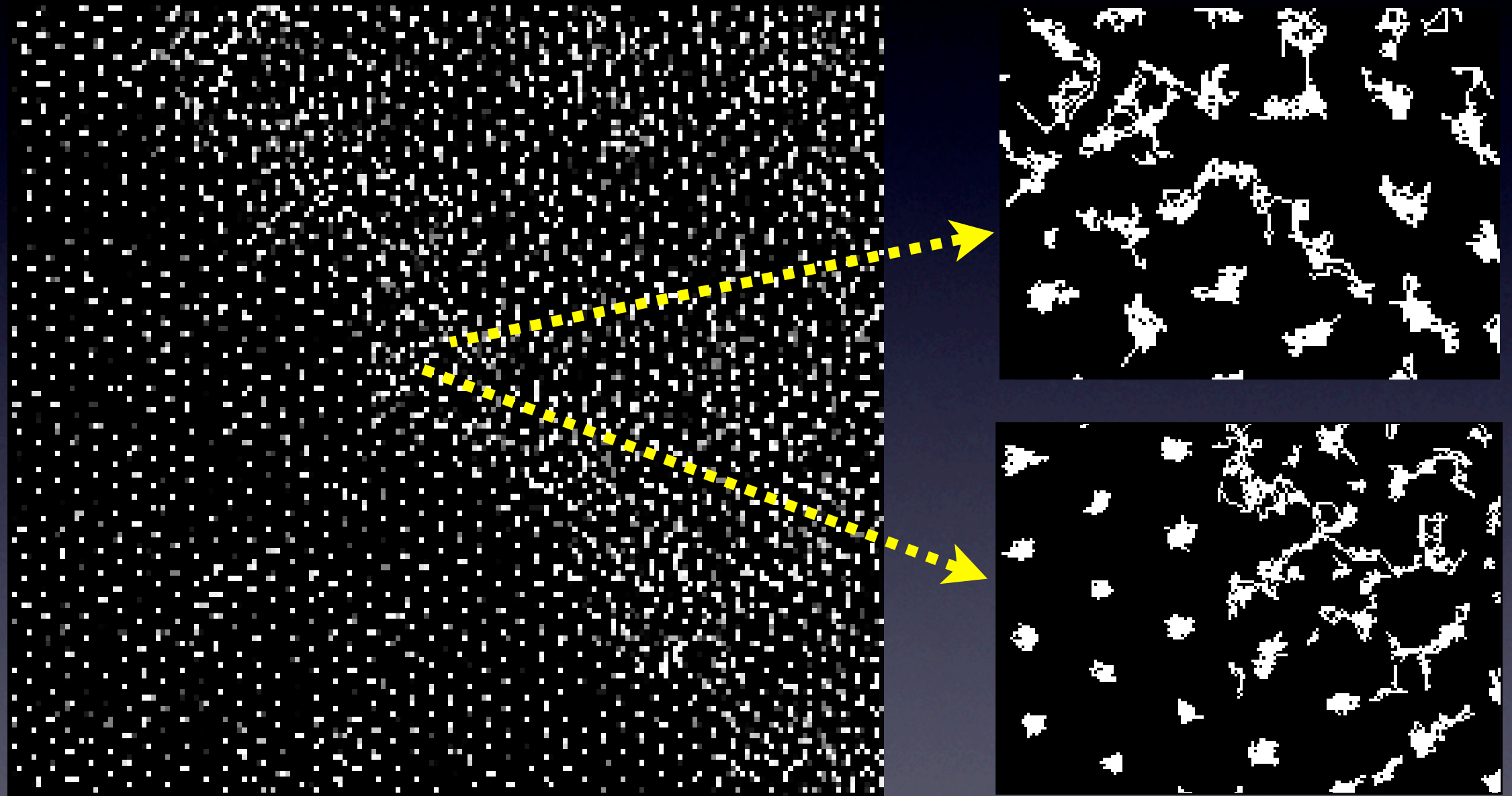
Diffusive:  $\text{MSD} \sim t$

Cage effect: subdiffusive

$$\text{MSD}_{\infty} \sim D_{\text{cage}}^2$$



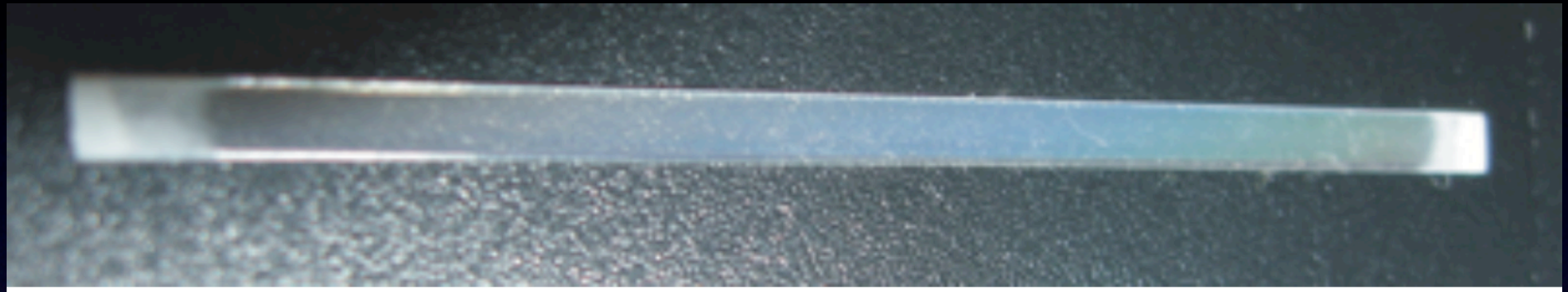
# Particle Tracking: Trajectories





# Visualizing Melting

Glass



Fluid

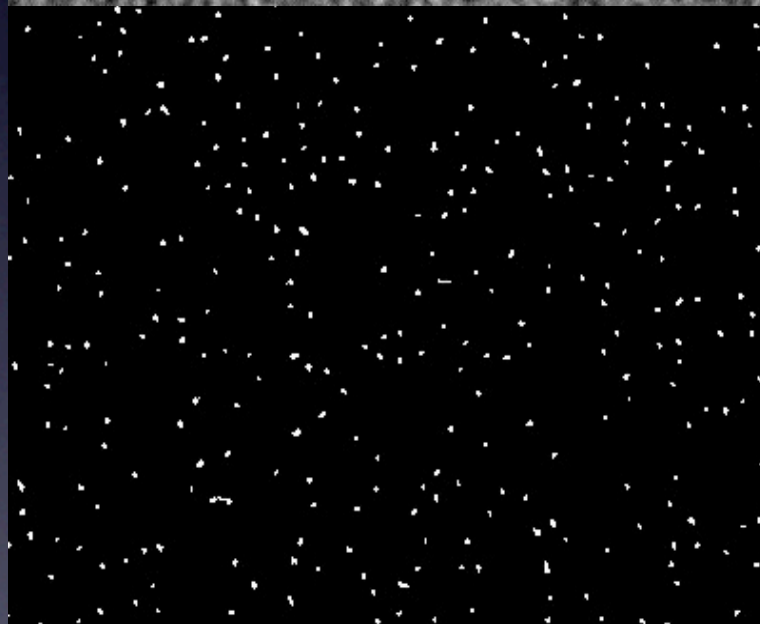
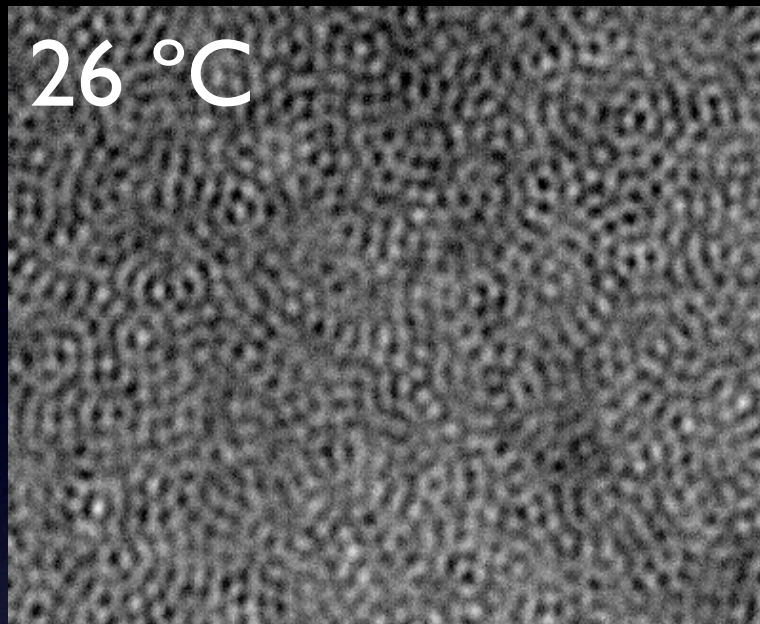


Crystal

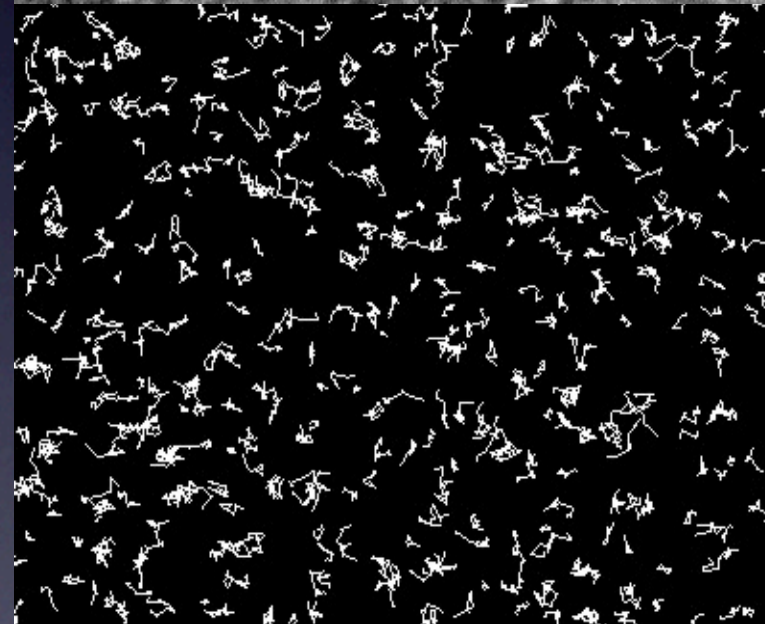
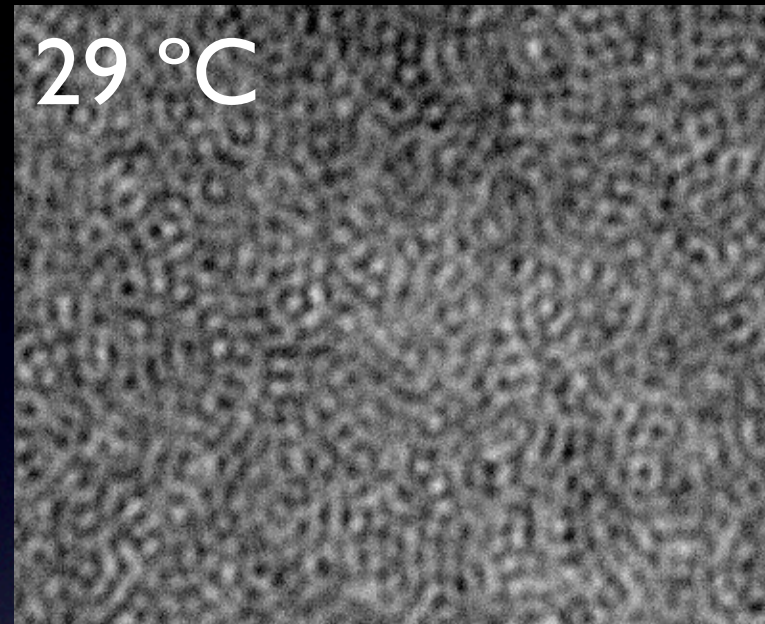




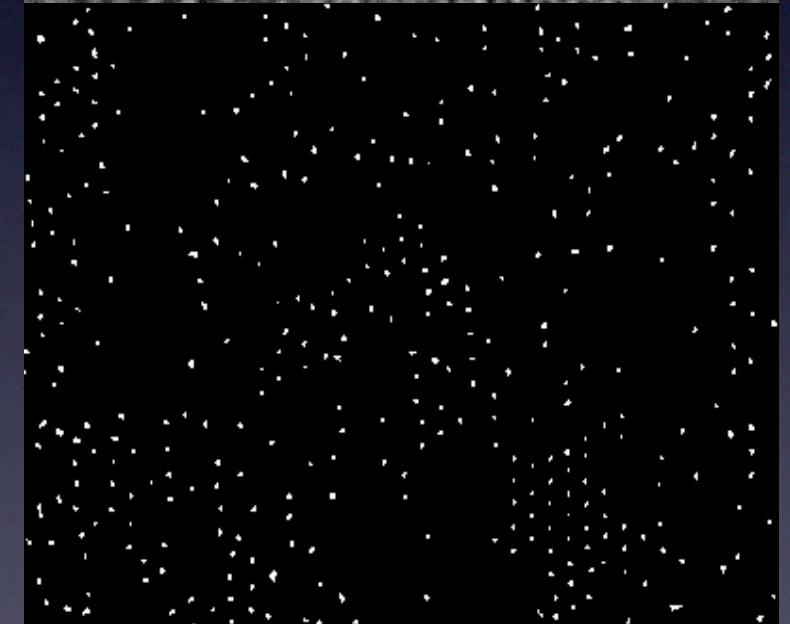
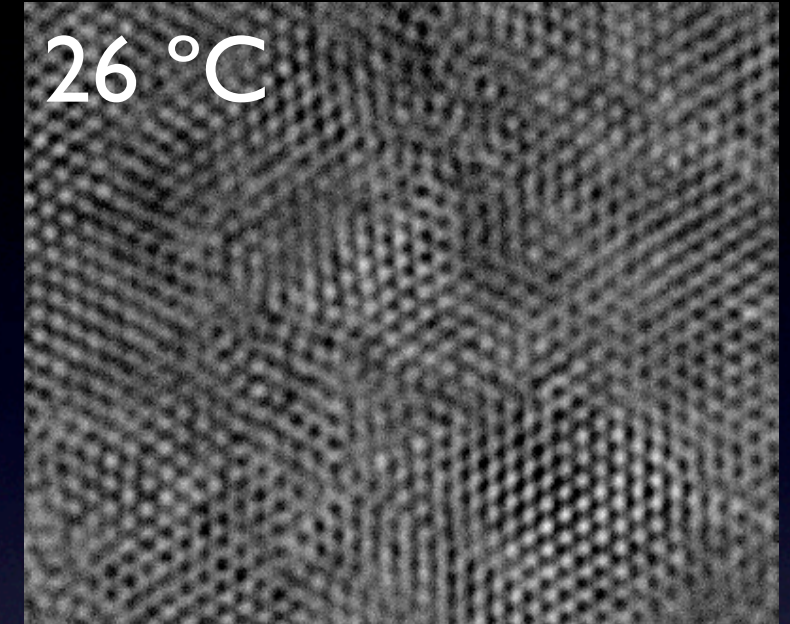
# Visualizing Melting



Glass



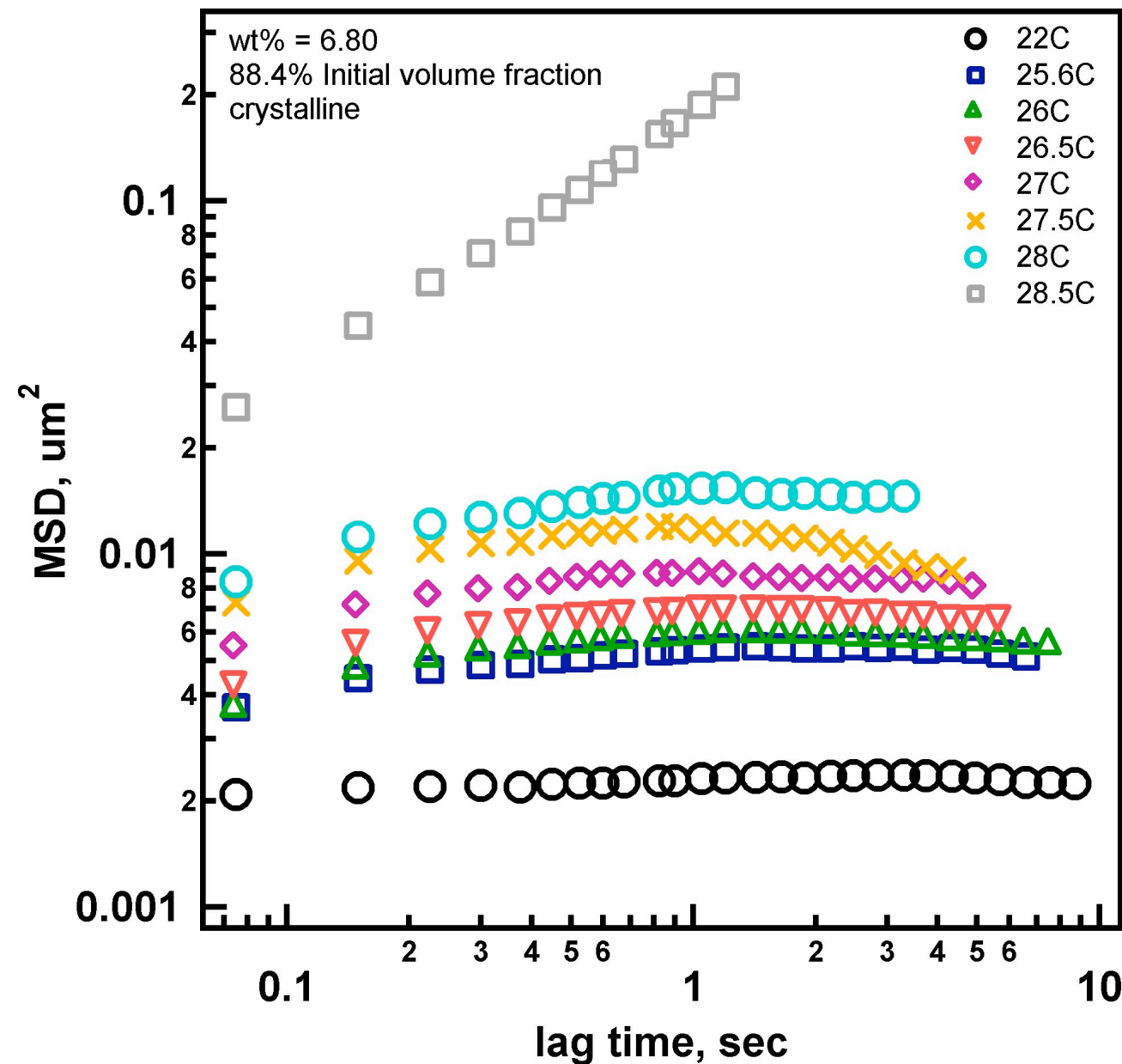
Fluid



Crystal



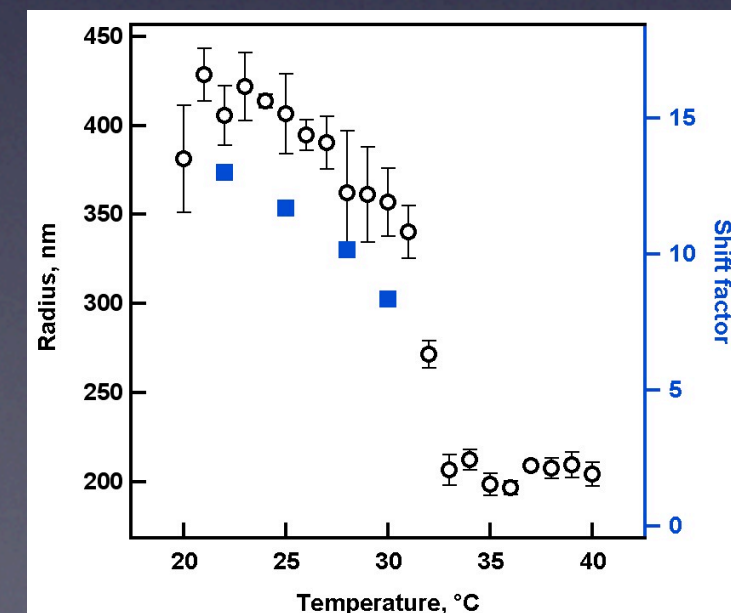
# Crystal Melting



~800-nm diameter  
pNIPAm spheres

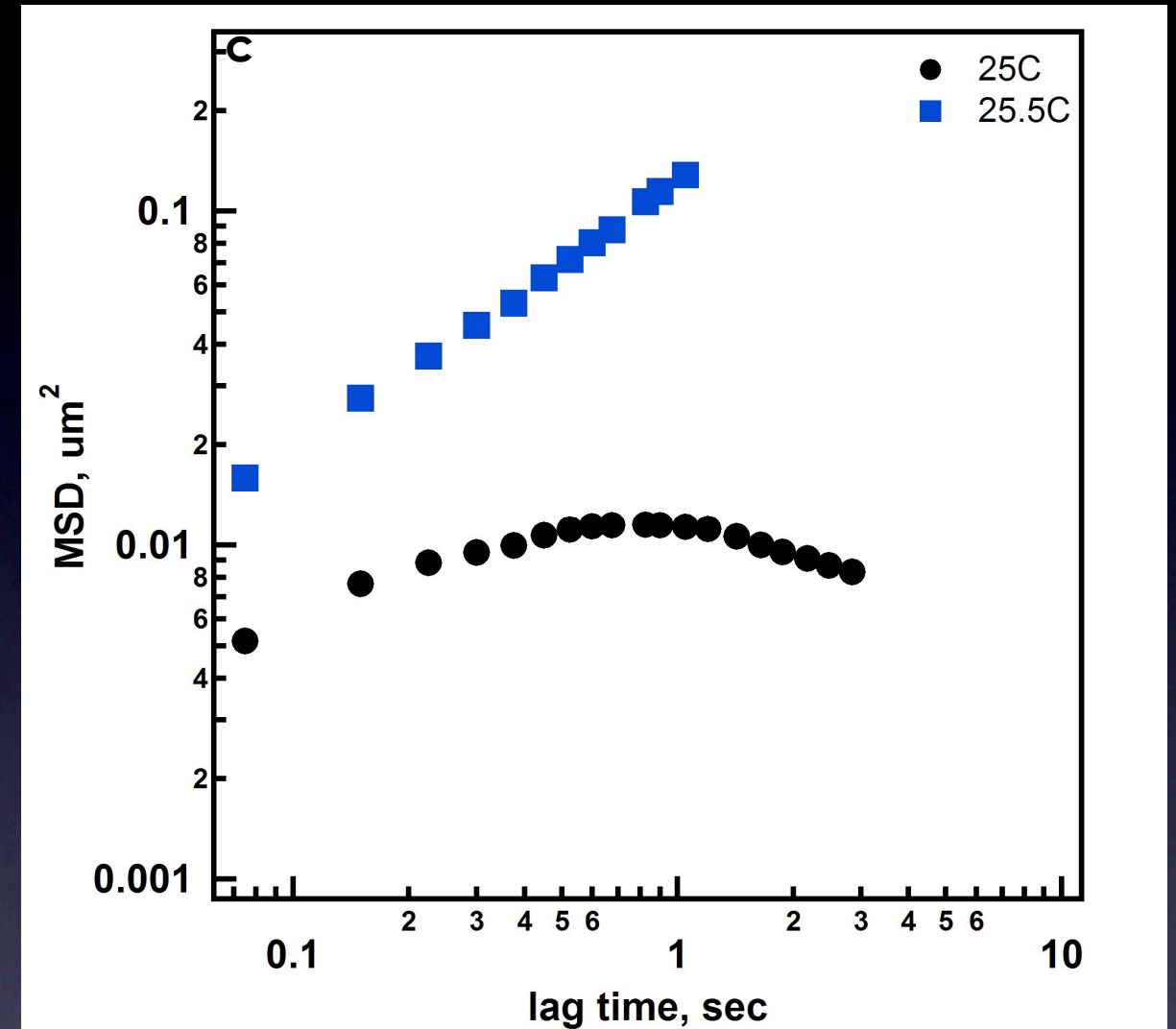
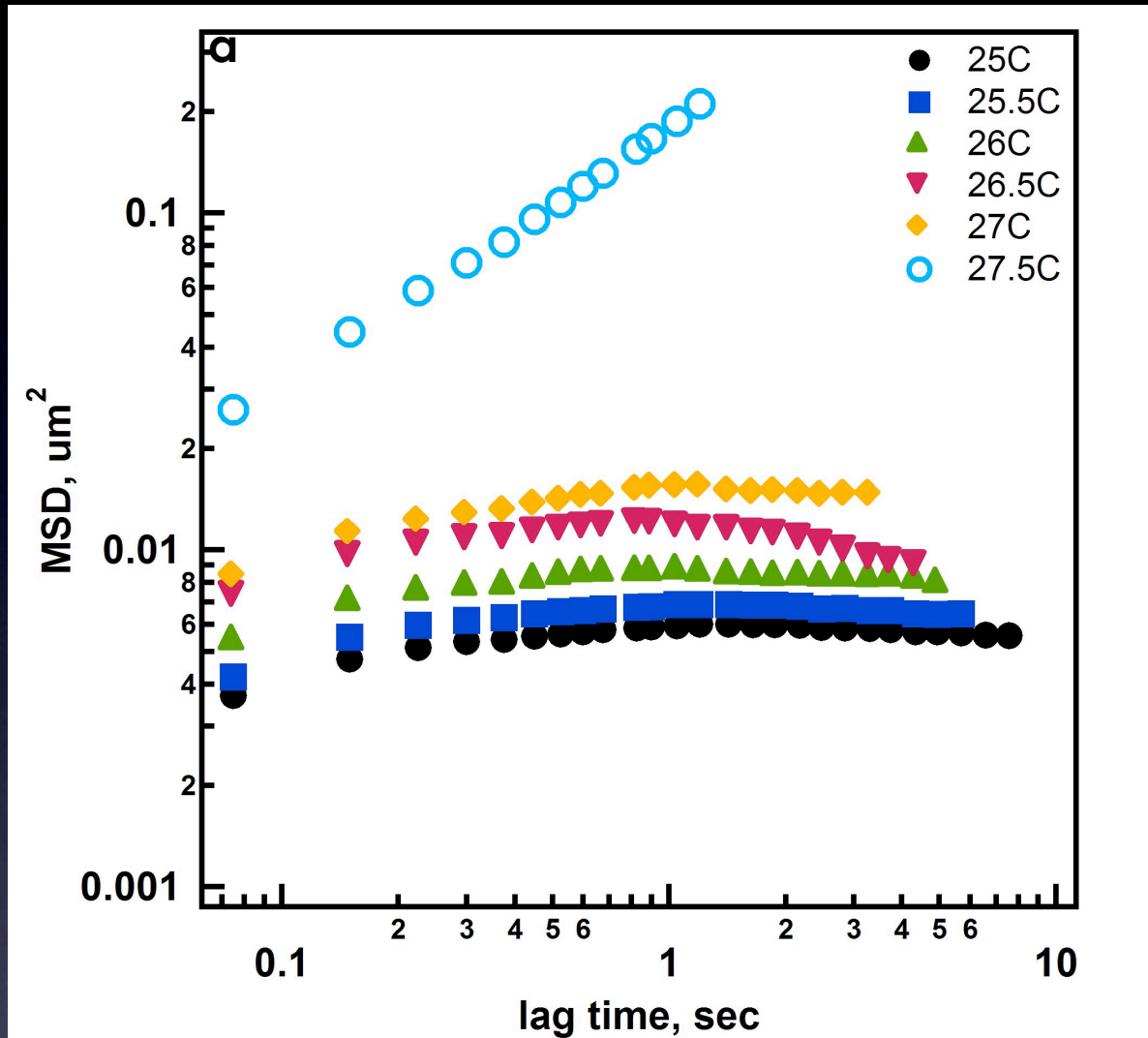
$$\phi = 88.4\%$$

2% cross-linked with *N,N'*-  
methylenebisacrylamide





# Effect of Initial Packing

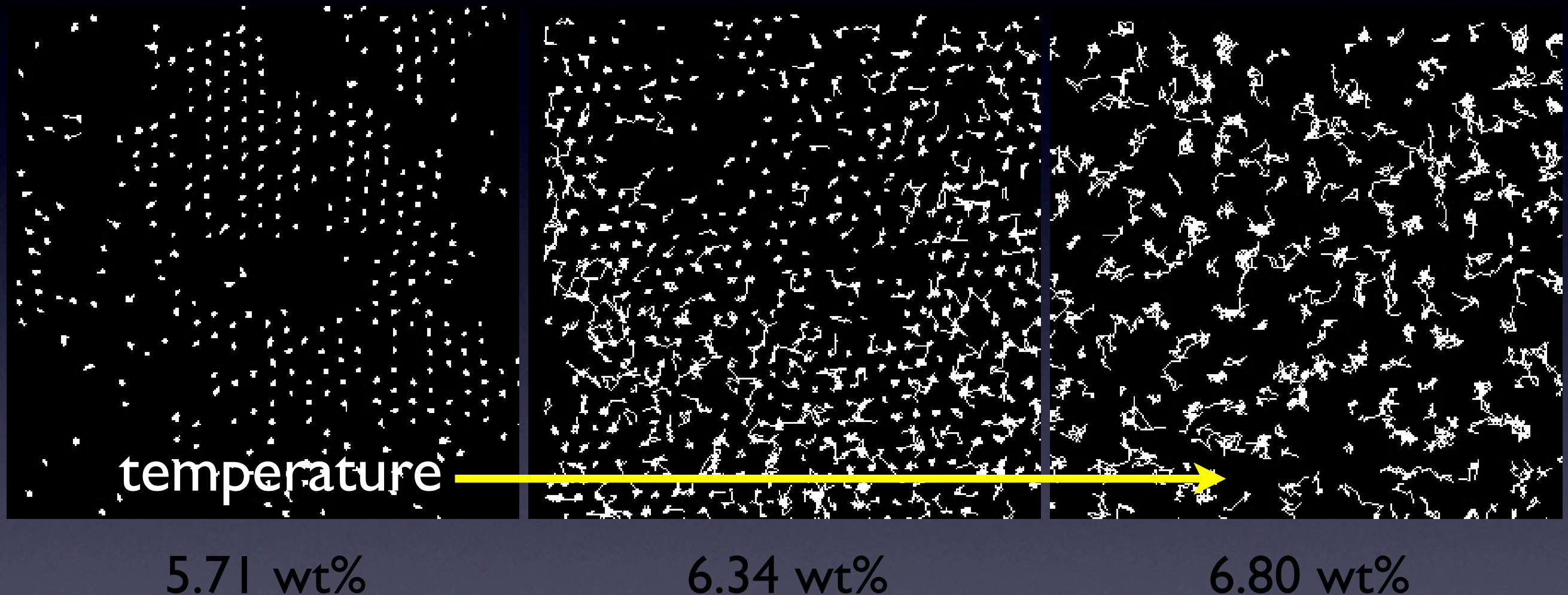


MSD of samples packed at Room Temperature.  
 $\phi_{\text{eff}} = 89.8\%$  (6.80wt%) (left) and 71.7% (5.44wt%) (right).



# Melting vs. $\phi_{\text{eff, initial}}$

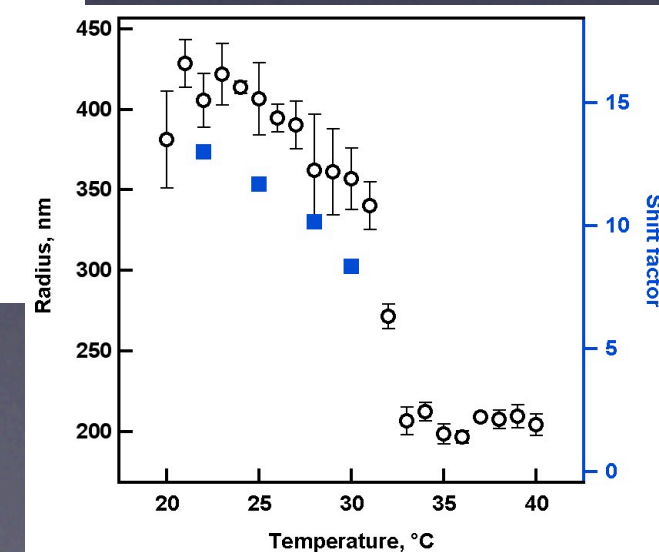
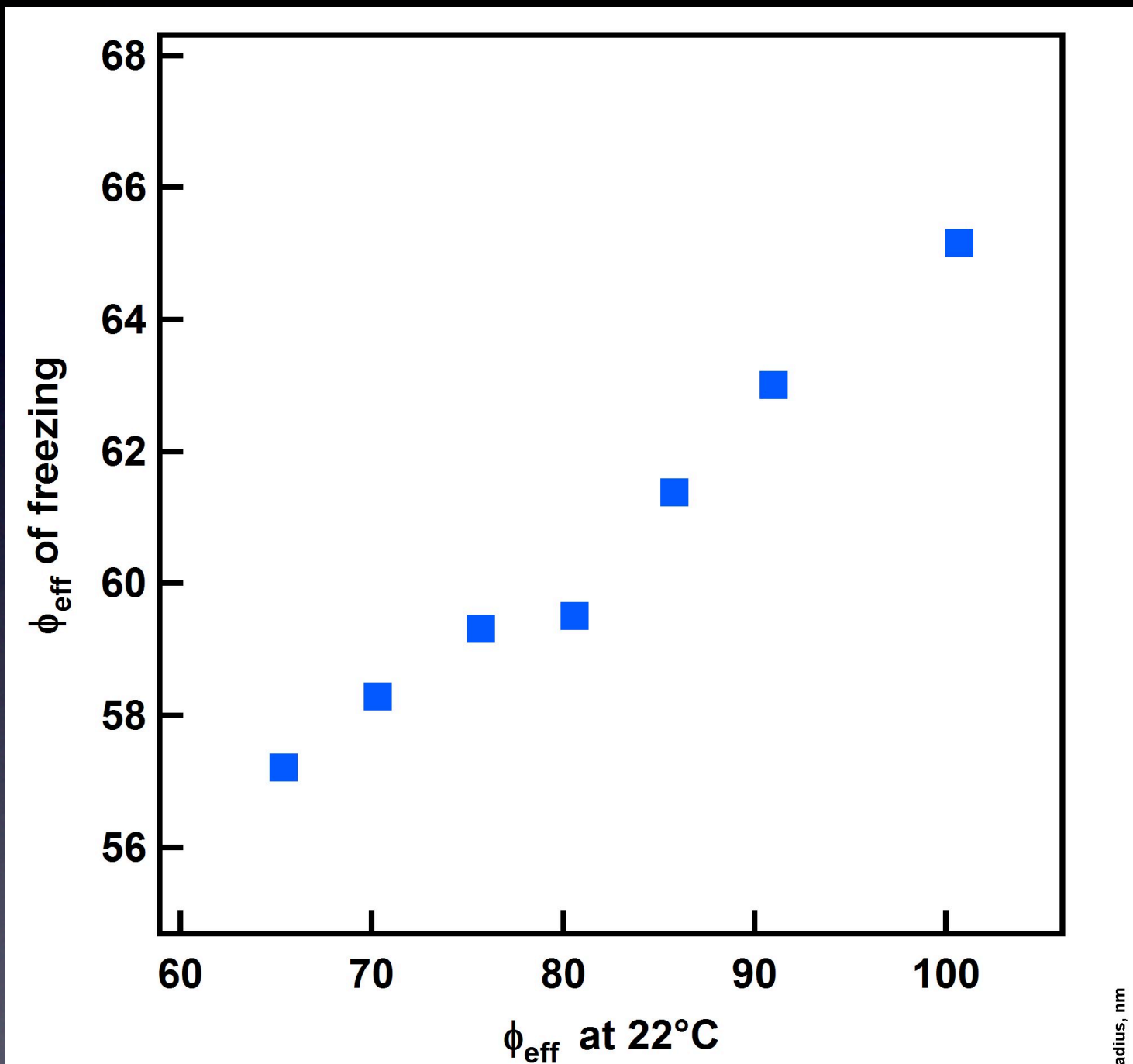
Three assemblies with a thermally regulated effective volume fraction of ~64-66%.



Denser assemblies melt easier?

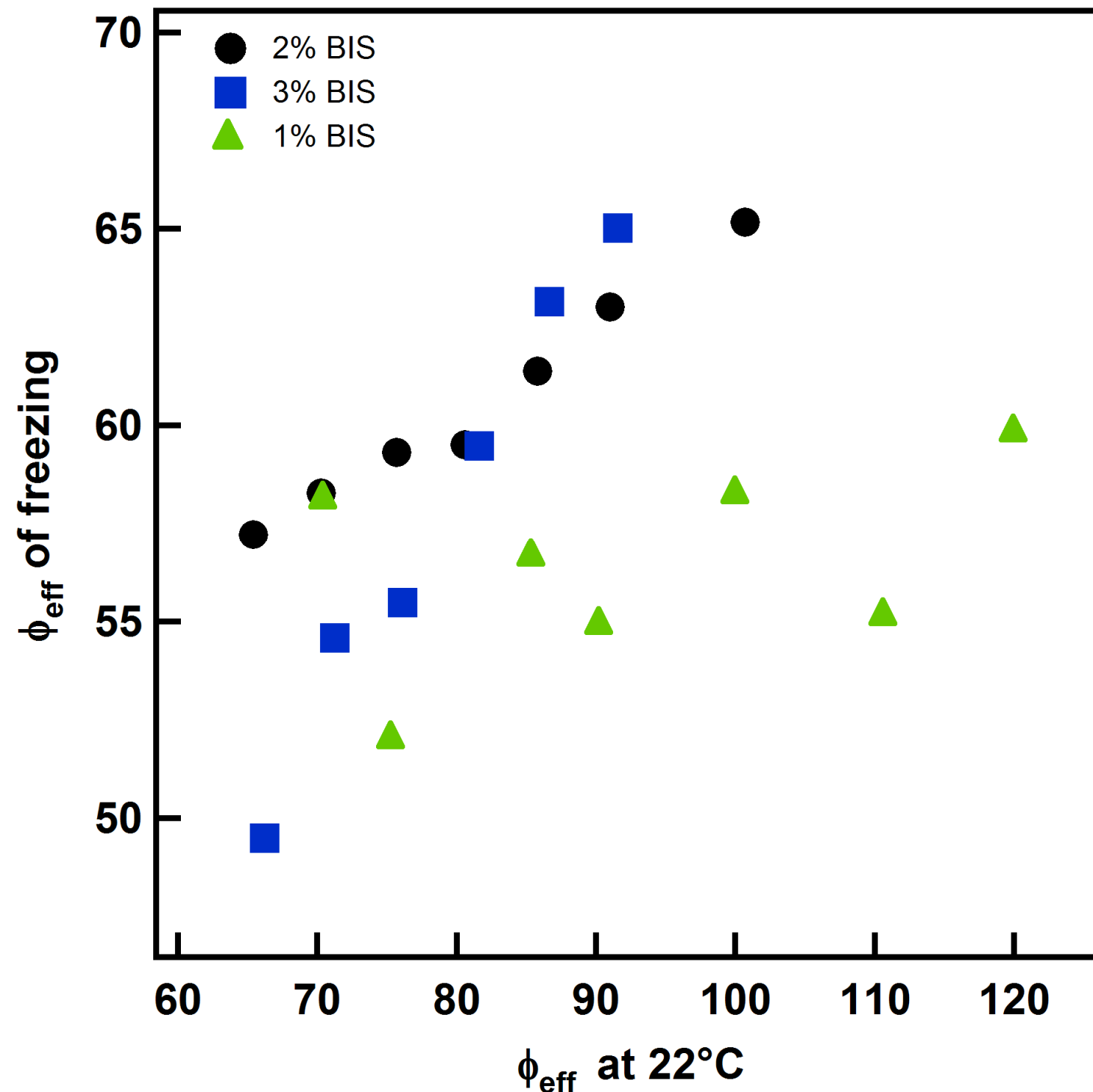


# Melting vs. $\phi_{\text{eff}}$ , initial





# Dependence on Softness

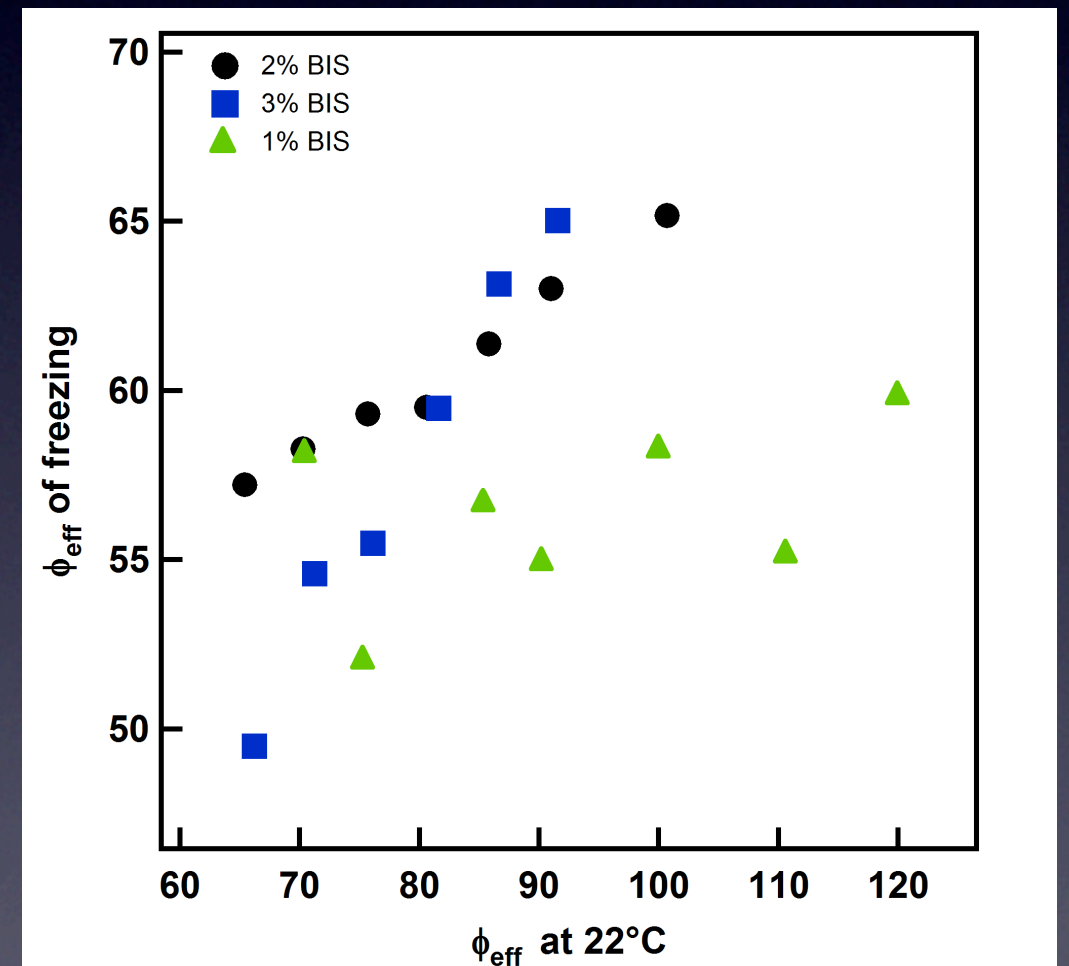
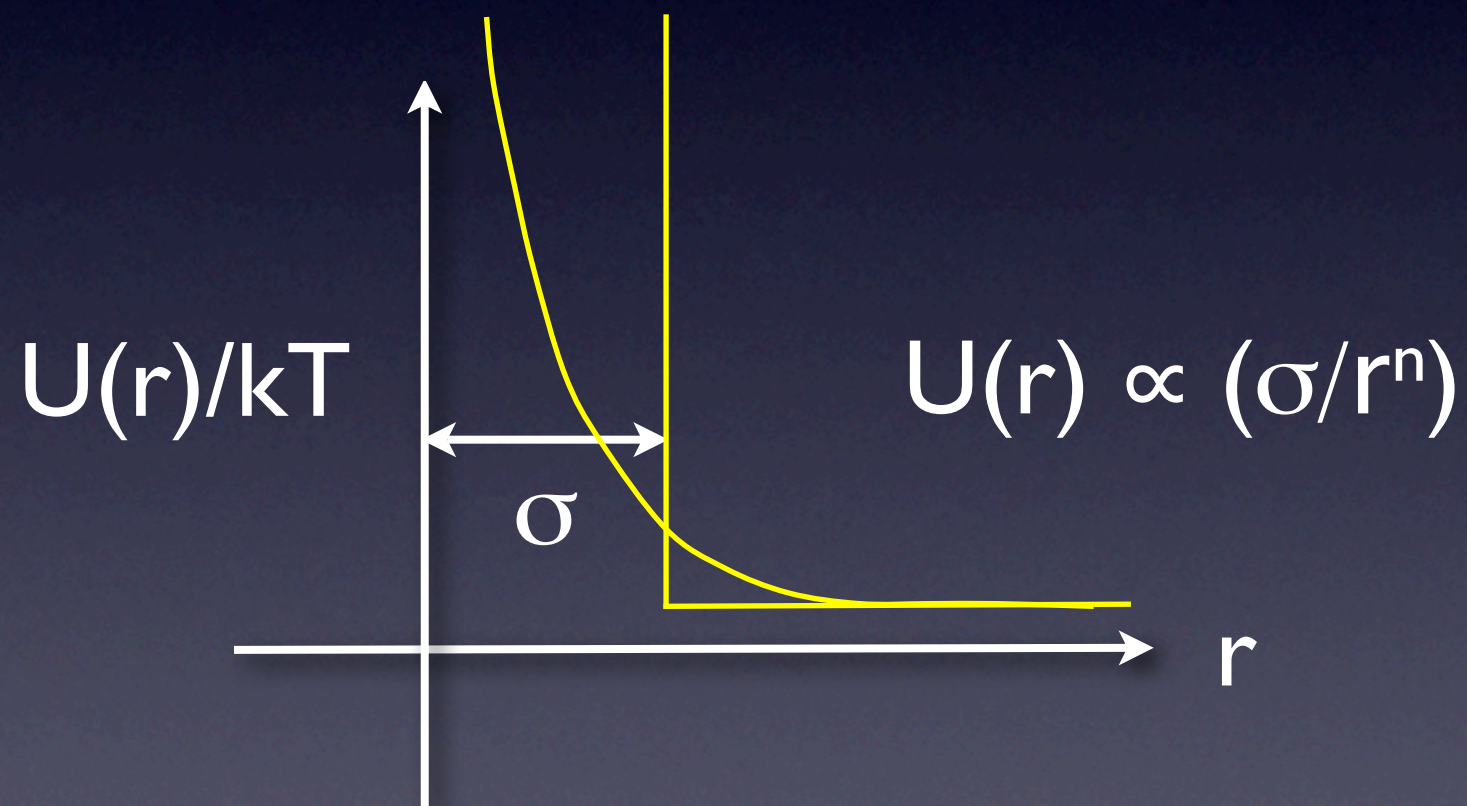


Softer particles  
show less packing  
dependence.



# Swelling and Softness

$$\frac{\pi}{k_B T} = \frac{\pi_{el} + \pi_M}{k_B T} = \frac{n_0}{N_x} \left[ \frac{1}{2} \left( \frac{n}{n_0} \right) - \left( \frac{n}{n_0} \right)^{\frac{1}{3}} \right] - \frac{1}{v} \left[ \ln(1 - nv) + nv + \chi n^2 v^2 \right]$$





# Summary: Microgel Packing

- Microgels represent a good model system for soft sphere packing.
- Particle tracking methods allow for objective determination of melting points/phase behavior.
- *The effective melting point provides insight into the local curvature/slope of the pair potential.*



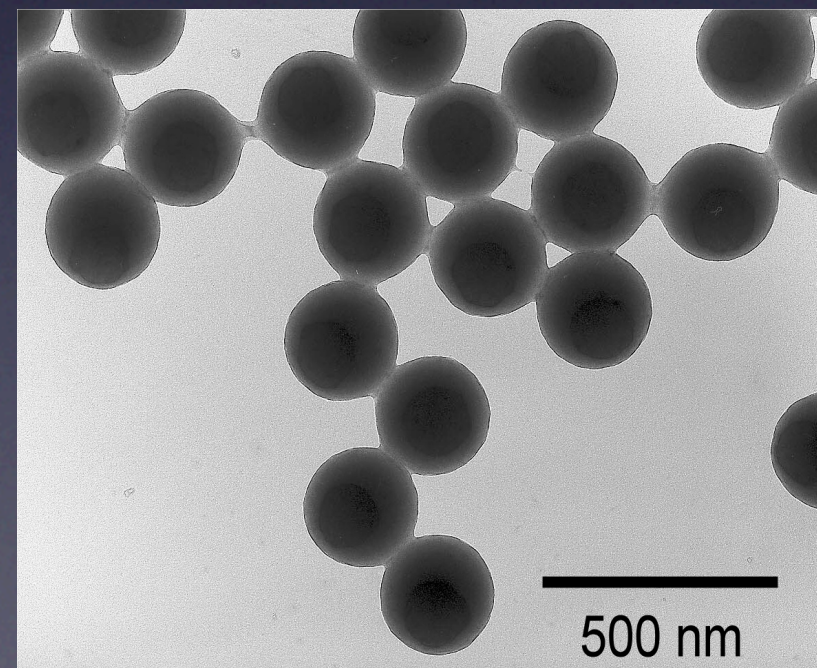
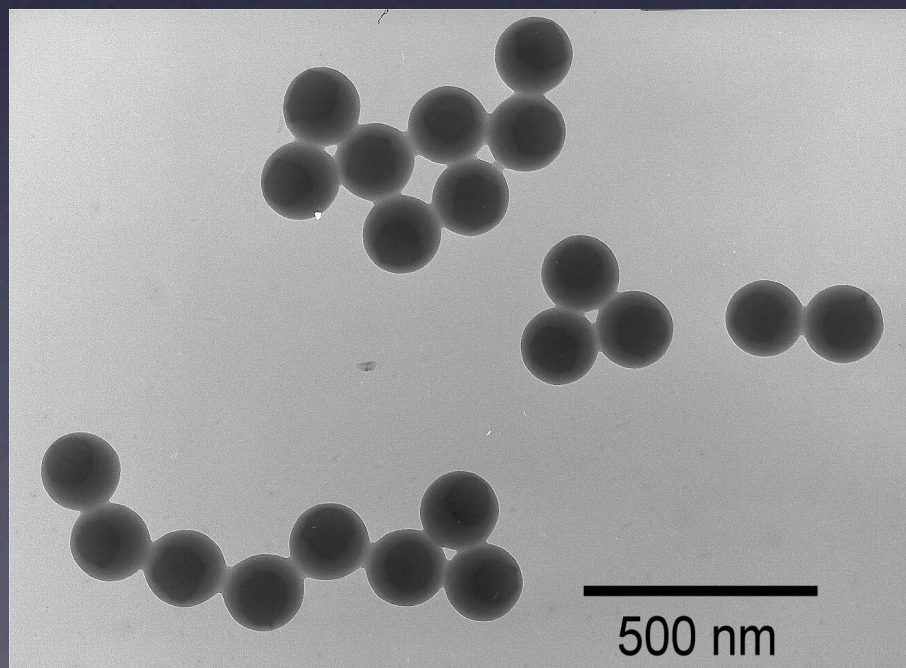
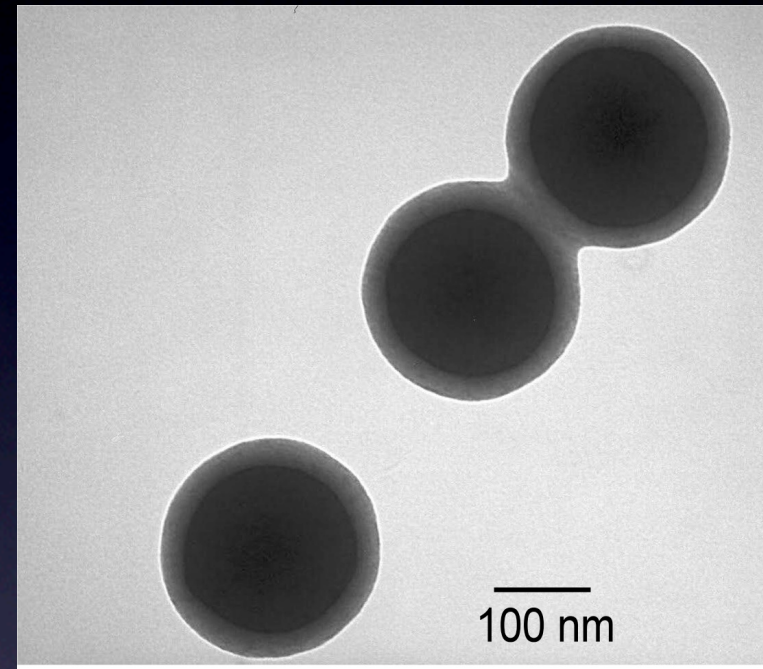
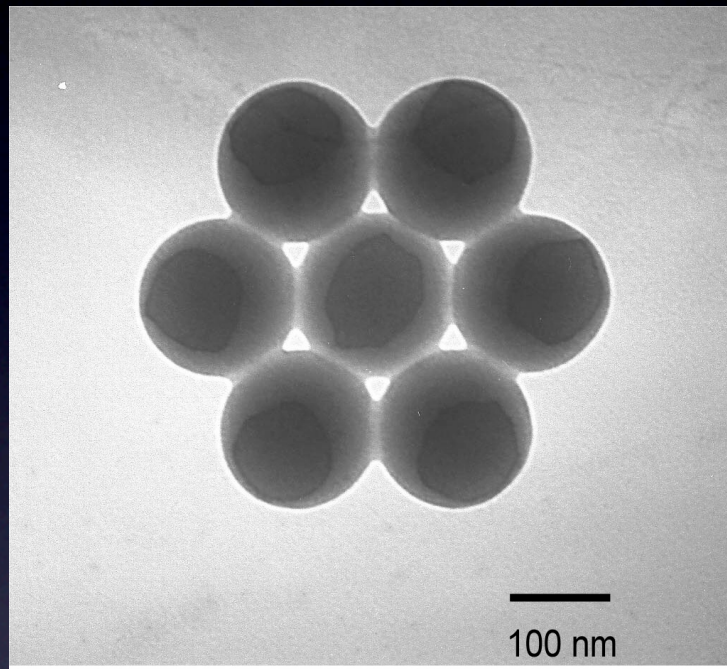
# Soft Interactions: Utility

## Paint-On Photonics



# Core/Shell Latex

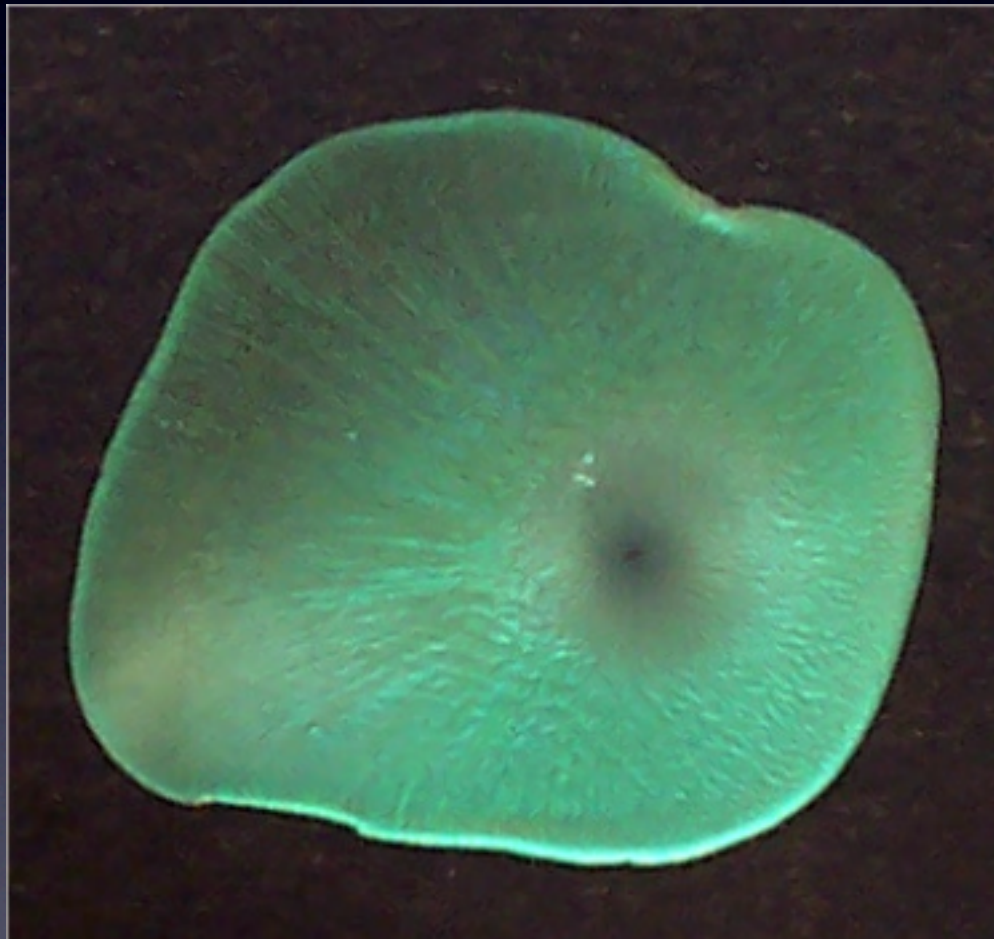
poly(styrene) core + pNIPAm shell



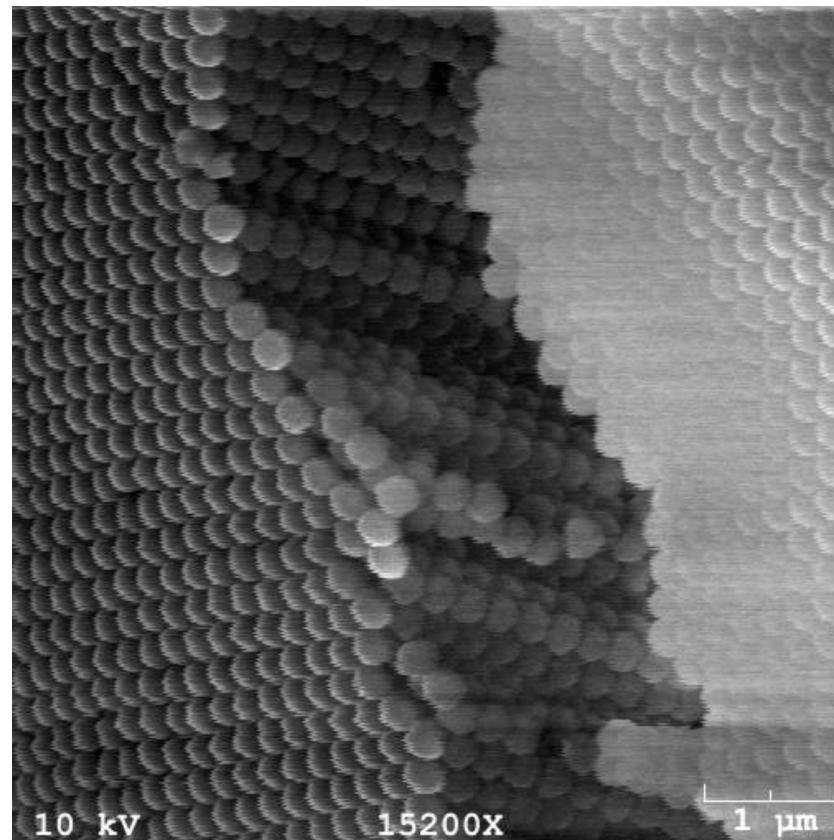
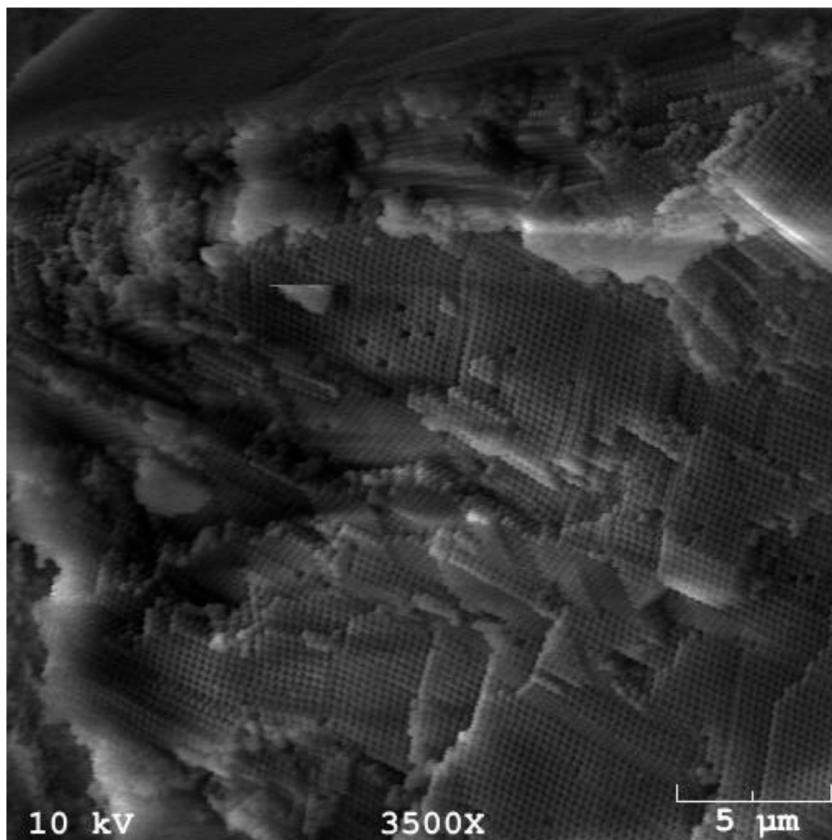
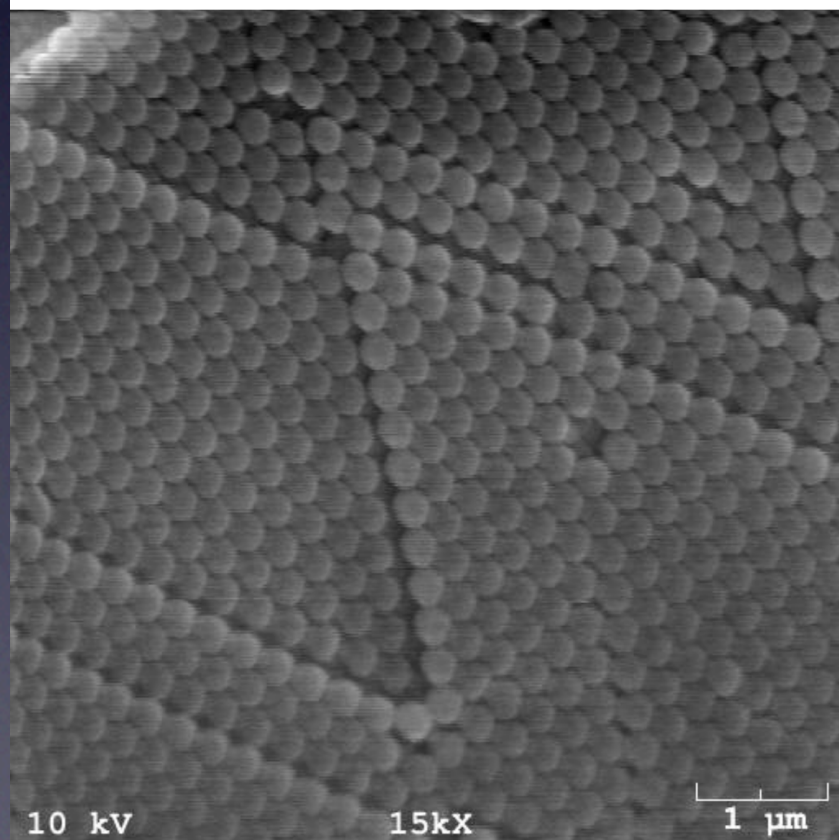
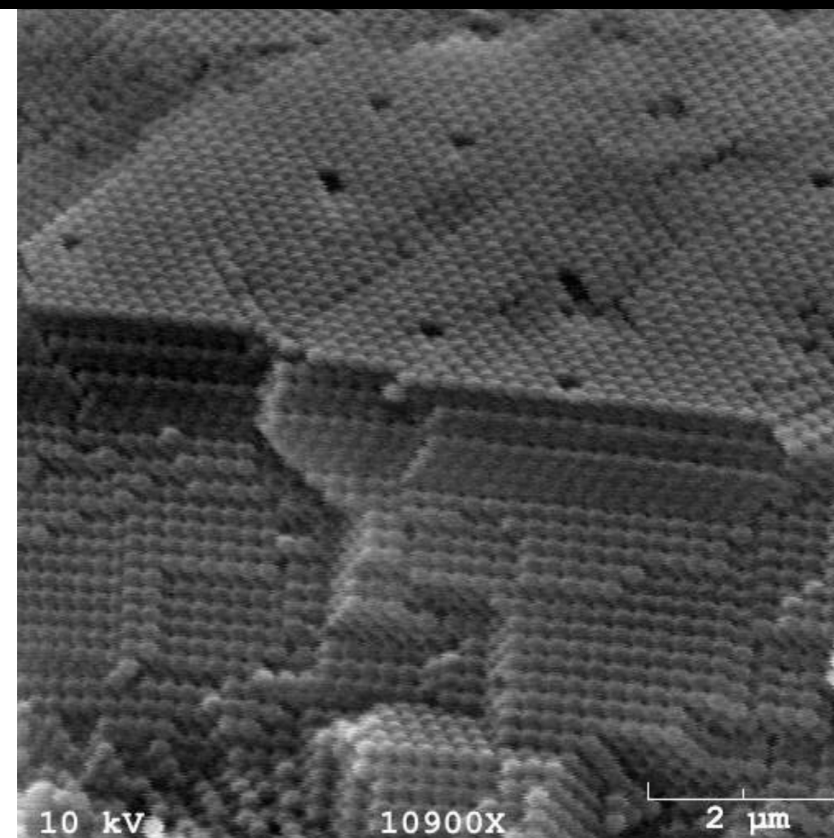
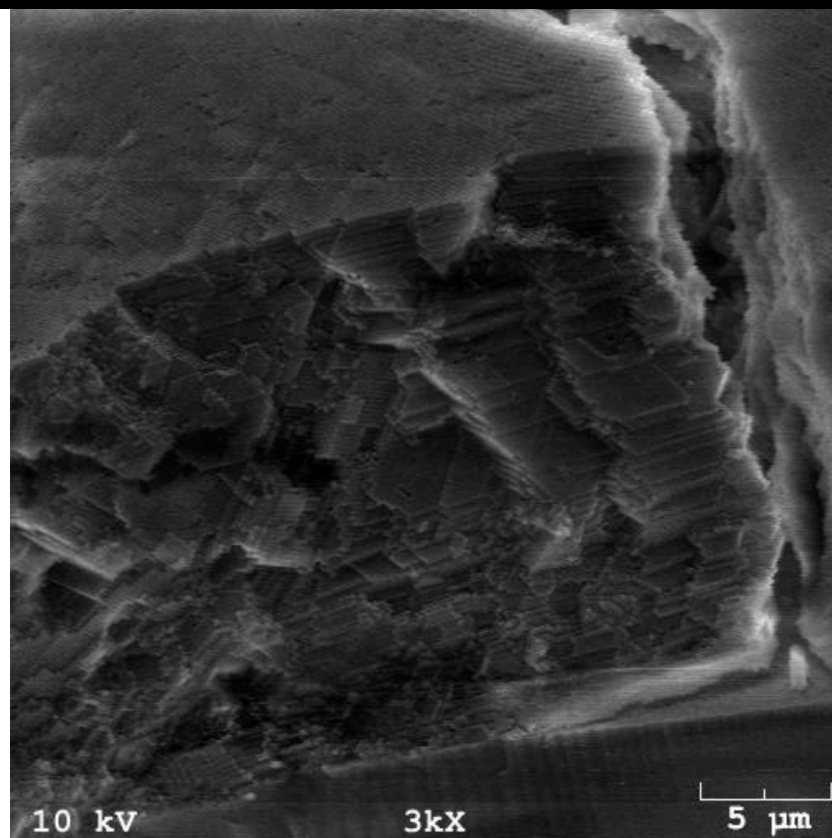
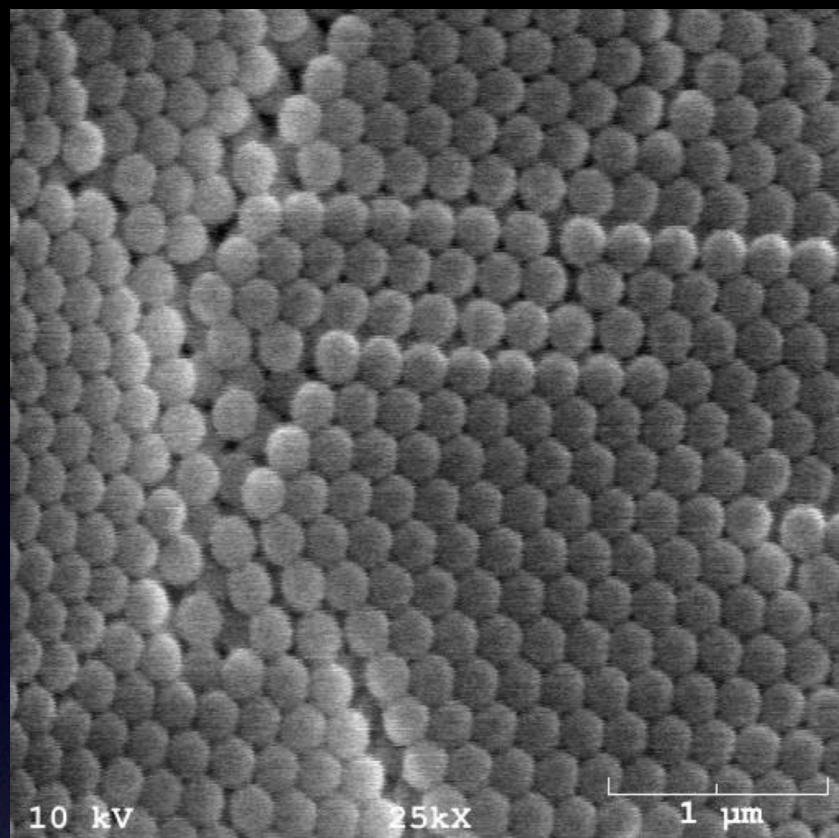


# Photonic Inks

Hard/soft core/shell latexes spontaneously assemble upon drying.

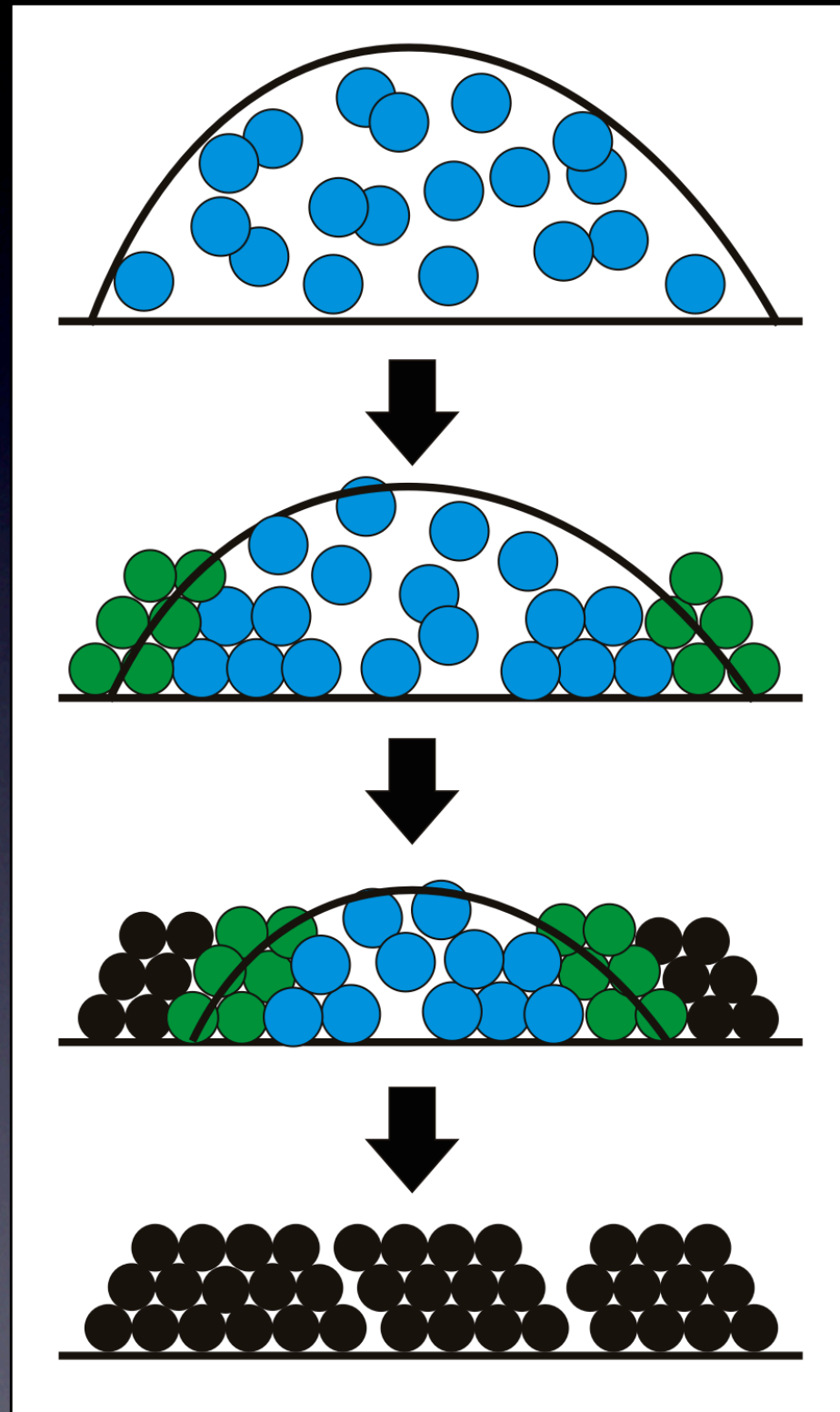
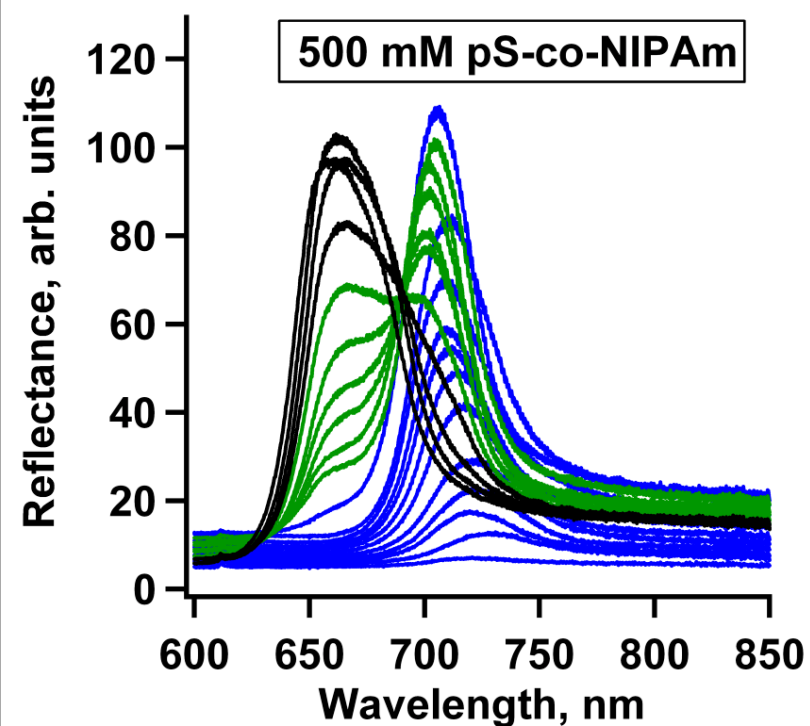
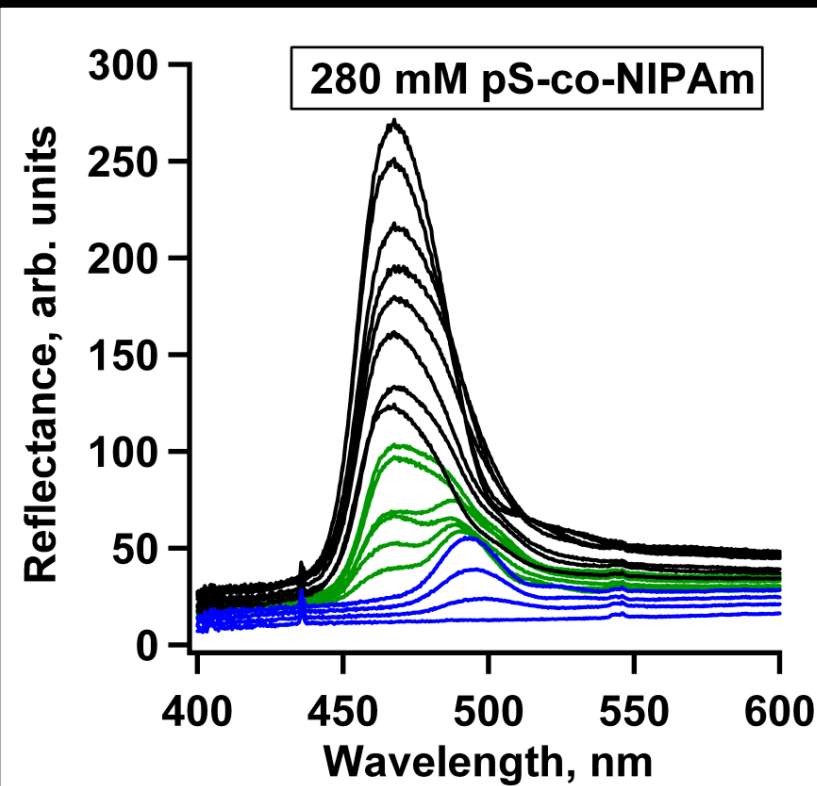








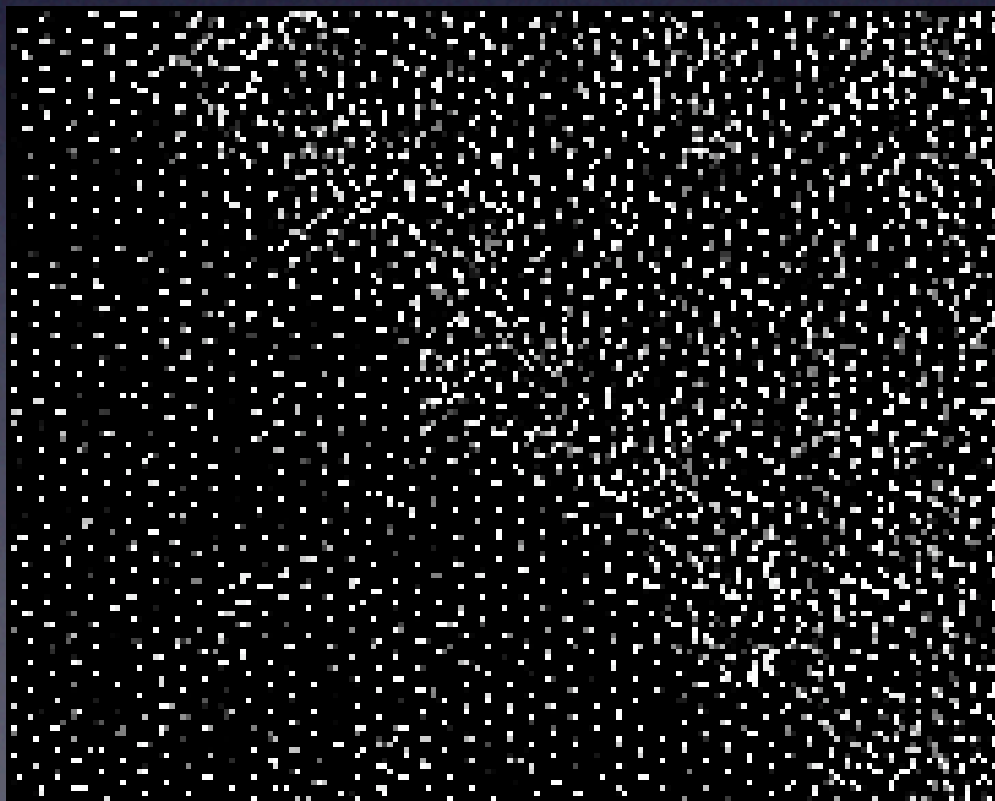
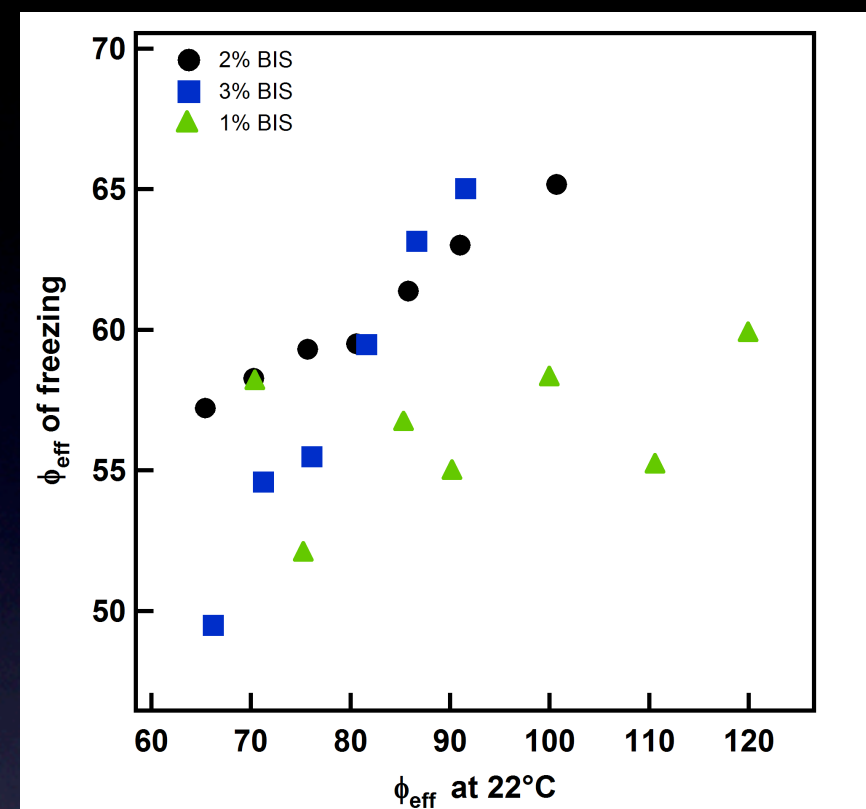
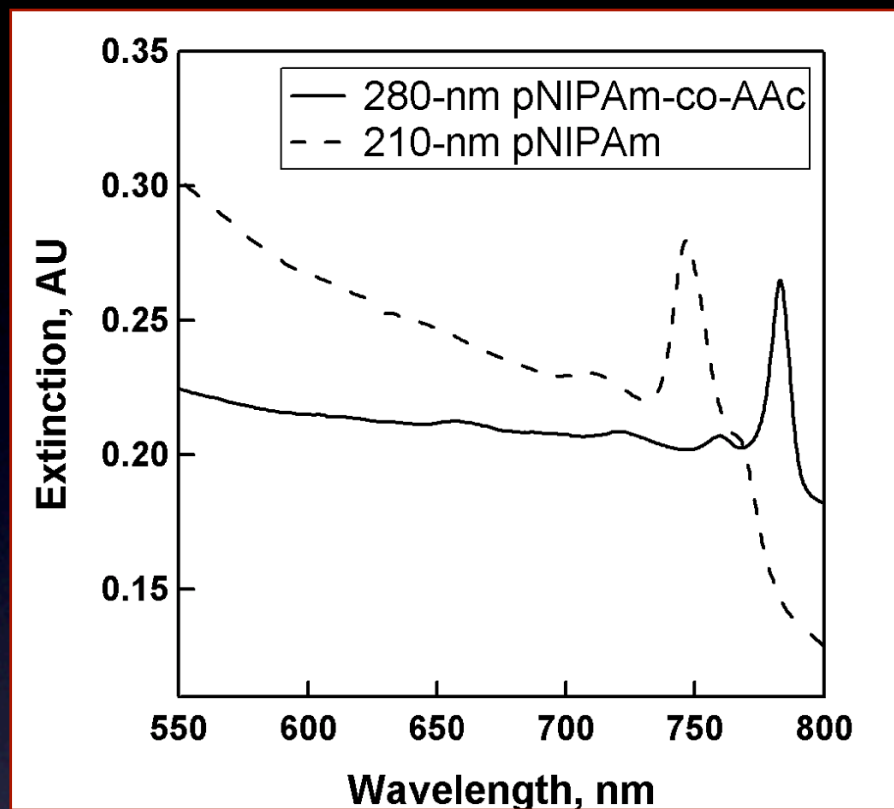
# Assembly Process



Dynamic transition from soft (repulsive) to soft (attractive, pNIPAm entanglement + hydrophobic) to hard (repulsive; polystyrene).



# Conclusions





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